### THE UNIVERSITY OF MANITOBA

## INFLUENCE OF TUBE INCLINATION ON THE FLOW-REGIME BOUNDARIES OF CONDENSING FLOWS: EXPERIMENTAL AND ANALYTICAL STUDIES

By Thambiayah Nitheanandan

A Thesis Submitted to the Faculty of Graduate Studies in partial fulfillment of the requirements for the degree of **Doctor of Philosophy** 

Department of Mechanical and Industrial Engineering Winnipeg, Manitoba



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# INFLUENCE OF TUBE INCLINATION ON THE FLOW-REGIME BOUNDARIES OF CONDENSING FLOWS: EXPERIMENTAL AND ANALYTICAL STUDIES

BY

#### THAMBLAYAH NITHEANANDAN

A Thesis submitted to the Faculty of Graduate Studies of the University of Manitoba in partial fulfillment of the requirements for the degree of

DOCTOR OF PHILOSOPHY

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### ABSTRACT

Flow-regime data of condensing steam inside an inclined 13.4-mm I.D. tube are presented. The effect of upward and downward inclinations within ±10° on the different transition lines is discussed. In all test runs, complete condensation was achieved inside the condenser, with or without a full-tube condition at the exit depending on the total mass flow rate and the inclination angle. It is shown that the zones occupied by the wavy and slug regimes experience significant shifts, whereas the effect on the annular-flow boundary appears to be insignificant at the present small inclination angles. The present data sets are compared with adiabatic gas-liquid flow-regime maps developed analytically and experimentally for horizontal and inclined tubes. Deviations due to the condensation process are observed; however, consistent trends are identified among the two types of flow. For small inclinations the trend shown by condensing flow in the horizontal position is similar to the trend shown by gas-liquid flow with a slight upward inclination. The occurrence of slugging in the horizontal condenser was found to be coincident with the condition of tube running full at the exit. When the tube was not running full at the exit. slugging was not observed. A simple correlation was developed for the upper bound on slugging. This correlation agreed well with the experimental data.

A mechanistic model was developed for determining the stratified boundary for condensing flows in horizontal and slightly inclined tubes based on mass, momentum and energy conservation laws. Two formulations, namely a complete and a simplified version are considered for the equilibrium liquid level. Good agreement is found between the two

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formulations and generalized results were derived from the simplified version of the model. From these results, the effect of condensation is shown to be equivalent to adding a small upward inclination in adiabatic gas-liquid flow. The predicted transition line is compared with flow-regime data of different fluid properties, tube diameters, and inclinations. The predictions showed good agreement with horizontal and inclined flow data of different fluids and tube diameters.

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# NOMENCLATURE

А	= cross-sectional area of the tube, m <sup>2</sup>
Ā	= dimensionless tube cross-sectional area
$A_{G}$	= cross-sectional area occupied by the vapor phase, m <sup>2</sup>
$\overline{A}_{G}$	= dimensionless vapor cross-sectional area
A' <sub>G</sub>	= vapor cross-sectional area above the wave crest, $m^2$
A <sub>L</sub>	= liquid cross-sectional area, m <sup>2</sup>
$\overline{A}_{L}$	= dimensionless liquid cross-sectional area
$C_{Gf}$	= coefficient given in Equation (5.11b)
$C_{Lf}$	= coefficient given in Equation (5.11a)
$C_{pL}$	= liquid specific heat, J/kg.K
$C_{3\mathrm{G}}$	= distribution parameter of the vapor defined in Equation (5.5a)
$C_{3L}$	= distribution parameter of the liquid defined in Equation (5.5b)
D	= tube diameter, m
$D_G$	= vapor hydraulic diameter, m
$\overline{D}_{G}$	= dimensionless vapor hydraulic diameter
DL	= liquid hydraulic diameter, m
$\overline{D}_{L}$	= dimensionless liquid hydraulic diameter
E	= parameter defined by Equation (5.18)

F = modified Froude number defined in Equation (5.30)

- $F_B$  = Bernoulli force per unit surface area, N/m<sup>2</sup>
- $F_a$  = gravitational force per unit surface area, N/m<sup>2</sup>
- F<sub>v</sub> = reaction force per unit surface area due to momentum change during condensation, N/m<sup>2</sup>
- $f_G = vapor friction factor defined by Equation (5.11b)$
- $f_L$  = liquid friction factor defined by Equation (5.11a)
- G = total mass flux,  $kg/m^2$ .s
- $G_1$  = liquid mass flux, kg/m<sup>2</sup>.s
- $G_{G}$  = vapor mass flux, kg/m<sup>2</sup>.s
- g = gravitational acceleration,  $m/s^2$
- $G_N$  = mass flux entering the liquid due to condensation, kg/m<sup>2</sup>.s
- H = dimensionless condensation heat-transfer parameter defined by Equation (5.15g)
- $h_{G}$  = vapor height, m
- $h'_{G}$  = vapor height above the wave crest, m
- $h_L = liquid height, m$
- h<sub>L</sub> = dimensionless equilibrium liquid height
- $h_{av}$  = average heat-transfer coefficient, W/m<sup>2</sup>.K
- h<sub>fa</sub> = latent heat of vaporization, J/kg
- $h'_{fg}$  = modified latent heat defined in Equation (5.17), J/kg
- $j_{G}$  = dimensionless vapor velocity defined by Equation (4.4)
- $j_{L}^{*}$  = dimensionless liquid velocity defined by Equation (4.5)
- $k_L$  = liquid thermal conductivity, W/m.K

m = coefficient in Equation (5.11b)

- m = mass flow rate, kg/h
- n = coefficient in Equation (5.11a)
- P = local static pressure,  $N/m^2$
- $P_{av}$  = mean saturation pressure, N/m<sup>2</sup>
- $(\Delta p)_{N}$  = pressure change due to mass transfer, N/m<sup>2</sup>
- q" = average heat flux, W/m<sup>2</sup>
- $Re_{GS}$  = vapor superficial Reynolds number defined by Equation (2.2c)
- $Re_{LS}$  = liquid superficial Reynolds number defined by Equation (2.2b)
- R<sub>SM</sub> = minimal liquid hold up within a liquid slug

 $S_{G}$  = vapor perimeter, m

- S<sub>G</sub> = dimensionless vapor perimeter
- S<sub>i</sub> = interfacial perimeter, m
- S<sub>i</sub> = dimensionless interfacial perimeter
- $S_L$  = liquid perimeter, m
- $\overline{S}_{I}$  = dimensionless liquid perimeter
- $T_s$  = local saturation temperature, °C
- T<sub>s. av</sub> = mean saturation temperature, °C
- $\Delta T$  = saturation to wall temperature, °C
- u<sub>G</sub> = local vapor velocity, m/s
- $\langle u_G \rangle_G$  = vapor velocity averaged over the vapor phase, m/s
- u<sub>i</sub> = mean interfacial velocity, m/s

u<sub>L</sub> = local liquid velocity, m/s

 $\langle u_1 \rangle_1$  = liquid velocity averaged over the liquid phase, m/s

V<sub>GS</sub> = superficial vapor velocity, m/s

V<sub>LS</sub> = superficial liquid velocity, m/s

 $v_{GN}$  = mean vapor velocity normal to the interface, m/s

- $v_{LN}$  = mean liquid velocity normal to the interface, m/s
- $\dot{W}_i$  = mass flow rate crossing the interface per unit volume, kg/m<sup>3</sup>.s
- X = Lockhart-Martinelli parameter defined in Equation (5.15e)

x = vapor quality

- Y = dimensionless inclination parameter defined by Equation (5.15f)
- Z = axial coordinate along the tube axis, m
- Z = dimensionless axial coordinate along the tube axis

#### **Greek letters**

- $\alpha$  = local void fraction
- $\beta$  = parameter defined by Equation (5.15b)
- $\beta'$  = parameter defined by Equation (5.20a)
- $\gamma$  = parameter defined by Equation (5.15c)
- $\gamma'$  = parameter defined by Equation (5.20b)
- $\epsilon$  = parameter defined by Equation (5.15a)
- $\zeta$  = parameter defined by Equation (5.15d)
- $\eta$  = interfacial momentum transfer parameter
- $\theta$  = tube inclination from horizontal

- $\mu_L$  = liquid dynamic viscosity, N.s/m<sup>2</sup>
- $v_{G}$  = vapor kinematic viscosity, m<sup>2</sup>/s
- $v_L$  = liquid kinematic viscosity, m<sup>2</sup>/s
- $\rho_G$  = vapor density, kg/m<sup>3</sup>
- $\rho_L$  = liquid density, kg/m<sup>3</sup>
- $\tau_i$  = average interfacial shear stress, N/m<sup>2</sup>
- $\sigma$  = surface tension, N/m
- $\tau_{wG}~~$  = average wall shear stress on gas phase, N/m²  $\,$
- $\tau_{\text{WL}}$  ~ = average wall shear stress on liquid phase, N/m²  $\,$

#### Chapter 1

### INTRODUCTION

The flow of condensing fluids inside tubes occurs in a wide range of engineering applications. Numerous examples of these applications can be found in the power generation, refrigeration, process, air-conditioning and spacecraft industries. In the power-generation industry, condensers play an important role in providing the low-temperature heat sink required in the operation of power cycles. During postulated Loss of Coolant Accidents in pressurized-water nuclear power plants, reflux condensation provides an important heat removal mechanism in vertical inverted U-tube steam generators. In the refrigeration and air-conditioning industry, the heat absorbed from a low-temperature heat reservoir is rejected through air- or water-cooled condensing units into a high-temperature heat reservoir. In spacecrafts, where high-capacity thermal transport is required at low mass flow rates, thermal load is regulated by two-phase systems [utilizing the latent heat] operating under microgravity conditions. In chemical process industries condensing units are extensively used for fractional distillation of substances.

Such large and important uses in industry requires that condensers are designed effectively and appropriately. For an effective design of condensers, the heat, mass and momentum transport mechanisms must be properly understood. In condensers the void fraction continuously decreases until complete condensation is achieved, and the flow never fully develops as it progresses along the condensation path. As the liquid and vapor

fractions change gradually along the flow direction, the forces acting on the flow also change. A shift in the dominant forces acting on the flow is accompanied by a change in the flow regime. Consequently, the mass, momentum and heat transport mechanisms change, from one flow regime to another along the condensation path. The changing and non-developing nature of condensing flows brings about a complex interaction between the thermal and hydrodynamic characteristics of the flow. The dependence of design parameters such as the friction factor and Nusselt number on the flow regimes of condensing flows has been illustrated [ Bell *et al.*, 1970; Sardesai *et al.*, 1981; Nitheanandan *et al.*, 1990 ]. Therefore, flow-regime prediction has been identified as an essential part of the design process in condensing flows.

A hydrodynamically coupled transport mechanism motivated several studies of flow-regime transition in adiabatic and diabatic flows [Soliman, 1986; Barnea and Taitel, 1986]. The adiabatic gas-liquid flow studies covered, to some degree, the effects of tube diameter, fluid properties and tube inclination. The diabatic studies involving condensation, however, are only confined to a variety of tube diameters, fluid properties and flow rates in the horizontal position.

One interesting aspect of the studies on condensing vapor flows is that there is consistent disagreement between adiabatic flow-regime maps and the location of visually observed flow regimes during condensation, especially in the slug and wavy regimes. The continuously changing void fraction, liquid level and flow velocities have been attributed to this disagreement [ Rashwan and Soliman, 1987; Rahman *et al.*, 1985 ]. The disagreement between the adiabatic gas-liquid flow maps and the flow-regime data of

condensing flows prompted the development of flow-regime maps exclusively for condensing vapor flows [ e.g., Brebar *et al.*, 1980; Soliman, 1986; Gupta *et al.*, 1986 ]. All these flow-regime maps dealt only with the horizontal orientation of the tube.

Rahman *et al.* (1985) postulated that the increasing liquid depth in a horizontal condenser is similar to an adiabatic gas-liquid flow provided a small upward inclination is given to the tube. This similarity between slightly inclined adiabatic gas-liquid flow maps and the horizontal condensing flow regime data, at least in trend, was demonstrated by Rahman *et al.* (1985).

This thesis is motivated by the need for extending the state of knowledge [ both experimentally and theoretically ] to the effect of tube inclination on the flow regime transitions during condensation. In doing so, it will be possible to explain the discrepancy between the results from adiabatic flow and those from condensing flow. In more explicit terms, the objectives of the present study are:

- (a) to develop new experimental data on the flow regimes of condensing steam inside a tube with different angles of upward and downward inclinations, including the horizontal orientation [ no similar data is available yet in the literature ],
- (b) to determine the effect of inclination on the flow regime boundaries of condensing flows,
- (c) to compare the new data with the existing correlations for gas-liquid flows in order to obtain improved understanding of the possible relationships [ in magnitude and trend ] between the regime boundaries of the two types of

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flow,

- (d) to develop a generalized theoretical model for the transition boundary between the stratified and nonstratified flows during condensation inside horizontal and slightly inclined tubes, and
- (e) to compare the new model with data of different tube diameters, fluid properties, and tube inclinations in order to demonstrate the capability of the model.

#### Chapter 2

### LITERATURE REVIEW

Two-phase flow occurring inside tubes is generally classified based on the presence [ diabatic flow ] or absence [ adiabatic flow ] of heat transfer through the tube wall. Adiabatic gas-liquid flows occurring in horizontal, vertical and inclined tubes have been subjected to several experimental and analytical studies. The primary objective of the experimental studies was to observe and map-out the flow regimes for different cross-sectional geometries, fluid properties, and inclinations. Based on the broad base of experimental data, analytical and empirical flow-regime transition correlations have been formulated. The empirical correlations are limited to the range of experimental conditions on which the correlations were based. On the contrary, the analytical correlations may be extrapolated [ with caution ] to conditions where no data are available. By contrast, the data base for condensing flow regimes does not include any information about the effects of tube inclination.

In this chapter the existing condensing flow-regime data and the flow-regime maps [ analytical and empirical ] are discussed. This discussion is followed by a review of pertinent adiabatic gas-liquid maps developed for horizontal and inclined tubes.

#### 2.1 Condensing Flow-Regime Data

A number of studies have been directed towards experimentally generating data

on the condensing flow-regime transitions. A major portion of these data were reported by Soliman and Azer (1971, 1974), Traviss and Rohsenow (1973), Fuji *et al.* (1976), Tandon *et al.* (1983), Rahman *et al.* (1985), and Rashwan (1987). These data sets cover a tube inside-diameter range of 4.8 to 37.6 mm and five working fluids [R-11, R-12, R-22, R-113 and steam]. The test condensers used in these studies were double pipe heat exchangers where the condensing fluid flowed through the inner tube while the coolant [water was used in all experiments as the coolant] flowed through the outer jacket. Short visual observation sections were installed at a number of locations along the test condenser to enable visual observation of the flow regimes. The thermodynamic quality existing at each of the visual sections was calculated based on a heat balance application. All these data correspond to horizontal flow.

The flow-regime classification used by investigators in the condensing-flow studies were generally consistent. Seven major flow regimes and three transitional flow regimes were identified. The sequential development of these flow regimes in a condenser from the inlet to the outlet is shown in Figure 2.1. The seven major flow regimes are mist flow, annular flow, semiannular flow, wavy flow, slug flow, stratified flow and plug flow. The three transitional flow regimes are mist-annular flow, annular-wavy flow and semiannular-wavy flow. Visual classification of the transitional flow regimes were often difficult and subjective. Therefore, special techniques, such as the use of a stroboscope, were required to slow the flow down to make objective identification of these flow regimes. The descriptions used by investigators to classify the major and the transitional flow regimes are [ see Figure 2.2 ]:







**Mist flow**: No stable liquid film was apparent. Most of the liquid phase was entrained by the vapor in the form of a mist.

**Annular flow**: A stable liquid film covered the entire tube wall, while the vapor flowed in the core. Part of the liquid phase was entrained by the vapor. Asymmetry was apparent in the liquid film with the maximum thickness being at the bottom of the tube.

**Semiannular flow**: The flow had an appearance similar to the annular flow, except that the stable film did not cover the entire wall periphery. A small portion of the upper half of the tube appeared dry, while the liquid film thickness increased to a maximum at the bottom.

**Wavy flow**: The two phases were separated, with the liquid flowing at the bottom of the tube. The velocity difference between the vapor and liquid caused the liquid surface to be wavy. The wavelength increased with the decrease in quality. A draining thin film may appear on the upper half of the wall periphery.

**Slug flow**: The flow was basically wavy; however, surface waves grew frequently forming slugs wetting the upper tube wall. The slugs travelled at high speeds and the frequency of their occurrence depended on the flow conditions.

**Stratified flow**: Liquid flowed at the bottom of the tube and vapor at the top with a smooth interface. This flow regime existed mainly near the exit of the condenser in cases where the mass flux was small.

**Plug flow**: The flow appeared as a single-phase liquid flow with the intermittent appearance of large vapor plugs at the upper tube wall. Vapor plugs were irregular in shape, different in size and appeared to be flowing at the same velocity of the liquid.

**Mist-annular flow**: Intermittent liquid films appeared but were swept away after their appearance to become part of the mist.

Annular-wavy flow: The flow had the annular appearance but the thickness of liquid increased at the bottom forming a thick stratum.

**Semiannular-wavy flow**: The flow had the semiannular appearance but with a thick stratum flowing at the bottom of the tube. A fraction of the upper half of the tube was still covered by a stable liquid film.

#### 2.2 Condensing Flow-Regime-Transition Correlations

#### 2.2.1 Flow-regime maps

A number of flow-regime maps were developed for horizontal condensers. Among them, Soliman and Azer (1974) proposed two different maps; one of them used the vapor mass flux, G<sub>G</sub>, and the ratio of liquid and vapor mass fluxes, G<sub>L</sub>/G<sub>G</sub>, as coordinates. The second map proposed by the above authors used the average velocity of the liquid phase,  $\langle u_L \rangle_L$ , and [  $(1 - \alpha)/\alpha$  ] as coordinates. The third map, suggested by Breber *et al.* (1980), used the nondimensional vapor velocity, j<sub>G</sub>\*, and the Lockhart-Martinelli parameter, X, as coordinates. A fourth map, suggested by Tandon *et al.* (1983) used j<sub>G</sub>\* and [  $(1 - \alpha)/\alpha$  ] as coordinates.

The generality of the full-map approach in predicting all flow regime transitions in a condenser is not currently accepted. It was recognized that every flow regime is uniquely dominated by a single dominant force. A shift in the dominant force results in a change in flow regime. Therefore, attempting to define transition boundaries in maps based on two fixed coordinate axes tend to predict one or more transitions relevant to these axes adequately while showing highly unacceptable performance in other transitions. More recent studies [ Fathi, 1980; Rahman, 1983; Rahman *et al.*, 1985; Soliman, 1986 ] compared the available flow-regime data with the existing condensing flow-regime maps and found the full-map approach to be inadequate in defining all the transitions occurring in a condenser. Consequently, attempts were made to correlate each transition boundary individually.

#### 2.2.2 Individual Analytical Correlations

Three analytical correlations for flow-regime transition in horizontal condensers were reported by Soliman (1982 and 1983) and Rashwan and Soliman (1987). These three correlations are for the annular-to-wavy, mist-to-annular, and wavy-to-slug transitions, respectively. The first two correlations were compared with the existing flow-regime data by Rahman *et al.* (1985) and Rashwan (1987). The wavy-to-slug transition correlation was compared with the available data by Rashwan and Soliman (1987). Satisfactory results were obtained in all comparisons.

#### (a) The Mist-to-Annular Transition

Soliman (1983) developed a correlation for the mist-to-annular transition based on a force balance between the dominant destructive force and the stabilizing forces. The inertia force of the vapor was assumed to be the dominant destructive force acting on the liquid film, while the surface tension and liquid viscous forces were the major stabilizing forces. A modified Weber number was formulated based on a balance between the vapor inertia, liquid viscosity, and surface tension forces. Based on comparisons with the

experimental data, it was concluded that the mist-annular transition can be characterized by the modified Weber number for different fluid properties and tube diameters. Annular flow corresponded to Weber numbers below 20 and mist flow corresponded to Weber numbers greater than 30.

#### (b) The Annular-to-Wavy Transition

This transition line, developed by Soliman (1982), marks the shift from vapor-shearcontrolled flow into gravity-controlled flow. The hypothesis adopted in that analysis was that the annular-wavy transition occurs when the Froude number, which is a measure of the ratio of inertia to gravitational forces, reached a certain value. The resulting formulation for Froude number was compared with ten data sets and it was found that the annular-wavy transition coincided with a constant value of Froude number of about seven.

#### (c) <u>The Wavy-to-Slug Transition</u>

Rashwan and Soliman (1987) developed a theoretical model for the wavy-to-slug transition in condensing fluids inside horizontal tubes. The authors observed that the surface waves seemed to be travelling upstream and downstream when the tube was running full at the exit, in the horizontal tube. The interaction between the upstreamtravelling and the downstream-travelling waves resulted in a hydraulic jump. In the absence of a full tube at the exit the surface waves appeared to be travelling downstream only and as a result no slugging was observed. Based on these observations they characterized the flow upstream of the slugging location as supercritical and the downstream flow as subcritical. The slugging location was determined analytically when

the flow transits from supercritical flow to subcritical flow. The model showed good agreement with the available horizontal tube data.

#### 2.3 Adiabatic Flow-Regime-Transition Correlations (Empirical)

#### 2.3.1 Horizontal Flow

Among the most popular flow-regime maps used in horizontal gas-liquid flows are those suggested by Baker (1954) and Mandhane *et al.* (1974). Both maps used dimensional coordinates: Baker(1954) used  $G_{g}$  and  $G_{L}/G_{g}$  as coordinates with correction factors for physical properties, while Mandhane *et al.* (1974) used the gas superficial velocity  $V_{gs}$ , and the liquid superficial velocity,  $V_{Ls}$ , as coordinates. Based on a total of 5,935 observations, a map was proposed by Mandhane *et al.* (1974) which was shown to be an average of the flow regime maps proposed by Hoogendoorn(1959), Baker (1954), and Govier and Omar (1962). Mandhane *et al.* (1974) proposed correction factors to account for the effects of fluid properties on the transition boundaries.

#### 2.3.2 Inclined Flow

Several experimental studies have been reported with gas-liquid flows inside inclined tubes. Based on these experimental studies, a number of flow-regime maps have been developed. The gas-liquid flow regimes in horizontal and downward inclined tubes  $[0^{\circ}, -1^{\circ}, -5^{\circ}, -10^{\circ}, -30^{\circ}, -50^{\circ}, -70^{\circ}, -80^{\circ}, and -90^{\circ}]$  were experimentally studied by Barnea *et al.* (1982) using 2.55-cm and 5.1-cm I. D. pipes. The flow regimes were determined by visual observation and by conductivity probes. The experimental data were compared with the theoretical model suggested by Taitel and Dukler (1976). The theoretical prediction

of the intermittent-to-annular transition agreed with the data for up to about 10°. Within this range of inclination, Barnea *et al.* (1982) found that the intermittent-to-annular transition is best described by  $h_L/D = 0.35$ , rather than  $h_L/D = 0.5$  as suggested by Taitel and Dukler (1976). The model of Taitel and Dukler (1976), however, predicted the stratified-to-nonstratified transition in the whole range, i.e. 0° to -90°, of downward inclination satisfactorily.

Experimental data in 2.5-cm and 3.8-cm I. D. tubes with a two-phase mixture of refrigerant 113 as the test fluid were obtained by Crawford *et al.* (1985). An adiabatic test section was used in this experiment. Flow regimes were visually observed at downward angles of -90°, -60°, -45°, -30°, and -15° with the 2.5-cm tube, whereas only the -90° downward angle was tested with the 3.8-cm tube. The horizontal flow-regime transition conditions developed by Weisman et al. (1979) and Weisman and Kang (1981) were compared with the experimental data. Based on the comparisons, the annular and dispersed flow conditions for horizontal flow predicted the regime transition in downward inclinations satisfactorily. In the bubble-to-intermittent and separated-to-intermittent transitions, however, small modifications were applied to the horizontal correlations for satisfactory predictions.

Flow-regime data for upward inclined tubes [ at 0,  $+0.25^{\circ}$ ,  $+2^{\circ}$ ,  $+10^{\circ}$ ,  $+20^{\circ}$ ,  $+50^{\circ}$ ,  $+70^{\circ}$ , and  $+90^{\circ}$  ] were reported by Barnea *et al.* (1985). Experiments were conducted in 2.5-cm and 5.1-cm I.D. tubes. The data were compared with the horizontal and slightly inclined flow correlation [ Taitel and Dukler, 1976 ] and the vertical upward flow correlation [ Taitel *et al.*, 1980 ]. They hypothesized that the transition mechanisms in the whole

range of inclinations from -90° to +90° change gradually as the angle of inclination is changed gradually. For small inclinations, the Taitel and Dukler (1976) model adequately predicted the transition boundary, however, at large inclinations modifications were applied. When the inclinations were large, certain transition mechanisms became inoperative. For example, they observed that the bubbly flow regime did not occur for angles below 60°. Hence, a model to predict the limiting condition for the existence of bubbly flow became important. Small upward inclinations had a major effect on the transition from stratified-to-intermittent flow and on the transition from stratified-to-annular flow. Even for small angles [ less than 1° ], the stratified boundary shrank to a small bell-shaped region and the intermittent flow occupied the region previously occupied by stratified flow.

Mukherjee and Brill (1985) developed empirical transition correlations to predict the flow regimes in pipes at all possible inclinations. Experimental data were obtained using kerosene and lubricating oil as test fluids in a U-shaped, 3.81-cm I.D. steel pipe. Their empirical regime-transition correlations were obtained from a nonlinear regression analysis conducted on the test data.

The experimental trends observed by Mukherjee and Brill (1985) agreed with the observations made by Barnea *et al.* (1982 and 1985). For example, the stratified flow envelope increased as the downward inclination was increased from horizontal to -30°. In the downward flow, slug flow was observed only at high gas flow rates, whereas in the upward flow, slug flow expanded towards low liquid flow rates at the expense of stratified flow. The inclination angle had insignificant influence on the annular-mist boundary.

Kokal and Stanislav (1989) conducted flow-regime, liquid-holdup and pressure-drop studies in 25-m long test sections with 25.8-mm, 51.2-mm, and 76.3-mm I. D. tubes. The experimental set up was able to incline the test section within  $\pm 10^{\circ}$  from the horizontal. The flow regimes were observed visually and using volume sensor traces. The regime transitions were modelled and compared with the data. A dimensionless momentum equation developed by Taitel and Dukler (1976) was modified by using the friction-factor correlation given by Chen (1984). Taitel and Dukler (1976) used Blasius' equation to calculate the friction factors and assumed the interfacial friction factor was approximately equal to the gas friction factor. Kokal and Stanislav (1989) calculated the interfacial friction factor using the Ellis and Gay (1959) correlation. With these modifications, the stratified-nonstratified transition was derived analytically.

#### 2.4 Adiabatic Flow-Regime-Transition Correlations (Theoretical)

A generalized analytical model based on physical mechanisms was proposed by Taitel and Dukler (1976) for predicting all flow regime transitions in horizontal and nearhorizontal gas-liquid flows. The model defined specific physical mechanisms responsible for a given flow regime to exist. From these mechanisms analytical expressions were developed to define the transition boundaries.

Five basic regimes were considered important: stratified smooth, stratified wavy, intermittent [ slug and elongated bubble ], annular and dispersed bubble. Starting from a stratified equilibrium flow, a dimensionless momentum equation was derived. This equation determined the equilibrium liquid level as a function of two dimensionless
groups.

The stratified flow was assumed to be a basic flow configuration. When a given condition is satisfied, the flow changes from stratified to another regime. The mechanisms which cause these changes were expressed in terms of four dimensionless groups. Therefore, in order to locate a flow regime, only two dimensionless parameters are required for any given inclination. The model incorporated the effects of gas and liquid flow rates, physical properties of the fluids, pipe diameter and the angle of inclination on the transition boundaries.

Barnea (1986) suggested a unified model for all angles of inclination that can successfully predict the annular-to-intermittent flow transition in gas-liquid flow. Two mechanisms were considered in deriving this unified model; first the instability of the liquid film due to liquid drainage near the wall blocking the entrance, and the second, the blockage of the gas core due to a large supply of liquid in the film. Both of these mechanisms are applicable only outside the range of stable stratified flow.

Transition mechanisms for each individual flow regime boundary for the whole range of pipe inclinations were presented by Barnea (1987). This comprehensive model incorporated the models suggested by Taitel and Dukler (1976) and Barnea *et al.* (1982 and 1985). The authors demonstrated reasonable success against experimental data.

One of the most important transitions for the present investigation is the transition from stratified [ or wavy ] to nonstratified [ annular, slug and bubble ] flow. The stratified-nonstratified correlations of Barnea (1987), Mukherjee and Brill (1985), and Kokal and Stanislav (1989) are compared at  $-5^{\circ}$ ,  $-1^{\circ}$ ,  $0^{\circ}$  and  $+1^{\circ}$  inclinations in Figures 2.3, 2.4, 2.5,





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and 2.6, respectively. All three correlations predict a shrinking stratified region as the inclination increases from -10°. This trend agrees well with the trend observed in the experiments. The agreement among correlations in predicting the transition boundary is very good at low liquid superficial velocities, however, slight differences appear as the liquid superficial velocity increases beyond 0.1 m/s.

This review of existing adiabatic gas-liquid correlations and the experimental observations provide an insight into the different mechanisms that were assumed to be important in flow regime transitions. These physical mechanisms were based on experimental observation of the flow. Experimental methods have also shown that the flow regime is a function of several variables, such as fluid properties, flow rates, tube orientation, and tube size. Although several flow-regime-transition models have been proposed for the whole range of inclinations in the adiabatic gas-liquid flows, there are no studies [ analytical or empirical ] available that have investigated the effect of inclination on condensing flows. The condensing flow data that are available in the published literature deal only with the horizontal orientation. Therefore, the effect of inclination on condensing flow-regime transitions has been identified as the major objective of the present study.





### Chapter 3

# EXPERIMENTAL TEST FACILITY AND PROCEDURE

An experimental investigation was conducted to generate condensing flow-regime data in inclined tubes. As part of this experimental investigation, a test facility was designed and constructed. The experiment was conducted in a 13.4-mm I. D. tube with steam as the test fluid. Seven data sets were generated; three data sets each in the upward and downward inclinations, and one data set in the horizontal position. The objectives of the experimental investigation were:

- To obtain new flow-regime data in the upward [ +1°, +5°, and +10°], downward [ -1°, -5°, and -10° ], and in the horizontal positions. Attention is directed towards studying the effect of tube inclination on the flow-regime transitions during condensation.
- 2. To observe and record the sequence of flow-regime development under a range of mass flow rates inside the tube. The principal aim will be to locate the boundaries between the different flow regimes occurring in each inclination.
- 3. To investigate the upper bound for the slugging phenomenon during condensation.

# 3.1 The Steam Circuit

The test facility, shown schematically in Figure 3.1, is a closed-loop circuit on the test fluid [ steam ] side. A heat-exchanger-type boiler produced controllable amounts of steam from distilled water using a regulated supply [ at a pressure of about 780 kPa ] of building steam as a heat source. The degree of superheat in the steam entering the test section was controlled by a superheater installed downstream from the boiler. The superheater is basically a double-pipe heat exchanger [ 3-m long ] with the test fluid flowing inside the inner tube and the building steam flowing countercurrently inside the outer jacket. Type K copper tubing with 37.6-mm I.D. and 41.3-mm O.D. was used for the inner pipe, and 49.8-mm I.D. and 54.0-mm O.D. tubing was used for the outer pipe. The superheater was insulated with a 40-mm thick fiberglass insulation. The flow of building steam into the superheater was regulated by a needle valve. This provided some control over the degree of superheat of the test fluid.

Following the superheater, the flow was directed to a precondenser. This component was found to be necessary in previous investigations where large-diameter test condensers were used and it was desirable to achieve complete condensation within the test condenser. However, the precondenser was never engaged in the present experiment and the flow was channelled directly from the superheater to the test condenser.

A detailed description of the condenser is provided in a later section. The pressure at the test-condenser inlet was measured by a calibrated "USG" Bourdon-tube pressure gauge and the temperature was measured by a 20-gauge copper-constantan





thermocouple. The steam at the inlet of the test condenser was always in the superheated region. The pressure and temperature at the outlet of the test condenser were measured using a calibrated "Ashcroft" Bourdon-tube pressure gauge and a 20-gauge copper-constantan thermocouple, respectively. Complete condensation was always achieved in the test condenser during this experiment.

Downstream of the test condenser, a vapor-liquid separator was installed to receive the condensate. This component was found to be necessary in previous investigations in order to separate the vapor and liquid when complete condensation was not achieved in the test condenser. In this experiment, the separator was used as a liquid accumulator. It was basically a 42.4-L copper tank with a 309-mm long sight glass to indicate the height of the liquid inside, and covered on the outside by 63.5-mm thick fiberglass insulation. The outflow of liquid from the separator was controlled by a valve, and hence by adjusting the opening of this valve a steady liquid level can be achieved in which case the liquid flow rates into and out of the separator would be equal. Thus, measuring the rate of flow leaving the separator would give the total steam mass flow rate through the test condenser. This was done by two calibrated "Fischer and Porter" variable-area-type flowmeters with maximum capacities of 30.3 and 157 cm<sup>3</sup>/s. Either one of these flowmeters was used in any particular test run. An aftercooler was installed in the line between the separator and the liquid flowmeters. This insured liquid subcooling and avoided any possible flashing in the flowmeters. Each flowmeter was provided with a copper-constantan thermocouple immediately upstream. This allowed the measurement of condensate temperature for the purpose of evaluating the density at the flowmeters.

After measuring the flow rate, the condensate was discharged into a liquid receiver. The liquid receiver was 48.8 L in capacity provided with a sight glass to monitor the liquid level. The main purpose of the receiver was to insure a steady liquid supply to the circulating pump. The circulating pump is a single-speed, 0.56 kW centrifugal pump with a by-pass line used for returning the condensate back to the boiler.

The steam circuit described above was tested against leaks using compressed air. It proved to be leakproof up to a pressure of 400 kPa. Before the start of the experiments, the system was evacuated, then charged with steam and then re-evacuated. This was necessary to insure the absence of air or any noncondensable gases in the circuit during tests.

# 3.2 Test Condenser

The test section, shown in Figure 3.2 consisted of six copper, double-pipe heat exchangers, each followed by a visual section. The first four heat exchangers [ labelled A, B, C, and D ] were 0.61-m long, whereas the last two [ labelled E and F ] were 0.46-m long. The steam flowed in the inner pipe and the cooling water flowed countercurrently in the outer jacket. For all units, the inner pipe was type-K copper tubing, 13.4-mm I.D. and 15.9-mm O.D. The outer pipe was 18.9-mm I.D. and 22.2-mm O.D. All heat exchangers were covered by a layer of insulation in order to minimize heat losses to the surroundings.

Each visual section contained a 15-cm length of standard clear-glass tubing. The construction details of a typical visual observation section are shown in Figure 3.3. The



Figure 3.2 Schematic of the 13.4-mm I.D. test section.



visual sections consisted of high pressure glass tubes supported on both ends by a stuffing box to prevent leakage. Throughout the test section [ heat exchangers and visual sections ], the inside diameter was maintained uniform at 13.4 mm. Care was exercised in ensuring reasonable concentricity and coaxiality of the test section segments [ heat exchangers and visual sections ]. An insulated, straight length of 30 diameters was provided at the inlet and outlet sides of the test condenser in order to minimize end effects.

# 3.3 Measurement of Inclination Angle

The test section was mounted on a beam truss, shown schematically in Figure 3.4. Each test-section segment was clamped to the beam truss with two adjustable fixtures [Figure 3.5]. These adjustable fixtures provided sufficient flexibility for any level adjustments required between the beam truss and the test section. The beam truss was pivoted at the centre and was constructed with sufficient rigidity for minimum deflection at the two free ends. At the centre of the truss, a 13-mm thick [26.6-cm x 30-cm] steel plate was bolted. Two journal bearings were fixed to this steel plate, as shown in Figure 3.6. A 43-mm diameter steel shaft was passed through the journal bearings to provide rotational flexibility about the axis of the shaft. Slippage between the shaft and the journal bearings was prevented by a key inserted between them. The shaft was supported at both ends by self-aligning end bearings mounted on a pair of columns. The entire weight of the test section, visual section, adjustable fixtures and the steel truss was supported by these two vertical columns. On one end of the two supporting columns the shaft was





Figure 3.5 Construction details of the adjustable fixtures.



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Figure 3.6 Construction details at the centre of the truss beam.

extended to protrude by 75 mm, where an adjustable "platform mount", shown in Figure 3.7, was securely bolted. This piece was necessary in order to support a surveying level. The "platform mount" and the shaft were bolted such that both of them rotated without any slippage. A surveying level was bolted to the "platform mount", as shown in Figure 3.8. A graduated surveyor's staff rod was placed at a distance [B] from the axis of the shaft, as shown in Figure 3.9. The smallest graduation available on the staff rod is 1 mm. Therefore, the uncertainty in measuring the elevation of the test section can be assumed to be  $\pm 1$  mm. With the surveying level, a datum height was obtained when the test section, the beam truss, the "platform mount" and the surveying level were placed in the horizontal position. The axis of the shaft and the line of sight of the surveying level were ensured to lie in the same plane. Any inclination introduced to the test section rotates the surveying level about the axis of the shaft. As a result, the line of sight in the surveying level rotates about the axis of the shaft, as shown in Figure 3.9, by an angle equal to the inclination of the test section, thereby giving a new elevation reading on the staff rod. The difference between the current staff rod reading and the datum [ value obtained in the horizontal position ] gives the vertical height [ A ]. The angle of inclination of the test section was obtained by  $\theta = \tan^{-1} (A/B)$ .

# 3.4 The Cooling Water Circuit

A separate loop was used to supply cooling water to the test section and aftercooler. This circuit was designed to permit complete control on the flow rate of coolant to the aftercooler and each condensing unit. City water was used as the coolant









for this experiment in an open-circuit arrangement.

The circuit starts at a 190-litre surge tank provided with an overflow line to avoid any possible flooding. The water was circulated through the circuit by a 7.457-kW turbine pump with a maximum head of 155 m of water and a maximum discharge of 142 L/min. Downstream from the pump, a by-pass line was used to adjust the total rate of water supply to the cooling system. Parallel feed lines were installed to supply water to each condensing unit and the aftercooler. Each of these lines was provided with a check valve to avoid back-flow. The water leaving the condensing units and aftercooler was allowed to discharge into a common drain.

To control the cooling water flow rate to each unit of the test condenser and the aftercooler, a valve was installed in each of the upstream and downstream lines of these heat exchangers. The upstream valves were all kept wide open, and the flow rate was controlled by adjusting the downstream valves. This resulted in higher pressure in the cooling water and consequently prevented any possible boiling. The following instrumentation was provided to record the mass flow rate and the temperature rise across each heat exchanger. The first three condensers [ A, B, and C ] used "Fisher and Porter" variable-area type flowmeters. The maximum capacities of these flowmeters were 26.2 L/min, 25.7 L/min, and 16 L/min, respectively. The next two condensing units [ D and E ] used "Brooks" variable-area type flowmeters having a maximum capacity of 15.5 L/min. The last condensing unit F used a "Fisher and Porter" variable-area flowmeter with a maximum capacity of 9.8 L/min. All these flowmeters were calibrated before their use. The temperature at the inlet and outlet of each condensing unit was measured by 20-

gauge, copper-constantan thermocouples. A "Leeds and Northrup" digital potentiometer [ model 914 ] was used to measure the outputs of these thermocouples.

# 3.5 Experimental Procedure

For every data set representing a specific tube inclination, a number of test runs were conducted and the main variable changed from one test to the other was the mass flow rate of the test fluid. The flow regime was observed at each visual section in all test runs. Another important variable was the mass flow rate of cooling water flowing into the individual condenser units. By adjusting the cooling water flow rates it was possible to change the qualities, and possibly the flow regimes, at the different visual sections while keeping the steam flow rate approximately constant. The pressure in the test condenser depended on the flow rates of steam and coolant, hence it was not an independent variable. In order to calculate the inlet enthalpy of the steam it was necessary to maintain superheated conditions at the inlet end of the test condenser; however this superheat was not considered an experimental variable. In each data set, experimentation commenced from the lowest possible mass flow rate of steam through the test section and continued until the maximum possible steam flow was achieved while ensuring enough data were collected so that the transition lines between different flow regimes were established with reasonable confidence.

### 3.5.1 The Start-up Procedure

The following procedure was followed to prepare the experimental set-up for any particular test run:

- 1. The digital potentiometer was switched on.
- 2. The cooling water surge tank was filled to the overflow level.
- The cooling water circulating pump was turned on with its by-pass valve fully open.
- The valves upstream and downstream of each condensing unit were turned to the wide open position.
- 5. The by-pass valve of the cooling water circulating pump was partially closed to force the water to flow into the test condenser and aftercooler.
- The downstream values on the drain line of each condensing unit as well as the aftercooler were adjusted to establish the desirable flow rate and pressure of the cooling water.
- The building steam, after regulating its pressure, was allowed to flow through a valve into the boiler coil.
- The valves downstream of the separator [ condensate line ] were all closed.
- 9. When steam started flowing into the test condenser, the bleeding valve on top of the separator was gradually opened allowing air and noncondensable gases to ventilate out of the system. This valve was then closed.
- 10. When the liquid in the separator reached half level, the downstream valves [ condensate line ] were partially opened to allow the

condensate to flow into the appropriate flowmeter.

- 11. When the separator became half full, the condensate circulating pump was turned on with its by-pass valve continuously adjusted to maintain a constant liquid level in the liquid receiver and the boiler.
- 12. The flow rate of building steam into the boiler coil and superheater, cooling water flow rates, condensate flow rate out of the separator and rate of condensate flow back to the boiler were all adjusted continuously until steady-state conditions were achieved.

### 3.5.2 Steady-State Conditions

Before assuming that steady-state conditions were achieved in any test run, the following readings must have remained unchanged for at least 1/2 hour:

- 1. Liquid levels in the separator, liquid receiver and the boiler.
- 2. Pressure in the boiler.
- 3. Pressures at inlet and outlet of the test condenser.
- 4. Temperatures at condenser inlet, in the separator, and inlet and outlet [ cooling water ] of each condensing unit.
- 5. Flow rate of cooling water to each condensing unit.
- 6. Flow rate of condensate out of the separator.
- 7. Observed flow regime at each visual observation section.

Typically, the system required at least 2½ hours before steady state conditions could be reached.

# 3.5.3 <u>Recording of Data</u>

After steady-state conditions were established the following readings [ taken in British units and later converted to SI units ] were recorded in order:

- 1. The boiler pressure in psig.
- 2. The building steam pressure in psig.
- 3. Test condenser inlet and outlet pressures in psig.
- 4. Test condenser inlet temperature in °F.
- 5. Condensate temperature in the separator in °F.
- 6. Condensate temperature upstream of the flowmeter in °F.
- Cooling water flow rates to each unit of the test condenser in either L/min or percentage of maximum reading.
- Cooling water temperatures upstream and downstream of the condensing units in °F.
- 9. Condensate flow rate in percentage of maximum reading.

In addition to the above readings, the flow regime at each visual observation section was identified and recorded by a sketch and a detailed written description. The flow regime development from the inlet to the outlet of the test condenser was sketched separately for each test run.

# 3.5.4 The Shut-Down Procedure

In order to shut-down the experimental facility after recording of data and flow regime observations, the following procedure was followed:

1. Building steam to the boiler and superheater was shut down.

- When the boiler pressure dropped to near atmospheric, the flow of steam to the test condenser was stopped.
- 3. The condensate circulating pump was turned off.
- 4. The by-pass value of the cooling-water circulating pump was turned wide open, then the pump was switched off.

## 3.6 Data Reduction

The data recorded during the experiments of the present investigation were reduced on a Personal Computer using FORTRAN 77 language. The computer first calculated the rates of heat gained by the cooling water and the heat lost by the steam in the test condenser. Knowing the thermodynamic state [ pressure and temperature ] at the inlet and outlet of the test condenser, the flow rate of the test fluid, as well as the flow rate and temperature rise of the cooling water in each heat exchanger, it was possible to perform an overall energy balance on the whole condenser. Based on these values, the percentage heat balance error was evaluated as { rate of heat lost by steam - rate of heat gained by cooling water } / { rate of heat lost by steam } x 100. Only test runs with a heat balance error within ±10% were accepted. The operating pressure in the test condenser,  $P_{\rm av}$ , was calculated as the average of the inlet and outlet pressures. The average saturation temperature,  $T_{\rm s,av}$ , was evaluated corresponding to the operating pressure,  $P_{\rm av}$ . The operating conditions and heat balance errors for all the accepted runs are tabulated in Appendix A.

With the rate of heat transfer determined for each of the condenser units, it was possible to calculate the quality of the test steam at each of the visual sections from

simple heat balances following the procedure described by Fathi (1980). Once the quality was determined, the superficial liquid and vapor velocities were calculated at each visual section. All fluid properties needed in these calculations were determined at the operating pressure  $P_{av}$ . A list of the observed flow regimes, as well as the corresponding qualities, mass fluxes, and mean saturation temperatures is given in Appendix B.

### Chapter 4

# EXPERIMENTAL RESULTS AND DISCUSSION

# 4.1 Test Range and Experimental Uncertainty

The range of operating conditions for each of the seven data sets is given in Table 4.1. An attempt was made to keep the number of flow-regime classifications to a minimum. Four flow regimes were identified in this study. The descriptions used in classifying these regimes [ listed below for completeness ] are consistent with previous gas-liquid and condensation studies [ see Figure 2.2 ].

**Annular Flow**: A stable liquid film covered the entire tube wall, while the vapor flowed in the core. Part of the liquid phase was entrained by the vapor. Asymmetry was apparent in the liquid film with the maximum thickness being at the bottom of the tube.

**Annular-Wavy Flow**: The flow had annular appearance with a thin continuous film covering the top part of the tube; however, the thickness of liquid film increased at the bottom forming a thick stratum. A crucial feature of this classification is that the liquid height at the bottom had to exceed one quarter of the tube radius.

**Wavy Flow:** The two phases were separated with the liquid flowing at the bottom of the tube. Waves of different length and amplitude appeared at the vapor-liquid interface.

**Slug Flow**: The flow is basically wavy; however, surface waves grew frequently forming slugs wetting the upper tube wall. These slugs were pushed downstream by the vapor at a velocity much higher than the mean velocity of the remaining liquid. Frequency

Table 4.1 Range of operating conditions

\*.

Data Set	Inclination Angle	Mass Flux, G (kg/m².s)	System Pressure, P <sub>av</sub> (kPa)	Saturation Temp., T <sub>s.av</sub> (°C)	Superficial Vapor Velocity, V <sub>GS</sub> (m/s)	Superficial Liquid Velocity, V <sub>Ls</sub> (m/s)
Śwa	0 (horizontal)	21.9 - 273	99.9 - 182	99.6 - 117	0.10 - 200	0.018 - 0.29
2	1°(upward)	25.4 - 240	102 - 160	100 - 113	0.60 - 178	0.02 - 0.25
ო	ស	22.4 - 277	102 - 165	100 - 114	0.17 - 200	0.02 - 0.28
4	10°	47.1 - 262	106 - 168	101 - 115	0.37 - 184	0.02 - 0.27
വ	- 1°(downward)	32.9 - 223	102 - 154	100 - 112	0.10 - 185	0.02 - 0.23
Q	- 50	39.2 - 242	103 - 156	100 - 113	0.29 - 185	0.02 - 0.25
7	-10°	32.5 - 207	108 - 154	102 - 112	0.70 - 160	0.02 - 0.21

-

of formation for these slugs depended on flow conditions.

In the present study, flow-regime identification was mostly based on visual observations using the above descriptions. The distinguishing features among the annular, wavy, and slug flow regimes are so clearly identifiable that objective classification was possible without difficulty. On the other hand, the distinction between annular and annular-wavy was often hard to make with just visual observation. In these cases, an electronic stroboscope was used to visually slow down the flow and allow for a more confident classification. Visual observation is the most commonly used method of flow-regime identification [ e.g., Traviss and Rohsenow, 1973; Barnea et al., 1982; Tandon et al., 1983; Crawford et al., 1985; Barnea et al., 1985; Mukherjee and Brill, 1985 ].

A total of 395 test runs were performed in this investigation, out of which 90% of the test runs had heat balance errors within  $\pm 5\%$  and the remaining 10% of the test runs had heat balance errors within  $\pm 8\%$ . The flow regime data [ total of 1139 points ] obtained in this investigation will be presented in the form of flow regime maps using the superficial velocities V<sub>LS</sub> and V<sub>GS</sub> as coordinates. The superficial velocities were calculated using,

$$V_{LS} = G(1 - x)/\rho_L, \qquad (4.1)$$

and

$$V_{GS} = G \chi / \rho_G . \tag{4.2}$$

# Uncertainty estimates in the calculated values of $V_{LS}$ and $V_{GS}$ were determined for

all data points using the method described by Moffat (1988) based on 95% confidence levels, or 20/1 odds. For all data points, the uncertainty in V<sub>LS</sub> was estimated to lie within ±5.3%. A major portion of the data [ 855 points, or 75.1% ] corresponds to V<sub>GS</sub> ≥ 20 m/s. Out of this portion, 66.2% of the data points have uncertainties in V<sub>GS</sub> within ±5% and 32.2% have uncertainties in V<sub>GS</sub> outside ±5% but within ±10%. For the remaining data [ 284 points, or 24.9% ] corresponding to the low velocity range V<sub>GS</sub> < 20 m/s, uncertainty in V<sub>GS</sub> is generally outside ±10%. However, the magnitudes of estimated errors in V<sub>GS</sub> have an average value of ±2.1 m/s and never exceed ±2.8 m/s. The details of the uncertainty estimates are given in Appendix C. The inclination angle of the test section was measured as described in Chapter 3 using a surveying level. The uncertainty in measuring this angle is estimated to be within ±0.03°.

#### 4.2 Flow Condition at the Condenser Exit

Complete condensation was always achieved in the test section before discharging the flow into the separation tank where liquid and vapor existed with a stable interface. For the horizontal orientation and the three upward inclinations of  $+1^{\circ}$ ,  $+5^{\circ}$ , and  $+10^{\circ}$ , the condenser tube was always running full at the end of the condensation path. On the other hand, the full-tube condition was achieved only beyond certain flow rates with the downward inclinations even though complete condensation was achieved at all flow rates. For example, at 1° downward inclination [Figure 4.1], the discharging flow was stratified for all mass fluxes G < 58 kg/m<sup>2</sup>. s [corresponding to terminal velocities at the end of the condensation path of V<sub>LS</sub> < 0.052 m/s], and the tube ran full only for G > 58 kg/m<sup>2</sup>. s. In



the present experiment, the exit condition of stratified or full-tube was found to be independent of the rate of cooling and dependent only on the discharge flow rate [ Wallis et al., 1977 ]. The boundary between stratified and full-tube condition shifted to higher mass flow rates as the inclination angle increased; in  $-5^{\circ}$  [ downward ] inclination the stratified boundary coincides approximately with G = 128 kg/m<sup>2</sup>. s, whereas in  $-10^{\circ}$  [ downward] inclination the stratified boundary shifts to approximately G = 151 kg/m<sup>2</sup>. s. The tube condition at exit was found to be a major factor in determining whether or not slugging would occur, as discussed in the following section.

# 4.3 Effect of Inclination on the Flow-Regime Boundaries

The present results for the seven data sets are shown in Figures 4.2 - 4.8. For the horizontal orientation, Figure 4.2 shows that the wavy flow regime is limited to a small bell-shaped area. For small mass fluxes of G < 65 kg/m<sup>2</sup>. s [ corresponding to terminal velocities at the end of the condensation path of V<sub>LS</sub> < 0.058 m/s ], the flow regime progresses from annular to annular-wavy to wavy to slug before complete condensation with a full tube is achieved. With intermediate mass fluxes within 65 < G < 157 kg/m<sup>2</sup>. s [ corresponding to terminal velocities within 0.058 < V<sub>LS</sub> < 0.14 m/s ], wavy flow was not observed and the flow regime progressed from annular to annular-wavy to slug followed by complete condensation. Interestingly, slug flow was not observed in test runs with high mass flow rates corresponding to terminal velocities V<sub>LS</sub> > 0.14 m/s. Consistent with the observation by Rashwan and Soliman (1987), the occurrence of slugging in the present experiment always coincided with the full-tube condition at the end of the condensation



path. The upper limit [  $V_{LS} \approx 0.14$  m/s ] for slug initiation will be considered analytically in a later section.

The most significant effect of inclination observed during this experiment was on the wavy and slug flow regime boundaries. The bell-shaped wavy flow region, observed in the horizontal position [ Figure 4.2 ], disappears completely in the 1° upward inclination [ Figure 4.3 ]. Higher angles of inclination [ 5° and 10° ] produced small changes in the transition lines, as shown in Figures 4.4 and 4.5. The tube was always running full at the end of the condensation path for all test runs with upward inclination of 1° or higher. This coincided with the occurrence of slugging in all test runs with terminal velocities below the upper limit of V<sub>LS</sub> ≈ 0.14 m/s. It is interesting to note that this upper limit for slug initiation appears to be independent of inclination for angles below 10°.

In downward inclination, however, the area occupied by wavy flow expands at the expense of the slug flow area. Figure 4.6 shows the results for -1° [ downward ] inclination. In this case, the tube was running full at the end of the condensation path only for test runs corresponding to terminal velocities  $V_{LS} > 0.052$  m/s. The slug flow for this inclination appears to be limited to flow rates with terminal velocities within the range  $0.052 < V_{LS} < 0.14$  m/s. For  $V_{LS} < 0.052$  m/s, the tube did not run full at exit and the condensation path terminated with wavy [or stratified] flow. With further increase in downward inclination to 5° and 10°, Figures 4.7 and 4.8, respectively, show that slug flow disappears completely and its zone is now occupied by wavy flow. At these inclinations, the tube started running full at exit only with flow rates corresponding to terminal velocities  $V_{LS} > 0.14$  m/s. Figures 4.7 and 4.8 also show that the shift in the transition lines is












insignificant as the downward inclination angle changes from 5° to  $10^\circ$  .

The influence of inclination [ within  $\pm 10^{\circ}$  ] on the annular flow regime boundary is much less pronounced than the influence on the wavy and slug areas. The three downward inclinations considered in this investigation produced insignificant effects on this boundary [ Figure 4.9 ]. For upward inclinations, there appears to be a slight shift in the annular flow boundary towards lower vapor velocities, particularly in the region of high liquid velocities [ Figure 4.10 ].

Another interesting feature of the results in Figures 4.2 - 4.8 is that for  $V_{LS} > 0.14$  m/s; i.e., high total mass flow rates, the flow regime is annular-wavy near the end of the condensation path and this regime exists down to  $V_{GS}$  of about 1 m/s. By contrast, significantly higher values of  $V_{GS}$  are normally required in gas-liquid flows in order to support a liquid film at the wall. Two observations can be made in order to explain this difference between the two flow situations. First, in condensing flows, liquid is naturally formed on the tube wall which is not the case in adiabatic gas-liquid flows. Secondly, at the high flow rates corresponding to  $V_{LS} > 0.14$  m/s, the heat-transfer coefficient and the rate of condensation are high, thus contributing to an increased rate of liquid formation on the tube wall and a stable annular-wavy flow regime.

### 4.4 Estimate of the Upper Bound for the Slug Region

A flow mechanism has been developed by Rashwan and Soliman (1987) for the onset of slugging in horizontal condensers. As illustrated in Figure 4.11, slugging was proposed to be initiated by a hydraulic jump as the two-phase mixture changes from











supercritical to subcritical flow due to condensation. A mathematical model based on this criterion for slug initiation succeeded in predicting the wavy-slug transition for a large segment of the available data.

Starting from the above criterion by Rashwan and Soliman (1987), the objective here is to develop a simple analytical correlation for the upper bound of the slug flow region during condensation. It is proposed that this upper bound coincides with the condition where the flow rate is high enough to prevent the transition into subcritical flow. Therefore, at this bound, the two-phase flow would be supercritical throughout the condenser and it only becomes critical at the end of the condensation path. The criticality criterion, which is also the condition for no upstream propagation of surface waves, has been commonly developed as [ e.g., Wallis, 1969 ]

$$\frac{j_G^{*2}}{\alpha^3} + \frac{j_L^{*2}}{(1 - \alpha)^3} = 1$$
 (4.3)

where,

$$j_G^* = V_{GS} \left[ \rho_G / \{ g D (\rho_L - \rho_G) \} \right]^{0.5}, \qquad (4.4)$$

$$j_L^* = V_{LS} \left[ \rho_L / \{ g D (\rho_L - \rho_G) \} \right]^{0.5} , \qquad (4.5)$$

and  $\alpha$  is the void fraction.

At the end of the condensation path, the liquid is flowing under a stagnant vapor bubble and therefore,  $V_{gs} = j_g^* = 0$ . Substituting into Equation (4.3) results in

$$V_{LS} = [gD (1 - \alpha)^3 (1 - \rho_G / \rho_L)]^{0.5}$$
(4.6)

The motion of large bubbles through stationary liquids in horizontal ducts has been investigated by Benjamin (1968) assuming negligible viscous and surface tension effects. For the two-dimensional case of flow between two parallel plates, Benjamin (1968) predicted  $\alpha = 0.5$  far downstream of the bubble nose for the flow to be steady and free from energy dissipation. For the three-dimensional problem of liquid emptying from a horizontal tube, Benjamin (1968) obtained  $\alpha = 0.42$ . There are obvious similarities between the flow at the end of the condensation path, where liquid is flowing under a stationary bubble, and Benjamin's problem, where bubbles were flowing through a stationary liquid. As well, the liquid height in horizontal and slightly inclined tubes necessary for the slug formation was discussed by Taitel and Dukler (1976). They argued that slug flow will develop only when the liquid level is at or above the pipe centreline; i.e.,  $\alpha \leq 0.5$  and they used a constant value of  $\alpha = 0.5$  at the annular-slug boundary.

It seems from the above discussion that a reasonable estimate of  $\alpha$  in Equation (4.6) is somewhere between 0.42 and 0.5. Using these limits with steam-water at an average saturation temperature of 100°C [  $\rho_{\rm G} = 0.82$  kg/m<sup>3</sup> and  $\rho_{\rm L} = 951$  kg/m<sup>3</sup> ] and the present tube diameter D = 0.0134 m, Equation (4.6) produces V<sub>LS</sub> = 0.128 m/s at  $\alpha = 0.5$  and V<sub>LS</sub> = 0.16 m/s at  $\alpha = 0.42$ . These values form a narrow band around V<sub>LS</sub> = 0.14 m/s, which was obtained experimentally at this flow-regime boundary.

### 4.5 Comparisons with Gas-Liquid Correlations

Many of the trends discussed above for condensing flows, such as the prominence of slug flow in upward inclinations, the prominence of wavy flow in downward inclinations and the relative insensitivity of the annular flow boundary to small inclinations, are consistent with the trends reported for adiabatic gas-liquid flows. The objective of this section is to perform quantitative comparisons between the present data and some of the available gas-liquid flow regime maps [ empirical and theoretical ]. Perfect agreements should not be expected from these comparisons. However, this effort can illustrate the relationship, if any, between the flow-regime boundaries of the two types of flow, which may guide future studies in this area.

A comparison between the present data for horizontal flow and the horizontal, adiabatic, gas-liquid flow-regime map proposed by Mandhane et al. (1974) is shown in Figure 4.12. The necessary property corrections, as recommended by Mandhane et al., were applied to the boundaries. Reasonable agreement can be seen in the annular flow region. However, an obvious discrepancy appears in the slug flow region where the majority of these data points fall in the stratified and wavy areas of the map.

The varying liquid height along a horizontal condenser can influence the onset of slugging in ways similar to providing a very small upward inclination to a tube carrying a gas-liquid mixture. In order to test this hypothesis, the horizontal flow data are compared in Figure 4.13 with the theoretical map for a tube with +1° [ upward ] inclination proposed by Taitel and Dukler (1976). The theoretical boundaries shown in Figure 4.13 correspond to fluid properties of a saturated steam-water mixture at 110°C and a tube diameter of 13.4 mm. Even though the present data do not fall exactly in the same areas predicted by Taitel and Dukler (1976), the similarity in trend is obvious with the wavy flow limited to a small, bell-shaped area and the prominence of slug flow at low superficial vapor





velocities. As a further test of this hypothesis, a comparison was made between the present data of -1° [ downward ] inclination and the empirical map of Mandhane et al. (1974) for horizontal, gas-liquid flow. This comparison, given in Figure 4.14, shows a much better fit in the wavy and slug regions than the one seen earlier in Figure 4.12. The slug flow data in Figure 4.14 fall above the wavy flow data, as the map stipulates, although the exact transition between the two regimes is not exactly predicted. A closer agreement may be possible with data corresponding to a slightly higher downward inclination.

For the larger inclinations of  $\pm 5^{\circ}$  and  $\pm 10^{\circ}$ , comparisons are made in Figure 4.15 for upward flow and Figure 4.16 for downward flow between the present data and the predictions of Taitel and Dukler (1976). The transition lines in Figures 4.15 and 4.16 correspond to steam-water flow at 110°C in a 13.4 mm tube. According to the present data, the annular to slug transition in upward flows and the annular-to-wavy transition in downward flows do not shift significantly as the inclination angle changes from 5° to 10°. The predictions by Taitel and Dukler (1976), plotted for both angles in Figures 4.15 and 4.16, also show small shifts in both boundaries. As well, good agreement between data and predictions can be seen in both figures suggesting that gas-liquid correlations may apply satisfactorily for condensation with larger inclinations such as 5° and 10°. However, according to the previous comparisons, care must be exercised for smaller inclinations where, there appears to be a need for theoretical flow-regime correlations specific to condensing flows.







### Chapter 5

# THEORETICAL ANALYSIS OF THE STRATIFIED-NONSTRATIFIED TRANSITIONAL BOUNDARY

The objective of this theoretical analysis is to develop a physically-based, generalized, theoretical model for the transition boundary between the stratified and nonstratified flows during condensation inside horizontal and slightly inclined tubes. Attention is focused on this boundary since the present data suggest that the most significant deviation between adiabatic and condensing flows correspond to this boundary at small inclinations. Comparisons are made in the next chapter between the present analysis and data of different tube diameters, fluid properties, and tube inclinations in order to demonstrate the capability of the model.

The presence of heat transfer along the condensation path results in a continuously varying liquid height. Therefore, the flow never becomes fully developed, contrary to the case of adiabatic, gas-liquid flow. Influences of heat transfer and flow development are considered in the present analysis.

The stratified-nonstratified boundary can be analyzed through two different approaches. The traditional approach is through the application of the classical inviscid Kelvin-Helmholtz theory to explore the departure from a stratified configuration. This approach was followed by Taitel and Dukler (1976) in their analysis of the stratifiednonstratified transition during adiabatic gas-liquid flow inside horizontal and near

horizontal tubes. The second approach involves analyzing the stability of flow on the basis of wave theory. Wallis (1969) has shown that the condition for marginal stability of a flow phenomenon is obtained when the kinematic and dynamic wave velocities become equal. Recently Brauner and Maron (1991) proposed that, in addition to the above criteria, the stability problem may also be analyzed using the well-posedness of the hyperbolic transient equations that govern the stratified flow. They have shown that the boundary of the stratified configuration can be represented by a buffer zone confined between a lower bound given by the stability of flow and an upper bound given by the well-posedness of the transient equation.

Two different approaches were attempted in the present analysis. These are the Kelvin-Helmholtz approach, later followed by Taitel and Dukler (1976), and the mathematical approach proposed by Brauner and Maron (1991). The results from both approaches were compared and found to be very close for all inclinations. Therefore, it was decided to include all derivations and results obtained from extending the approach of Brauner and Maron (1991) to condensing flows in Appendix D.

The modelling approach followed in the remaining part of this chapter, and the results presented in the following chapter, are based on extending the well-known work of Taitel and Dukler (1976) to condensing flows. First, a stratified flow condition is assumed and the equilibrium liquid level is determined from application of the appropriate conservation laws. The boundary of stratified flow is then determined by considering the mechanism by which transition from the stratified condition is expected to take place.

## 5.1 Equilibrium Liquid Level [Complete Formulation]

The one dimensional, co-current stratified flow in an inclined condenser tube is shown schematically in Figure 5.1. The flow of liquid and vapor is at equilibrium under the influences of wall and interfacial drag, gravity, acceleration, momentum transfer and pressure gradient. The flow is assumed to be steady and both phases are in thermodynamic equilibrium with constant properties. The tube has a uniform cross section along the flow direction.

An equation for the equilibrium liquid level can be derived by performing mass and momentum balances on the differential control volume shown in Figure 5.1. Considering the liquid and vapor phases separately, conservation of mass results in the following relations, respectively:

$$\rho_L \frac{\partial}{\partial Z} \left[ \langle u_L (1 - \alpha) \rangle \right] = \dot{W}_i, \qquad (5.1)$$

and

$$\rho_{G} \frac{\partial}{\partial Z} \left[ \langle u_{G} \alpha \rangle \right] = - \dot{W}_{i}, \qquad (5.2)$$

where Z is the axial coordinate along the tube axis,  $u_L$  is the local liquid velocity,  $u_G$  is the local vapor velocity,  $\alpha$  is the local void fraction, and  $\mathring{W}_i$  is the mass flow rate crossing the interface per unit volume. The angle brackets [ < > ] used in the present formulation indicate averaging over the entire cross-sectional area of the tube. After reduction, the



momentum balances applied to the liquid and vapor phases produce, respectively,

$$\frac{\partial P}{\partial Z} + g \rho_L \sin \theta + g \rho_L \cos \theta \frac{\partial h_L}{\partial Z} + \frac{\tau_{WL} S_L}{A < 1 - \alpha >} - \frac{\tau_i S_i}{A < 1 - \alpha >}$$

$$- \left[ \frac{(1 - \eta) < u_G \alpha >}{<1 - \alpha > < \alpha >} - \frac{(C_{3L} - \eta) < u_L (1 - \alpha) >}{(<1 - \alpha >)^2} \right] \frac{\partial}{\partial Z} \left[ \rho_L < u_L (1 - \alpha) > \right]$$

$$+ C_{3L} \rho_L \frac{< u_L (1 - \alpha) >}{<1 - \alpha >} \frac{\partial}{\partial Z} \left[ \frac{< u_L (1 - \alpha) >}{<1 - \alpha >} \right] = 0, \qquad (5.3)$$

and

$$\frac{\partial P}{\partial Z} + g \rho_G \sin \theta + \frac{\tau_{WG} S_G}{A < \alpha >} + \frac{\tau_I S_I}{A < \alpha >}$$

$$- \left[ \left( 1 - \eta - C_{3G} \right) \frac{\langle u_G \alpha >}{(\langle \alpha > \rangle)^2} + \frac{\eta \langle u_L (1 - \alpha) \rangle}{\langle 1 - \alpha > \langle \alpha >} \right] \frac{\partial}{\partial Z} \left[ \rho_G \langle u_G \alpha > \right]$$

$$+ C_{3G} \rho_G \frac{\langle u_G \alpha >}{\langle \alpha >} \frac{\partial}{\partial Z} \left[ \frac{\langle u_G \alpha >}{\langle \alpha >} \right] = 0, \qquad (5.4)$$

where P is the static pressure,  $\theta$  is the tube inclination,  $h_L$  is the liquid height, A is the cross-sectional area of the tube,  $\tau_{WL}$  is the average wall shear stress on the liquid phase,  $\tau_{WG}$  is the average wall shear stress on the vapor phase, and  $\tau_i$  is the average interfacial shear stress. Definitions of S<sub>G</sub>, S<sub>L</sub>, and S<sub>i</sub> are given in Figure 5.2. The coefficients C<sub>3G</sub> and C<sub>3L</sub> are distribution parameters commonly defined by [e.g., Hancox and Nicoll, 1971]



Figure 5.2 Definition of cross-sectional parameters.

$$C_{3G} = \frac{\langle \alpha \ U_G^2 \rangle}{\langle \alpha \rangle \ (\langle U_G^2 \rangle_G)^2} , \qquad (5.5a)$$

and

$$C_{3L} = \frac{\langle (1 - \alpha) u_L^2 \rangle}{\langle 1 - \alpha \rangle (\langle u_L \rangle_L)^2}, \qquad (5.5b)$$

where the symbols [ < ><sub>G</sub> ] and [ < ><sub>L</sub> ] indicate averaging over the vapor and liquid flow areas, respectively. In deriving Equations (5.3) and (5.4), the interfacial momentum transfer was formulated using the interfacial rate of mass transfer  $W_i$  and the mean interfacial velocity  $u_i$ , which was related to the averaged phase velocities by the relation [ Yadigaroglu and Lahey, 1976 ]

$$u_I = \eta < u_L >_L + (1 - \eta) < u_G >_G$$
 (5.6)

The rate of condensation can be evaluated from a simple heat balance as follows:

$$\dot{W}_{i} = \frac{4 q''}{D h_{ig}},$$
 (5.7)

where q" is the average heat flux based on the whole pipe perimeter and  $h_{fg}$  is the latent heat of vaporization. Equation (5.7) was substituted in Equations (5.1) and (5.2) and the pressure-gradient term was eliminated between Equations (5.3) and (5.4) using Equations (5.1) and (5.2) in the reduction. Thus, after algebraic manipulation, a momentum equation for the mixture was produced

$$\frac{\tau_{WL} S_L}{A_L} - \frac{\tau_{WG} S_G}{A_G} - \tau_I S_I \left[ \frac{1}{A_G} + \frac{1}{A_L} \right] + \left( \rho_L - \rho_G \right) g \sin \theta$$

$$+ \frac{\pi D q''}{A h_{fg}} \left\{ \frac{\langle u_L (1 - \alpha) \rangle}{\langle 1 - \alpha \rangle} \left[ \frac{2 C_{3L} - \eta}{\langle 1 - \alpha \rangle} - \frac{\eta}{\langle \alpha \rangle} \right] \right\}$$

$$+ \frac{\pi D q''}{A h_{fg}} \left\{ \frac{\langle u_G \alpha \rangle}{\langle \alpha \rangle} \left[ \frac{2 C_{3G} + \eta - 1}{\langle \alpha \rangle} + \frac{\eta - 1}{\langle 1 - \alpha \rangle} \right] \right\}$$

$$- \left[ C_{3L} \rho_L \frac{\left( \langle u_L (1 - \alpha) \rangle \right)^2}{\left( \langle 1 - \alpha \rangle \right)^3 A} + C_{3G} \rho_G \frac{\left( \langle u_G \alpha \rangle \right)^2}{\left( \langle \alpha \rangle \right)^3 A} \right] \left( \frac{dA_L}{dh_L} \frac{\partial h_L}{\partial Z} \right)$$

$$+ \rho_L g \cos \theta \left( \frac{\partial h_L}{\partial Z} \right) = 0 , \qquad (5.8)$$

where

$$A_G = A < \alpha > , \qquad (5.9a)$$

and

$$A_1 = A < 1 - \alpha > .$$
 (5.9b)

The shear stresses appearing in Equation (5.8) were formulated using these conventional expressions [Taitel and Dukler, 1976]

$$\tau_{WL} = f_L \frac{\rho_L (\langle u_L \rangle_L)^2}{2}, \qquad (5.10a)$$

$$\tau_{WG} = f_G \frac{\rho_G (\langle u_G \rangle_G)^2}{2}, \qquad (5.10b)$$

$$\tau_{i} = f_{G} \frac{\rho_{G} \left[ \langle u_{G} \rangle_{G} - \langle u_{L} \rangle_{L} \right]^{2}}{2} , \qquad (5.10c)$$

where the friction coefficients are given by

$$f_L = C_{Lf} \left( \frac{D_L < u_L >_L}{v_L} \right)^{-n}$$
, (5.11a)

and

$$f_G = C_{Gf} \left( \frac{D_G < u_G^{>}_G}{v_G} \right)^{-m}$$
, (5.11b)

while the liquid and vapor hydraulic diameters are given by

$$D_L = \frac{4 A_L}{S_L} , \qquad (5.12a)$$

$$D_G = \frac{4 A_G}{S_G + S_I}$$
 (5.12b)

The coefficients appearing in Equations (5.11a) and (5.11b) were set as  $C_{Lf} = C_{Gf} = 0.046$ and n = m = 0.2 for turbulent flow, and  $C_{Lf} = C_{Gf} = 16$  and n = m = 1 for laminar flow. The actual Reynolds numbers [based on the phasic flow areas] were used in determining the transition between laminar and turbulent flow.

Equations (5.10) to (5.12) were substituted into Equation (5.8), and the mixture momentum equation was further reduced using the following identities:

$$V_{LS} = \langle u_L \rangle_L \langle 1 - \alpha \rangle = \langle u_L (1 - \alpha) \rangle, \qquad (5.13a)$$

and

and

$$V_{GS} = \langle u_G \rangle_G \langle \alpha \rangle = \langle u_G | \alpha \rangle, \qquad (5.13b)$$

where  $V_{LS}$  and  $V_{GS}$  are the superficial liquid and vapor velocities, respectively. In final dimensionless form, the mixture momentum equation can be written as

$$\varepsilon X^{2} - \beta - 4 Y + \gamma H = \zeta \frac{\partial \overline{h_{L}}}{\partial \overline{Z}}, \qquad (5.14)$$

where

$$\epsilon = \left(\overline{D}_{L} \frac{\overline{A}}{\overline{A}_{L}}\right)^{-n} \left(\frac{\overline{A}}{\overline{A}_{L}}\right)^{2} \frac{\overline{S}_{L}}{\overline{A}_{L}} , \qquad (5.15a)$$

$$\beta = \left( \overline{D}_{G} \frac{\overline{A}}{\overline{A}_{G}} \right)^{-m} \left( \frac{\overline{A}}{\overline{A}_{G}} \right)^{2} \left\{ \frac{\overline{S}_{G}}{\overline{A}_{G}} + \left[ \frac{\overline{S}_{I}}{\overline{A}_{L}} + \frac{\overline{S}_{I}}{\overline{A}_{G}} \right] \left[ 1 - \left( \frac{V_{LS}}{V_{GS}} \right)^{2} \frac{\overline{A}_{G}}{\overline{A}_{L}} \right]^{2} \right\}, \quad (5.15b)$$

$$\gamma = \pi \left( \frac{V_{LS}}{V_{GS}} \right) \frac{\overline{A}}{(\overline{A}_L)^2} \left[ 2 C_{3L} - \eta \left( 1 + \frac{\overline{A}_L}{\overline{A}_G} \right) \right]$$
  
+ 
$$\pi \frac{\overline{A}}{(\overline{A}_G)^2} \left[ 2 C_{3G} - (1 - \eta) \left( 1 + \frac{\overline{A}_G}{\overline{A}_L} \right) \right], \quad (5.15c)$$

$$\zeta = \left[ \frac{2\left(\frac{\rho_L}{\rho_G}\right)}{C_{Gf}\left(\frac{V_{GS}D}{v_G}\right)^{-m}} \right] \left[ \frac{1}{\bar{A}} \left\{ C_{3L}\left(\frac{V_{LS}}{V_{GS}}\right)^2 \left(\frac{\bar{A}}{\bar{A}_L}\right)^3 + C_{3G}\left(\frac{\rho_G}{\rho_L}\right) \left(\frac{\bar{A}}{\bar{A}_G}\right)^3 \right\} \frac{d\bar{A}_L}{d\bar{h}_L} - \frac{g D \cos \theta}{(V_{GS})^2} \right],$$
(5.15d)

$$X^{2} = \frac{\frac{4 C_{Lf}}{D} \left(\frac{V_{LS} D}{v_{L}}\right)^{-n} \frac{\rho_{L} V_{LS}^{2}}{2}}{\frac{4 C_{Gf}}{D} \left(\frac{V_{GS} D}{v_{G}}\right)^{-m} \frac{\rho_{G} V_{GS}^{2}}{2}},$$
 (5.15e)

$$Y = \frac{-\left(\rho_L - \rho_G\right)g\sin\theta}{\frac{4 C_{Gf}}{D}\left(\frac{V_{GS}D}{\nu_G}\right)^{-m}\frac{\rho_G V_{GS}^2}{2}},$$
(5.15f)

and

$$H = \frac{2 q''}{h_{fg} \rho_G V_{GS} C_{Gf} \left(\frac{V_{GS} D}{v_G}\right)^{-m}} .$$
 (5.15g)

All parameters with a bar superscript in Equations (5.14) and (5.15) are nondimensionalized using the reference variables D for length, D<sup>2</sup> for area, and the superficial velocities  $V_{LS}$  and  $V_{GS}$  for the mean liquid and vapor velocities, respectively. Equation (5.14) reduces to the Taitel and Dukler (1976) model when H = 0 [ i.e., no heat transfer ] and  $\partial \overline{h_L}/\partial \overline{Z} = 0$  [ i.e., fully -developed conditions with constant liquid height ].

The term q" in Equation (5.15g) was evaluated by using an appropriate correlation that can give the condensing heat-transfer coefficient at the tube wall. In this study, a correlation by Collier (1981) was used. During stratified flow in a condenser tube, the flow experiences an adverse pressure gradient while there is considerable shear force on the liquid due to vapor flow. Collier (1981) modified Nusselt's theory by including the effect of vapor shear on the cross-sectional average heat-transfer coefficient. His modified correlation is given by

$$h_{av} = \frac{q''}{\Delta T} = E \left[ \frac{\rho_L \left( \rho_L - \rho_G \right) g h'_{fg} k_L^3}{D \mu_L \Delta T} \right]^{0.25}, \qquad (5.16)$$

where

$$h'_{fg} = h_{fg} + 0.68 (C_{P_L} \Delta T),$$
 (5.17)

 $k_L$  is the liquid thermal conductivity,  $\mu_L$  is the liquid viscosity,  $C_{pL}$  is the liquid specific heat, and  $\Delta T$  is the saturation-to-wall temperature difference. The parameter E is a correction factor given by Collier (1981) in table form and is closely represented by the following polynomial:

$$E = \langle \alpha \rangle \left[ 2.04 - 4.30 \langle \alpha \rangle + 4.45 (\langle \alpha \rangle)^2 - 1.46 (\langle \alpha \rangle)^3 \right]$$
 (5.18)

### 5.2 Equilibrium Liquid Level [Simplified Formulation]

The presence of the term  $\partial \overline{h_L} / \partial \overline{Z}$  in Equation (5.14) reflects the reality of the developing nature of the flow. However, starting from an initial condition at Z = 0, a numerical procedure is necessary in order to progress the solution along the condensation path. A simplified approach was considered whereby the term  $\partial \overline{h_L} / \partial \overline{Z}$  in Equation (5.14) was dropped and the ratio  $[V_{LS}/V_{GS}]$  was assumed negligible in Equations (5.15b), (5.15c), and (5.15d). Thus, the model reduces to

$$\varepsilon X^{2} - \beta' - 4 Y + \gamma' H = 0, \qquad (5.19)$$

where

$$\beta' = \left( \overline{D}_{G} \frac{\overline{A}}{\overline{A}_{G}} \right)^{-m} \left( \frac{\overline{A}}{\overline{A}_{G}} \right)^{2} \left\{ \frac{\overline{S}_{G}}{\overline{A}_{G}} + \frac{\overline{S}_{i}}{\overline{A}_{L}} + \frac{\overline{S}_{i}}{\overline{A}_{G}} \right\} , \qquad (5.20a)$$

$$\gamma' = \pi \frac{\overline{A}}{\left(\overline{A}_{G}\right)^{2}} \left[ 2 C_{3G} - (1 - \eta) \left( 1 + \frac{\overline{A}_{G}}{\overline{A}_{L}} \right) \right] , \qquad (5.20b)$$

and  $\varepsilon$  is given by Equation (5.15a). In this formulation,  $\varepsilon$ ,  $\beta'$ , and  $\gamma'$  are unique functions of  $\overline{h}_L$ . Therefore, for given values of X, Y, and H, Equation (5.19) can be solved algebraicly for the corresponding value(s) of  $\overline{h}_L$ . A quantitative assessment of this approach is given in the following chapter.

Of course, this approach may be considered meaningful only if it produces results close enough to those of Equation (5.14). Any deviation between the two sets of results would be due to the effect of the gradient of the interface on the equilibrium liquid level. This simplified approach, if successful, can produce generalized results of  $\overline{h}_L$  as a function of X, Y, and H. A quantitative assessment of this approach is given in the following chapter.

### **5.3 Transition Criterion**

A finite amplitude disturbance on the smooth interface between the two phases is shown in Figure 5.3. Taitel and Dukler (1976) developed [ for adiabatic gas-liquid flow ] a criterion for the condition where a finite wave amplitude would grow based on Kelvin-Helmholtz theory. The wave amplitude would grow when the gas flow rate is large





enough over the wave crest to cause a lift force [Bernoulli effect ]. Dukler (1978) proposed a transition criterion for boiling flows based on this mechanistic approach. This approach is extended to condensing flows in this study.

In condensing flows, in addition to the lift force from the vapor flow, a destabilizing effect is created by the reaction force to vapor molecules condensing on the vapor-liquid interface. The condition for the finite amplitude wave to grow is assumed to take the form

$$F_B \ge F_a - F_V , \qquad (5.21)$$

where  $F_v$  is the reaction force due to momentum change during condensation per unit surface area,  $F_B$  is the Bernoulli force due to the accelerating vapor above the wave per unit surface area, and  $F_g$  is the gravitational force per unit surface area. The gravitational force is given by

$$F_{g} = (h_{G} - h'_{G}) (\rho_{L} - \rho_{G}) g \cos \theta, \qquad (5.22)$$

where  $h_{G}$  and  $h'_{G}$  are the distances above the interface to the top surface, as shown in Figure 5.3.

The Bernoulli force can be formulated as

$$F_{B} = \frac{1}{2} \rho_{G} \left( < u_{G} >_{G} \right)^{2} \left[ \left( \frac{A_{G}}{A'_{G}} \right)^{2} - 1 \right] , \qquad (5.23)$$

where  $A_{G}$  and  $A'_{G}$  are the flow cross-sectional areas of the vapor phase where the vapor heights are  $h_{G}$  and  $h'_{G}$ , respectively.

The force due to the momentum change during condensation can be obtained through the Reynolds flux concept given by Wallis (1969). From mass continuity across the interface, we get

$$\rho_{G} V_{GN} = \rho_{L} V_{LN} = G_{N} , \qquad (5.24)$$

where  $v_{GN}$  and  $v_{LN}$  are the mean velocity components normal to the interface acting towards the liquid surface, and  $G_N$  is the mass flux entering the liquid due to condensation. It can be shown that the pressure drop  $(\Delta p)_N$  associated with this mass transfer is

$$(\Delta p)_N = G_N \left( v_{GN} - v_{LN} \right) = \left( \frac{G_N}{\rho_G} \right)^2 \left[ \rho_G - \frac{\rho_G^2}{\rho_L} \right].$$
 (5.25)

Since  $\rho_L >> \rho_G$ , the last term within the parenthesis in Equation (5.25) can be ignored. From a simple heat balance,  $G_N$  can be estimated. The reaction force due to condensation can finally be written as

$$F_V = (\Delta p)_N = \left[ \frac{\pi D q''}{h_{fg} S_i} \right]^2 \frac{1}{\rho_G} . \qquad (5.26)$$

Equations (5.22), (5.23) and (5.26) were substituted into Equation (5.21) using definition (5.15g) for the relationship between q<sup>#</sup> and H. Thus, the following formulation for the transition criterion was obtained:

$$(\langle u_{G} \rangle_{G})^{2} \geq \left\{ \frac{\left(\rho_{L} - \rho_{G}\right) g \cos \theta}{\rho_{G}} \left(h_{G} - h'_{G}\right) - \left[\frac{\pi D H V_{GS}}{2 S_{i}} C_{Gf} \left(\frac{V_{GS} D}{v_{G}}\right)^{-m}\right]^{2} \right\} \times \left[\frac{2 A'_{G}^{2}}{A_{G}^{2} - A'_{G}^{2}}\right]$$
(5.27)

For small finite disturbances,  $A'_{G}$  can be expanded in a Taylor series around  $A_{G}$  keeping only the first term of the series and ignoring the higher-order terms. Thus,

$$(\langle u_{G}\rangle_{G})^{2} \geq \left\{ \frac{\left(\rho_{L} - \rho_{G}\right) g A_{G} \cos \theta}{\rho_{G} \frac{dA_{L}}{dh_{L}}} - \left(\frac{D}{h_{L}}\right) \left[ \left(\frac{\pi D V_{GS} H}{2 S_{i}}\right) C_{Gi} \left(\frac{V_{GS} D}{\nu_{G}}\right)^{-m} \right]^{2} \right] \times \left\{ \frac{2 \left(\frac{A'_{G}}{A_{G}}\right)^{2}}{1 + \frac{A'_{G}}{A_{G}}} \right\}$$
(5.28)

Following Taitel and Dukler (1976), the first quantity between brackets on the right hand side of Equation (5.28) was approximated by  $(1 - h_L /D)^2$ . Introducing this approximation and simplifying using Equation (5.13b), we get this final form for the transition criterion

$$F^{2}\left(\frac{d\overline{A}_{L}/d\overline{h}_{L}}{\overline{A}_{G}}\right)\left(\frac{(\overline{A}/\overline{A}_{G})^{2}}{(1-\overline{h}_{L})^{2}}+\frac{1}{\overline{h}_{L}}\left[\frac{\pi}{2}\frac{H}{\overline{S}_{i}}C_{Gf}\left(\frac{V_{GS}}{\nu_{G}}\right)^{-m}\right]^{2}\right) \geq 1 \quad , \quad (5.29)$$

where,

$$F^{2} = \frac{V_{GS}^{2}}{D g \cos \theta} \frac{\rho_{G}}{\rho_{L} - \rho_{G}} , \qquad (5.30)$$

and the term  $dA_L/dh_L$  is determined from simple geometric considerations [ Taitel and Dukler, 1976 ] as,
$$\frac{d\bar{A_L}}{d\bar{h_L}} = \sqrt{1 - (2\bar{h_L} - 1)^2} .$$
 (5.31)

Computed results from the two formulations; the approximate [ given by Equation (5.19) ] and the complete [ given by Equation (5.14) ], will be compared in the following chapter. Based on the comparisons, one of the methods will be adopted to obtain the equilibrium liquid levels for condensing flows in inclined tubes. The predictions of the equilibrium liquid level will then be applied to the transition criterion. From this transition criterion, the stratified-nonstratified transition boundary will be determined for different fluid properties and tube diameters. These analytical boundaries will then be compared with the experimental data.

#### Chapter 6

# THEORETICAL RESULTS AND COMPARISONS

The boundary between stratified and nonstratified flow during condensation in horizontal and slightly inclined tubes is given by Equation (5.29). Application of this equation requires knowledge of the dimensionless liquid height h. A mechanistic model has been developed for the evaluation of  $\overline{h_L}$  with two possible formulations; a complete formulation given by Equations (5.14) and (5.15), and a simplified formulation given by Equations (5.19) and (5.20). In order to solve either formulation, suitable values for the coefficients  $C_{3G}$ ,  $C_{3L}$ , and  $\eta$  are required. Hancox and Nicoll (1971) recommended a value between 1.0 and 1.2 for the distribution coefficients  $C_{3G}$  and  $C_{3L}$ , depending on the flow regime. All results in this study were obtained with a value of 1.0 for the distribution parameters. This choice makes the present results for the special case of adiabatic flow identical to those of Taitel and Dukler (1976). A number of suggestions have been made for the momentum transfer parameter  $\eta$  ranging from 0.5 to 1.0 [ Wallis, 1969; Yadigaroglu and Lahey, 1976 ]. The interfacial velocity is influenced by the relative magnitudes of the average phase velocities and the liquid height. For small liquid heights, the interfacial velocity would be more influenced by the average velocity of the liquid because of the proximity of the wall to the interface. Similarly, near the end of the condensation path, the interfacial velocity is more likely to be closer to the average vapor velocity. Therefore, an appropriate estimate of n must take into consideration the changes in the liquid height along the flow. A simple relationship,  $\eta$  = 1 — h\_L/D, was used in

generating the present results.

In the following sections, a comparison is made between the results of the complete and the simplified formulations of the equilibrium-liquid-level model, followed by a presentation of the  $\overline{h_L}$ -results, and finally the predictions of the stratified-nonstratified transition criterion are presented and compared with experimental flow-regime data.

### 6.1 Comparison Between the Complete and Simplified Formulations

The development of  $h_L/D$  along the condensation path was obtained for the case of condensing steam at a saturation temperature of 100°C inside a tube with D = 13.4 mm for a saturation-to-wall temperature difference of 10°C. These results are presented sequentially from Figure 6.1 for  $\theta = +10^{\circ}$  [ upward ] to Figure 6.7 for  $\theta = -10^{\circ}$  [downward]. The curves corresponding to the complete and simplified formulations are marked [ CF] and [ SF ], respectively, in Figures 6.1 to 6.7. For all inclinations except the horizontal, the results cover the range of total mass flow rates  $21.6 \le \dot{m} \le 144$  kg/h, which coincides with the mass-flow range tested in the experimental investigation [ Chapter 4]. In the horizontal position the maximum value of mass flow rate tested was 1080 kg/h. This higher value of mass flow rate was used to illustrate that the CF and SF formulations are capable of providing very close results when the mass flow rates are sufficiently high.

In executing the complete formulation, it was assumed that the region  $\overline{Z} \le 0$  is adiabatic with a very small liquid height  $(h_L/D)_o = 0.005$  and that condensation starts at  $\overline{Z} = 0$ . Therefore, an initial solution [ at  $\overline{Z} = 0$  ] was established by solving Equations (5.14) and (5.15) iteratively for the adiabatic condition [  $H = \partial \overline{h}_L/\partial \overline{Z} = 0$  ], thus yielding















the corresponding initial quality  $x_o$ . The solution was then advanced along the condenser using an explicit finite-difference scheme. After numerical experimentation, it was found that the results become grid-independent with a grid size of about  $\Delta \overline{Z} = 0.001$ . Numerical experiments were also conducted in order to study the effect of the initial value  $(h_L/D)_o$  and it was found that starting from values lower than 0.005 had insignificant effect on the rest of the solution domain. For each value of  $\dot{m}$ , the solution was then advanced using Equations (5.14) and (5.15) and values of  $h_L/D$  and x were determined at each axial station  $\overline{Z}$ .

Results were also obtained from the simplified formulation using Equations (5.19) and (5.20) at the same conditions applied to the complete formulation. At each axial station, the value of x was matched for the two formulations and the value of  $h_L/D$  for the simplified formulation was determined.

Figures 6.1 to 6.7 show generally good agreement between the two solutions, particularly for  $x \ge 0.2$  and larger values of  $\dot{m}$ . The simplified formulation produced multiple solutions of  $h_L/D$  for the same x at low values of  $\dot{m}$  and x. The existence of multiple solutions for this type of formulation was discussed in a recent paper by Landman (1991), who argued that the lowest value of  $h_L/D$  at a given x is the most stable solution. Keeping that in mind, it may be concluded from Figures 6.1 to 6.7, that the simplified formulation is reasonably accurate for the present application. In most instances, the stratified-nonstratified transition was found to occur at condenser locations where the deviation between the two solutions is practically indistinguishable [Figure 6.4].

### 6.2 Equilibrium Liquid Level

The simplified formulation was solved for a wide range of parameters and the results are shown in Figures 6.8 - 6.13. Figure 6.8 corresponds to H = 0, and it is identical to the results of Taitel and Dukler (1976). Multiple solutions are predicted for the upward inclinations corresponding to Y < -4 over a range of X. With condensation, as shown in Figure 6.9 - 6.13, the influence on the results is very small for large Y-values. However, significant changes in  $h_L/D$  occur for small values of Y with multiple solutions possible for even downward inclinations. The influence of H on the results of  $h_L/D$  is consistent in trend with the introduction of an additional upward inclination on the adiabatic solution. This is further illustrated in Figure 6.14 for the horizontal orientation Y = 0. It can be seen from Figures 6.8 and 6.14 that increasing H for Y = 0 produces trends in the  $h_L/D$ -values similar to decreasing Y [ or increasing upward inclination ] for H = 0.

Examining the results in Figures 6.8 - 6.13, we note that the multiple roots for the equilibrium liquid level occur at lower values of Y as H increases. For example, multiple roots are shown for Y = -4 when H = 0 [Figure 6.8 ], whereas, at H = 1, multiple roots appear at Y = -3 [Figure 6.9 ]. This trend is seen for all values of H tested. The region of X where multiple roots appear corresponds to low qualities, as demonstrated earlier in Figures 6.1 - 6.7.

In the region of X where the equilibrium liquid level is multivalued, a maximum of three roots are possible. As H is increased, the roots with a value of  $h_L/D < 0.5$  tend to decrease in value whereas the roots with a value of  $h_L/D > 0.5$  tend to increase in value.



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Figure 6.14 Equilibrium liquid level for Y = 0.

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No attempt was made in this investigation to explain the physical meaning of having multiple values of  $h_L/D$  at the same flow parameters. It is possible that this mathematical behaviour is due to the assumed formulations of the wall and interfacial shear stresses, but does not have physical basis. This point was not explored further because the stratified-nonstratified boundary, which is the main objective of this analysis, was always found in the region where a unique solution existed.

### 6.3 Transition Criterion

The stratified-nonstratified transition criterion was applied by solving Equations (5.19), (5.20), (5.29), and (5.30) simultaneously. In order to demonstrate the trend in these results, the case of condensing steam [ Figure 6.15 ] at a saturation temperature of 100°C in a tube with 25.4-mm I.D. using  $\Delta T = 10^{\circ}$ C is compared with the adiabatic case [ Figure 6.16 ]. Both sets of results indicate that the stratified region shrinks in size as the upward inclination angle increases. This is consistent with the experimental results shown in Chapter 4, where the wavy flow regime was not observed in upward inclinations for  $V_{LS} \ge 0.02$  m/s. Considering Figures 6.15 and 6.16 comparatively indicates that for large inclinations, e.g.,  $\theta = -5^{\circ}$  and  $-10^{\circ}$ , the transition line is not significantly influenced by condensation. However, at small inclinations [ $-1^{\circ} \le \theta \le 1^{\circ}$ ], the deviation is obviously significant and it is consistent with the trend that condensation influences the transition line in a manner similar to the introduction of a small upward inclination in adiabatic flow.

#### 6.4 Comparisons with Experimental Data

Comparisons were made between the present theory and the present flow-regime







data, as well as others available in the literature for condensation of different fluids inside tubes of different diameters. A sample of these results is shown in Figures 6.17 - 6.23 for horizontal and downward inclined tubes. For upward inclinations, the present data [ which are the only available results ] did not include wavy/stratified flow.

Figure 6.17 shows the comparison between the flow-regime data of Soliman and Azer (1974) for condensing R-12 inside a horizontal 12.7-mm I.D. condenser and the stratified- nonstratified transition line based on the present analysis. The calculations are made for a saturation temperature of 27.8°C and a saturation to wall temperature difference equal to 10°C. It is clear from the figure that the present theory predicts the boundary of the wavy-flow region very well, both at the annular-wavy and the wavy-slug transitions.

Figure 6.18 shows the comparison with the data for Rashwan (1987). In producing the transition line in this figure, the saturation to wall temperature difference was selected equal to 20°C. This is a reasonable value considering the saturation temperature of steam [  $100^{\circ}$ C ] and the average cooling water temperature [  $\approx 50^{\circ}$ C ] used in Rashwan's experiment. After accounting for the thermal resistances of the cooling water and the tube wall, a reasonable estimate for  $\Delta$ T was found to be about 20°C. The data correspond to a horizontal, 25.3-mm I.D. tube. Again, the stratified-nonstratified transition line predicts the data very well.

Figure 6.19 compares the data of Traviss and Rohsenow (1973) with the present analysis. These data were obtained with R-12 condensing at  $T_s = 27.8^{\circ}$ C inside an 8-mm I.D. horizontal tube. The predictions are made with  $\Delta T = 10^{\circ}$ C. Traviss and Rohsenow





Figure 6.18 Comparisons between the present theory and data of Rashwan (1987).



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reported that wavy flow was not observed in their experiment and they only observed annular, semiannular, and slug flow. Figure 6.19 shows that the present theory is consistent with these observations.

Figure 6.20 compares the R-113 data of Soliman and Azer (1974) with the present analysis. In generating the transition line, a  $\Delta T = 15^{\circ}C$  was used. The data was obtained in a 12.7-mm I.D. horizontal tube. The transition is predicted reasonably well.

Figure 6.21 compares the present horizontal data and the transition line. A saturation to wall temperature difference equal to 20°C was used in the analysis. Although the transition line appears shifted to the left, the agreement is considered fair in view of the fact that the trend of the data is very well predicted. Figure 6.22 compares the present data at  $-1^{\circ}$  [ downward ] inclination with the analytical prediction. Although a few data points in the region V<sub>GS</sub> < 1 m/s are inadequately predicted, the agreement is considered reasonably good. Excellent agreement is shown in Figure 6.23 between the present combined data of  $-5^{\circ}$  and  $10^{\circ}$  [ downward ] inclination and the analysis. The experimental data and theory are also in agreement with the trend whereby changing the inclination from  $-5^{\circ}$  and  $10^{\circ}$  does not significantly influence the stratified-flow boundary.

It is fair to conclude from the above comparisons that the present theory for predicting the stratified-nonstratified boundary is in fairly good agreement with a wide range of experimental data.

#### Chapter 7

# CONCLUSIONS

An experimental investigation has been conducted in order to study the effect of inclination on the two-phase flow regimes of condensing flow inside a tube. The data correspond to steam at a mean saturation temperature of about 110°C condensing inside a 13.4-mm I. D. tube with inclination angles within  $\pm 10^{\circ}$ . Inside this range of inclination angles, the annular flow regime boundary experiences very small [ almost insignificant ] shifts. On the other hand, small inclinations of only 1° [ upward or downward ] from the horizontal resulted in significant changes in the wavy and slug regions. Wavy flow is more prominent in downward inclinations and slug flow is more prominent in upward inclinations boundaries due to changes in the inclination angle from 5° to 10° are found to be insignificant.

The existence of slug flow was found to coincide always with the full-tube condition at exit. If the tube was not running full at the end of the condensation path, i.e. stratified conditions at exit, slugging was not observed. Beyond a certain mass flux, which was found to be independent of inclination, slugging was not observed and the flow regime progressed from annular to annular-wavy to complete condensation with full tube. This upper bound on slugging during condensation was analyzed and the resulting simple correlation agreed well with the present data.

Comparisons with some of the available gas-liquid correlations suggested that for small inclinations [e.g.,  $\pm 1^{\circ}$ ], the present results for a given angle are consistent in trend

with those of gas-liquid flow with slight upward inclination added to the given angle. This is attributed to the increasing liquid height along the condenser. For larger angles [ e.g., 5° and 10° ], the present data agreed reasonably well in magnitude and trend with the gas-liquid correlation of Taitel and Dukler (1976).

A mechanistic model has been developed for the evaluation of the equilibrium liquid level during condensation inside horizontal and slightly inclined tubes. Basic conservation equations of mass, momentum, and energy have been applied on a differential control volume. Two possible formulations were developed; a complete and a simplified versions. The resulting values of h<sub>L</sub>/D from the two versions were compared at different inclinations and mass flow rates. Very good agreement was obtained, particularly at large mass flow rates and large qualities for all inclinations tested. The location where transition took place was found to be in the region where there was excellent agreement between the two methods. Therefore, the simplified method was utilized in predicting the equilibrium liquid levels in this study.

Using the simplified method, equilibrium liquid levels for different values of the heat transfer parameter H were generated. These curves qualitatively show that inclining the tube upward in adiabatic gas-liquid flow [ decreasing the parameter Y ] is equivalent to increasing the heat transfer parameter H. This is consistent with the condensing flow experimental observations.

A stratified [ wavy ] to nonstratified regime transition criterion for condensing flows was developed using a force balance on a finite amplitude wave. The stratified [ wavy ] transition boundary predicted by the proposed model was compared with different data

sets. It is shown that the present theory is capable of good agreement with experimental data in magnitude and trend.

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#### Appendix A

#### **OPERATING CONDITIONS AND HEAT BALANCE**

This appendix lists the operating conditions for the seven data sets corresponding to the horizontal, and  $+1^{\circ}$ ,  $+5^{\circ}$ ,  $+10^{\circ}$ ,  $-1^{\circ}$ ,  $-5^{\circ}$ , and  $-10^{\circ}$  inclinations. For each test run, the values of the operating pressure  $P_{av}$ , corresponding saturation temperature  $T_{s, av}$ , total mass flux G, rate of heat lost by steam  $Q_s$ , rate of heat gained by cooling water  $Q_w$ , and the percentage heat balance error are listed. The percentage heat balance error is given by

Run	$P_{av}$	$\mathbf{T}_{s,av}$	G	Qs	Q <sub>w</sub>	Error %
Indinyer	kPa	°C	kg/s.m²	kW	kW	
1	124.6	105.9	123.86	43.42	41.58	4.2
2	124.6	105.9	123.86	43.35	42.70	1.5
3	138.1	108.9	158.84	54.59	52.02	4.7
4	170.2	115.2	225.14	79.03	76.09	3.7
5	170.2	115.2	254.60	90.62	87.31	3.7
6	131.4	107.5	134.91	49.51	49.82	-0.6
7	186.4	118.0	105.44	38.26	40.26	-5.2
8	134.7	108.2	186.47	66.25	62.58	5.5
9	106.6	101.5	86.72	31.36	32.14	-2.5
10	101.5	100.1	50.41	18.46	18.11	1.9
11	105.0	101.0	45.82	10.81	10.50	1.8
12	102.1	100.2	37.48	13.73	15.98	-1.9
13	105.5		43.32	15.89	10.18	-1.8
14	119.1	104.6	88.80	34.31 20 29	33.90	-5.1
15	104.7	100.9	55.44	40.48	<b>40.03</b> 16.60	-0 9
16	104.7	101.9	44.99 CE 11	10.40	10.0U	-0.0
17	108.0	101.8	00.44	43.99	43.JL 12 79	<u> </u>
10	101.0	100.2	34.03	12.07	12.70	-0.1
19	101.8	100.2	34.3/	7 99	7 80	-0.1
<b>∠</b> ∪ 21	99.9	99.0 100 6	41.05	1.90	1/ 32	2.2
41 22	105.2	101.5	40.40	17 10	16 57	3.2
22	100./	101.5	21 61	11 52	12 02	_1 3
<u>2</u> 3	104.4	100.3	10 16	17 97	16 81	
44 25	102 /	100.0	49.10	16 37	15 73	3 9
45 26	102.4	101.3	63 77	23 12	22.49	2.7
20	107.5	101.7	59.59	21.60	22.51	-4.2
28	107.5	101.7	64.60	23.34	22.44	3.8
29	108.2	101.9	59.59	21.57	20.47	5.1
30	113.3	103.2	66.27	24.13	23.46	2.8
31	116.3	103.9	75.87	27.36	27.16	0.7
32	112.9	103.1	65.02	23.57	24.07	-2.1
33	116.3	103.9	72.53	26.27	27.20	-3.5
34	118.1	104.4	82.54	30.03	30.27	-0.8
35	117.5	104.2	82.96	30.07	28.91	3.8
36	119.2	104.6	84.63	30.45	28.46	6.5
37	117.5	104.2	89.22	32.08	29.63	7.6
38	117.5	104.2	88.80	32.32	30.85	4.5
39	109.0	102.1	90.71	32.70	31.30	4.3
40	111.1	102.6	81.50	29.62	30.58	-3.2
41	111.1	102.6	87.03	31.59	30.13	4.6
42	117.9	104.3	105.44	37.81	35.19	6.9
43	114.5	103.5	96.23	34.55	32.21	6.8
44	111.1	102.6	88.87	32.23	30.71	4.7
45	111.1	102.6	92.55	33.62	31.56	6.1
46	181.6	117.2	273.02	92.84	90.35	2.7
47	181.6	117.2	273.02	93.05	90.56	2.7
48	168.1	114.8	236.19	83.39	83.02	0.4
49	164.7	114.2	245.39	86.14	87.21	-1.2
50	140.6	109.5	190.15	67.21	67.68	-0.7
51	160.8	113.5	230.66	80.74	82.54	-2.2

#### TABLE A.1 Operating conditions for data in the horizontal position

	Run number	$\mathtt{P}_{av}$	T <sub>s,av</sub>	G	Qs	Q <sub>w</sub> kW	Error %
		kPa	°C	kg/s.m²	kW		
	52	144.0	110.2	197.52	68.82	69.18	-0.5
	53	157.5	112.9	217.77	74.87	74.47	0.5
	54	147.1	110.8	215.93	76.01	75.96	0.1
	55	143.7	110.1	197.52	69.21	71.91	-3.9
	56	143.7	110.1	199.36	70.24	72.36	-3.0
	57	153.9	112.2	226.98	80.45	82.19	-2.2
	58	140.9	109.5	195.67	69.48	67.79	2.4
	59	137.5	108.8	171.73	60.51	61.09	-0.9
	60	127.4	106.6	166.21	59.12	54.89	7.2
	61	120.6	105.0	116.49	41.98	39.43	6.1
	62	120.6	105.0	120.17	43.14	41.14	4.6
	63	138.4	109.0	191.99	67.73	63.89	5.7
	64	124.9	106.0	134.91	48.02	47.46	1.2
	65	124.9	106.0	142.27	50.72	49.51	2.4
	66	118.1	104.4	109.13	39.03	37.93	2.8
	67	118.1	104.4	112.81	40.12	39.30	2.0
	68	119.3	104.7	112.81	40.19	40.55	-0.9
	69	124.4	105.9	142.27	50.24	50.75	-1.0
	70	102.8	100.4	27.16	10.07	10.40	-3.3
	71	102.8	100.4	27.75	10.27	10.69	-4.1
	72	102.8	100.4	28.34	10.54	10.75	-2.0
	73	102.8	100.4	35.81	13.32	13.29	0.2

TABLE A.1 Operating conditions for data in the horizontal position (cont'd.)

Run	$\mathtt{P}_{\mathtt{av}}$	T <sub>s,av</sub>	G	Qs	Qw	Error %
number	kPa	°C	kg/s.m <sup>2</sup>	kW	kW	
1	105.4	101.1	53.33	19.15	20.48	-6.9
2	105.4	101.1	53.33	18.98	18.34	3.3
3	106.9	101.5	51.67	18.42	18.17	1.3
4	106.9	101.5	50.41	18.02	17.89	0.7
5	106.9	101.5	51.67	18.50	17.84	3.6
6	106.9	101.5	49.16	17.67	17.85	-1.0
7	103.8	100.7	37.90	13.72	14.16	-3.3
8	103.8	100.7	41.23	14.94	15.35	-2.7
9	103.8	100.7	33.72	12.24	12.84	-4.9
10	102.1	100.2	32.89	11.91	12.47	-4.6
11	102.1	100.2	34.14	12.38	12.92	-4.4
12	102.1	100.2	34.14	12.41	12.48	-0.6
13	106.2	101.3	52.92	19.16	20.02	-4.5
14	106.2	101.3	53.33	19.28	19.89	-3.4
15	102.8	100.4	57.51 52.00	20.87	20.20	3.4
10	102.8	100.4	54.08	18./9	19.54	-3.9
10	111 2	102.0	66.77	44.0/	20.37	-2.0
10	112 0	102.7	70 03	24.30	25.52	-5.0
19	113.0	103.1	67 94	23.32	25 02	_1 8
20	117 1	103.1	91 20	24.50	23.02	-1.0
41 22	118 8	104.1	81 71	29.04	30 94	- <u>4</u> .7
22	115 4	103 7	85 47	31.14	30.95	0 6
23	118 8	104 6	80 46	28 97	29 82	-2 9
25	112 6	103 0	76 29	27 87	28 60	-2 6
26	116.0	103.9	78.37	28.61	27.91	2.4
27	116.0	103.9	77.95	28.38	27.74	2.3
28	109.2	102.1	80.46	29.11	28.52	2.0
29	113.5	103.2	96.23	35.03	33.97	3.0
30	110.1	102.4	88.87	32.59	31.62	3.0
31	113.5	103.2	96.23	34.98	34.44	1.5
32	110.1	102.4	99.92	36.50	36.04	1.3
33	109.3	102.2	96.23	35.20	33.84	3.9
34	109.3	102.2	94.39	34.48	33.03	4.2
35	106.0	101.3	85.19	31.18	30.55	2.0
36	112.8	103.1	123.86	45.38	46.64	-2.8
37	116.1	103.9	129.38	46.91	47.55	-1.4
38	116.1	103.9	136.75	49.89	48.01	3.8
39	114.4	103.5	133.06	48.62	48.19	0.9
40	109.2	102.1	103.60	37.86	37.98	-0.3
41	109.2	102.1	105.44	38.33	37.42	2.4
42	112.6	103.0	105.44	38.26	37.94	0.8
43	109.2	102.1	105.44	38.43	38.86	-1.1
44	112.6	103.0	122.02	44.18	42.26	4.3
45	124.2	105.8	142.27	50.98	49.10	3.7
46	124.2	105.8	134.91	48.43	49.03	-1.2
47	120.8	105.0	138.59	49.87	49.89	0.0
48	120.8	105.0	140.43	50.48	49.10	2.7
49	127.6	106.6	158.84	57.00	55.46	2.7
50	125.9	106.2	158.84	57.22	57.27	-0.1
51	131.0	107.4	158.84	20.01	55.62	Τ.8

### TABLE A.2 Operating conditions for data in -1° [ downward ] inclination

	Run number	$\mathtt{P}_{\mathtt{av}}$	$T_{s,av}$	G kg/s.m <sup>2</sup>	Q <sub>s</sub> kw	Q <sub>w</sub> kw	Error %
		kPa	°C				
,	52	127.6	106.6	155.16	55.55	55.58	-0.1
	53	139.0	109.1	171.73	60.87	59.70	1.9
	54	138.1	108.9	168.05	59.73	61.16	-2.4
	55	132.2	107.7	166.21	59.22	59.61	-0.7
	56	133.9	108.0	177.26	63.59	62.28	2.1
	57	149.0	111.2	223.30	79.01	74.70	5.5
	58	147.3	110.9	223.30	79.27	75.83	4.3
	59	154.1	112.2	217.77	76.87	74.28	3.4
	60	111.4	102.7	103.60	37.58	37.18	1.1
	61	113.1	103.1	107.28	38.86	38.82	0.1
	62	108.0	101.8	109.13	39.71	38.65	2.7
	63	109.8	102.3	99.92	36.50	35.02	4.1

TABLE A.2 Operating conditions for data in -1° [ downward ] inclination (cont'd.)

Run	$\mathbf{P}_{av}$	T <sub>s,av</sub>	G	Qs	Q <sub>w</sub>	Error %
	kPa	°C	kg/s.m²	kW	kW	
1	111.7	102.8	66.69	24.23	23.04	4.9
2	116.8	104.1	76.70	27.81	27.09	2.6
3	111.8	102.8	77.54	28.19	27.39	2.8
4	116.9	104.1	85.47	30.95	29.46	4.8
5	113.4	103.2	96.23	34.37	33.08	3.7
6	125.0	106.0	136.75	48.08	48.60	-1.1
7	125.0	106.0	136.75	48.76	51.52	-5.7
8	118.3	104.4	112.81	40.59	42.83	-5.5
9	121.6	105.2	116.49	41.39	42.38	-2.4
10	130.1	107.2	147.80	52.48	55.50	-5.8
11	126.7	106.4	153.32	54.63	54.69	-0.1
12	142.0	109.7	173.58	61.00	62.32	-2.2
13	133.5	107.9	173.58	61.62	62.58	-1.6
14	147.0	110.8	219.61	76.90	70.65	8.1
15	148.1	111.0	203.04	72.12	75.05	-4.1
16	148.1	111.0	203.04	72.09	74.75	-3.7
17	153.6	112.1	241.71	85.39	86.97	-1.9
18	156.2	112.6	226.98	80.09	80.26	-0.2
19	119.1	104.6	122.02	43.49	44.75	-2.9
20	117.3	104.2	116.49	41.45	41.96	-1.2
21	106.5	101.4	99.92	35.68	36.08	-1.1
22	111.0	102.6	72.11	26.22	27.87	-6.3
23	110 7	102.6	73.36	26.74	26.52	0.8
24	118.7	104.5	83.38	30.32	31.05	-2.4
25	122.1	105.3	82.54	30.00	30.99	-3.3
20	115.1	103.6	107 54	44.73	43.78	2.1
47	115.1	103.6	147.54	46.14	45.34	1.7
28	121 7	104.5	147.04	53.88	53.40	0.8
29	122 0	105.9	157 00	52.37	56.12	-7.2
50	121 7	105.8	140 64	50.11	57.1V 55 97	-1.0
30 31	111 5	107.5	105 44	33.00	33.8/	-5.5
34	112 2	102.7	105.44	30.40	40.74	=7.0
33	112 2	103.2	107 20	20.40	40.43	-2.0
3 E	102 6	100.2	107.20	17 00	10 05	-2.9
35	100.0	102.0	60 01	21 00	10.05	-0.4
30	102.7	102.0	47 49	41.99 17 29	44.50	-2.0
30	102.7	100.4	10.15	1/ 2/	1/ 15	1 /
20	102.7	100.4	52 22	10 12	20 61	-6 0
35 A O	102.7	100.4	55 42	20 10	21 26	-5.0
∾o∨ /i1	102.7	100.4	A1 22	11 00	44.40	-2.2
42	102.8	100.4	50 00	18 11	18 67	-2.2
43	102.8	100.4	50.41	18.32	18.92	-3.3

### TABLE A.3 Operating conditions for data in -5° [ downward ] inclination

Run number	$P_{av}$	$T_{e,av}$	G	Qs	Q <sub>w</sub>	Error %
	kPa	°C	kg/s.m <sup>2</sup>	kW	kW	
1	121.2	105.1	98.08	35.85	36.99	-3.2
2	124.6	105.9	99.92	36.46	35.90	1.5
3	117.8	104.3	99.92	36.63	36.87	-0.6
4	117.8	104.3	99.92	36.59	37.17	-1.6
5	131.3	107.5	151.48	54.67	52.48	4.0
6	134.7	108.2	147.80	53.38	52.72	1.2
7	153.6	112.1	197.52	70.53	71.16	-0.9
8	150.2	111.4	206.72	73.12	75.04	-2.6
9	133.3	107.9	151.48	54.26	56.59	-4.3
10	140.1	109.4	166.21	58.72	59.79	-1.8
11	111.8	102.8	68.77	25.25	25.72	-1.9
12	111.8	102.8	57.09	21.00	21.35	-1.7
13	113.5	103.2	63.77	23.46	23.20	1.1
14	122.0	105.3	81.71	29.80	30.70	-3.0
15	122.0	105.3	84.63	31.14	30.27	2.8
16	107.8	101.8	81.50	30.00	31.00	-3.3
17	107.8	101.8	85.19	31.29	31.25	0.1
18	107.8	101.8	85.19	31.30	30.06	4.0
19	107.8	101.8	85.19	31.29	30.24	3.3
20	111.2	102.7	103.60	37.95	37.09	2.3
21	107.8	101.8	99.92	36.64	34.90	4.8
22	113.0	103.1	96.23	35.29	34.89	1.1
23	118.1	104.4	96.23	35.20	34.01	3.4
24	113.4	103.2	63.77	23.35	24.51	-5.0
25	108.3	101.9	32.47	11.97	12.27	-2.5
26	111.7	102.8	40.82	15.06	15.53	-3.1
27	111.7	102.8	52.92	19.48	20.15	-3.4
28	129.0	106.9	140.43	50.60	47.87	5.4
29	125.6	106.2	136.75	49.37	49.07	0.6
30	125.6	106.2	144.11	52.05	49.22	5.4
31	129.0	106.9	153.32	54.92	51.76	5.8
32	132.4	107.7	166.21	59.21	56.17	5.1
33	134.3	108.1	166.21	59.33	58.72	1.0
34	141.0	109.6	177.26	62.96	60.10	4.6
35	134.3	108.1	162.53	58.01	54.87	5.4
36	130.9	107.4	166.21	60.35	58.49	3.1
37	129.6	107.1	133.06	47.76	49.49	-3.6
38	126.2	106.3	134.91	48.85	49.86	-2.1
39	129.6	107.1	136.75	49.10	49.77	-1.4
40	122.9	105.5	136.75	50.04	49.17	1.7
41	128.1	106.7	144.11	52.97	54.86	-3.6
42	131.5	107.5	151.48	54.30	53.12	2.2
43	134.8	108.2	166.21	59.22	58.40	1.4
44	134.8	108.2	169.89	60.52	59.70	1.4
45	116.8	104.1	105.44	38.93	39.05	-0.3
46	116.8	104.1	98.08	36.22	36.21	0.0
47	111.7	102.8	70.45	26.21	25.44	2.9
48	115.2	103.7	63.77	23.68	24.71	-4.4
49	113.4	103.2	47.08	17.54	17.64	-0.6
50	115 2	103 7	51 25	19 10	10 07	1 0

### TABLE A.4 Operating conditions for data in -10° [ downward ] inclination

Run	$\mathbf{P}_{\mathbf{av}}$	$T_{s,av}$	G	Qs	Q <sub>w</sub>	Error %
namper	kPa	D°	kg/s.m²	kW	kW	
1	125.4	106.1	144.11	52.23	52.36	-0.2
2	125.4	106.1	147.80	53.49	53.36	0.2
3	128.7	106.9	144.11	52.47	52.56	-0.2
4	128.7	106.9	147.80	53.57	51.33	4.2
5	121.6	105.2	133.06	48.29	46.87	2.9
6	116.5	104.0	136.75	50.22	49.17	2.1
7	116.5	104.0	144.11	52.55	50.99	3.0
8	119.9	104.8	147.80	53.75	50.69	5.7
9	110.7	102.5	107.28	39.75	39.10	1.6
10	110.7	102.5	99.92	37.12	36.12	2.7
11	110.7	102.5	99.92	37.08	37.28	-0.5
12	110.7	102.5	99.92	36.82	35.81	2.7
13	110.7	102.5	99.92	37.10	36.95	0.4
14	106.3	101.4	85.19	31.49	30.69	2.5
15	106.3	101.4	88.87	33.02	32.08	2.8
16	106.3	101.4	92.55	34.30	32.73	4.6
17	106.3	101.4	92.55	34.34	32.61	5.1
18	109.7	102.3	88.87	32.78	32.14	2.0
19	106.5	101.4	60.43	22.58	22.24	1.5
20	106.5	101.4	57.51	21.48	20.97	2.4
21	106.5	101.4	57.51	21.42	21.17	1.2
22	106.5	101.4	57.51	21.41	21.74	-1.5
23	106.5	101.4	57.92	21.59	21.52	0.3
24	106.5	101.4	58.76	21.95	21.62	1.5
25	106.5	101.4	56.67	21.11	20.47	3.0
26	147.0	110.8	221.45	79.13	81.74	-3.3
27	153.7	112.1	228.82	81.56	85.24	-4.5
28	153.7	112.1	232.50	82.93	84.21	-1.5
29	153.7	112.1	225.14	80.49	83.06	-3.2
30	147.2	110.8	203.04	72.28	74.21	-2.7
31	143.8	110.1	199.36	71.23	73.26	-2.9
32	143.8	110.1	206.72	73.72	77.29	-4.8
33	143.8	110.1	203.04	72.38	73.58	-1.7
34	143.8	110.1	203.04	72.68	73.45	-1.1
35	140.4	109.4	197.52	70.78	71.97	-1.7
36	153.0	112.0	232.50	82.08	82.56	-0.6
37	156.4	112.6	239.87	84.67	83.45	1.4
38	153.0	112.0	228.82	81.08	82.17	-1.3
39	153.0	112.0	228.82	81.06	82.34	-1.6
40	153.0	112.0	226.98	80.69	80.63	0.1
41	159.8	113.3	239.87	85.02	84.27	0.9
42	121.7	105.2	147.80	53.30	51.27	3.8
43	121.7	105.2	136.75	49.28	50.75	-3.0
44	125.1	106.0	140.43	50.47	50.23	0.5
45	125.1	106.0	133.06	48.44	50.88	-5.0
46	101.6	100.1	25.39	9.42	9.77	-3.8
47	103.3	100.6	32.47	12.07	12.12	-0.4
48	103.3	100.6	33.31	12.40	11.95	3.6
49	103.3	100.6	32.05	11.95	12.40	-3.8
50	103.3	100.6	32.89	12.27	12.34	-0.6
51	102 2	100 6	40 07	15 60	16 05	2 6

### TABLE A.5 Operating conditions for data in $+1^{\circ}$ [ upward ] inclination

Run number	$P_{av}$	$T_{s,av}$	G	$Q_s$	Q <sub>w</sub>	Error %
	kPa	°C	kg/s.m²	kW	kW	
52	103.3	100.6	40.82	15.26	14.81	3.0
53	101.6	100.1	44.99	16.82	16.69	0.8
54	103.3	100.6	45.82	17.12	16.55	3.3
55	103.3	100.6	44.99	16.78	16.11	4.0
56	107.4	101.7	114.65	42.11	40.48	3.9
57	104.0	100.8	99.92	37.12	36.48	1.7
58	104.0	100.8	103.60	38.31	37.79	1.4
59	104.0	100.8	99.92	36.84	37.12	-0.7

TABLE A.5 Operating conditions for data in +1° [ upward ] inclination (cont'd)

TABLE A.6	Operating	conditions	for data	in +5°	[ upward ]	inclination
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Run	P <sub>av</sub>	T <sub>s,av</sub>	G	Qs	Q <sub>w</sub>	Error %
nullber	kPa	°C	kg/s.m²	kW	kW	
1	101.8	100.2	44.99	16.81	16.40	2.4
2	106.9	101.5	62.10	23.13	23.10	0.1
3	106.9	101.5	65.02	24.23	23.11	4.6
4	103.5	100.6	46.24	17.33	17.14	1.1
5	103.5	100.6	63.77	23.79	23.38	1.7
6	103.5	100.6	60.85	22.74	21.83	4.0
7	106.4	101.4	96.23	35.72	36.28	-1.6
8	106.4	101.4	96.23	35.77	35.95	-0.5
9	106.4	101.4	98.08	36.54	36.98	-1.2
10	106.4	101.4	98.08	36.46	37.26	-2.2
11	106.4	101.4	92.55	34.38	33.35	3.0
12	106.4	101.4	96.23	35.74	36.06	-0.9
13	106.4	101.4	96.23	35.84	36.48	-1.8
14	112.3	102.9	136.75	50.06	51.63	-3.1
15	107.8	101.8	140.43	51.38	51.66	-0.5
10	107.8	101.8	130./5	50.22	51.20	-2.0
10 10	104.4	101.9	140 43	44.91 E1 00	45.84	-2.0
10	120 0	102.0	101 63	51.20	51.31	-0.4
19	130.0	100.9	177 26	60.41	65.99	0.0
20	1/1 /	100.2	101 00	64.06	66.1/ 69 16	-3.3
21	138 0	109.0	191.99	67 37	68.10	-1 0
23	131 2	107 4	188 31	68 57	69 08	-1.0
24	131.2	107 4	188 31	68 21	69.00	-0.7
25	122.3	105.4	162.53	58.95	59.23	-0.5
26	118.9	104.6	151.48	55.05	57.94	-5.3
27	115.5	103.7	140.43	51.67	52.24	-1.1
28	115.5	103.7	144.11	52.83	54.48	-3.1
29	136.2	108.5	203.04	72.89	70.11	3.8
30	144.7	110.3	223.30	79.69	79.43	0.3
31	149.7	111.3	223.30	80.09	80.33	-0.3
32	146.3	110.7	221.45	79.39	79.14	0.3
33	103.0	100.5	22.44	8.36	8.53	-2.1
34	103.0	100.5	23.03	8.58	8.81	-2.7
35	103.0	100.5	23.91	8.91	8.82	1.0
36	103.0	100.5	23.62	8.79	9.08	-3.3
37	103.0	100.5	32.47	12.09	11.71	3.2
38	103.0	100.5	34.56	12.90	12.94	-0.3
39	103.0	100.5	38.73	14.48	14.01	3.2
40	102.7	100.4	36.64	13.73	13.39	2.5
41	102.7	100.4	38.73	14.53	14.49	0.2
42	102.7	100.4	42.90	16.09	15.77	2.0
43	102.7	100.4	43.74	16.41	16.49	-0.5
44	108.3	101.9	96.23	35.64	35.89	-0.7
45	104.9	101.0	81.50	30.41	29.24	3.8
46	104.9	101.0	88.87	33.14 22 10	31.99 31 73	3.5
4.7	104.9	101.0	00.0/	33.19	31./3 26 EA	4a - 4a 1 - 0
4 ð	104.9	101.0	/4.14 61 60	ム/ · ひ仏 つつ 1 A	40.J4 72 /0	42.0 1 4
49 E 0	104.9	101.0	52 22 52 23	ムコ・14 20 02	43.40 10 66	-1-4 1 0
50 E1	1046.9	101.0	53.33	40.04 10.02	18 00	1.0
Э <u>т</u>	TA4•2	TOT+0	JJ.JJ			72 • J

Run number	P <sub>av</sub> kPa	T <sub>s, av</sub> °C	G kg/s.m²	Q <sub>s</sub> kW	Q <sub>w</sub> kW	Error %
 52	158.4	113.0	269.33	96.35	91.21	5.3
53 54	161.8 165.1	113.7 114.3	276.70 276.70	98.76 98.77	94.09 93.50	4.7 5.3
55	161.8	113.7	269.33	96.29	91.92	4.5

TABLE A.6 Operating conditions for data in  $+5^{\circ}$  [ upward ] inclination (cont'd.)

Run	$P_{av}$	T <sub>s,av</sub>	G	Qs	Q <sub>w</sub>	Error %
number	kPa	°C	kg/s.m <sup>2</sup>	kW	kW	
1	106.3	101.4	47.08	17.65	17.03	3.5
2	106.3	101.4	50.83	19.06	18.56	2.7
3	111.4	102.7	63.35	23.59	24.09	-2.1
4	111.4	102.7	69.19	25.76	25.61	0.6
5	111.4	102.7	61.68	23.08	22.85	1.0
6	111.4	102.7	61.26	22.95	22.94	0.0
7	111.4	102.7	59.59	22.33	23.00	-3.0
8	111.4	102.7	65.44	24.46	23.25	5.0
9	114.0	103.4	74.20	27.67	26.69	3.5
10	114.0	103.4	71.28	26.54	26.33	0.8
11	114.0	103.4	75.45	28.02	27.88	0.5
12	114.0	103.4	77.12	28.72	29.25	-1.8
13	114.0	103.4	77.12	28.72	28.74	-0.1
15	116.0	103.9	129.38	4./.83	49.33	-3.1
15	116.0	103.9	125.70	40.24 15	40.50	-0.6
17	110.0	103.5	125.70	40.13	44/./9	-3.0
19	110 /	104.7	136.75	50.08	51.35	-2.0
10	110 /	104.7	122 06	10 07	50.47	-0.5
20	110 /	104.7	133.06	40.04	10.14	-4./
20	110 /	104 7	140 43	40.03 51 66	47.44 50 53	~1.3
22	116 0	103.9	136 75	50 39	50.55	-0 1
23	140.3	109.4	203 04	73 18	72 90	-0.1
24	140.3	109.4	203.04	73.11	73.36	-0.3
25	143.7	110.1	214.09	76.41	74.70	2.2
26	140.3	109.4	195.67	70.46	71.47	-1.4
27	140.3	109.4	195.67	70.70	71.91	-1.7
28	147.1	110.8	214.09	76.89	75.07	2.4
29	143.7	110.1	199.36	71.33	71.61	-0.4
30	143.7	110.1	203.04	71.85	72.83	-1.4
31	156.4	112.6	228.82	81.86	84.08	-2.7
32	153.0	112.0	228.82	81.52	83.55	-2.5
33	153.0	112.0	232.50	82.69	84.28	-1.9
34	156.4	112.6	232.50	82.53	83.75	-1.5
35	168.2	114.9	254.60	90.73	93.48	-3.0
36	164.8	114.2	258.28	91.87	93.14	-1.4
37	168.2	114.9	261.97	93.06	93.56	-0.5
38	164.8	114.2	261.97	93.03	93.56	-0.6
39	161.5	113.6	258.28	91.67	90.63	1.1
40	161.5	113.6	261.97	92.45	88.76	4.0
41	130.8	107.3	162.53	58.29	59.87	-2.7
42	134.2	108.1	166.21	59.34	61.84	-4.2
43	134.2	108.1	162.53	58.14	58.79	-1.1
44	130.8	107.3	158.84	56.56	58.04	-2.6
45	130.8	107.3	166.21	61.32	64.68	-5.5
46	127.4	106.6	166.21	60.43	63.51	-5.1
47	127.4	106.6	162.53	59.43	60.29	-1.4
48	124.1	105.8	162.53	59.44	61.06	-2.7
49	113.5	103.2	114.65	42.44	43.67	-2.9
50	113.5	103.2	114.65	42.43	41.99	1.0
51	113.5	103.2	114.65	42.30	43.14	-2.0
52	116.8	104.1	136.75	50.45	49.88	1.1

TABLE A.7 Operating conditions for data in +10° [ upward ] inclination

#### Appendix B

#### **FLOW-REGIME PARAMETERS**

The flow conditions corresponding to each visual observation [ or data point ] is tabulated in this Appendix. For each test run, the flow regimes observed in each visual section and the corresponding values of x,  $T_{s,av}$ , and G are provided. When the calculated value of the vapor quality [ based on thermodynamic equilibrium ] became negative [ indicating subcooled conditions ] a zero-value was entered and the data point was not used in plotting the flow-regime maps. The following abbreviations were used in listing the observed flow regimes.

ANNU	= Annular flow
ANWA	= Annular-wavy flow
WAVY	= Wavy flow
SLUG	= Slug flow
STRA	= Stratified flow
FULL	= Tube running full

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
1	A B C D E F	0.790 0.590 0.404 0.102 0.000 0.000	105.9	123.86	ANNU ANNU ANNU ANWA FULL FULL
2	A B C D E F	0.792 0.589 0.386 0.099 0.000 0.000	105.9	123.86	ANNU ANNU ANNU ANWA FULL FULL
3	A B C D E F	0.830 0.653 0.482 0.159 0.025 0.000	108.9	158.84	ANNU ANNU ANNU ANNU ANWA FULL
4	A B C D E F	0.842 0.650 0.389 0.116 0.000 0.000	115.2	225.14	ANNU ANNU ANNU ANWA FULL FULL
5	A B C D E F	$0.758 \\ 0.498 \\ 0.266 \\ 0.015 \\ 0.000 \\ 0.00$	115.2	254.60	ANNU ANNU ANNU ANWA FULL FULL
6	A B C D E F	0.798 0.598 0.366 0.000 0.000 0.000	107.5	134.91	ANNU ANNU FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
7	A B C D E F	$0.696 \\ 0.418 \\ 0.096 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	118.0	105.44	ANNU ANNU ANWA FULL FULL FULL
8	A B C D E F	0.633 0.335 0.142 0.012 0.000 0.000	108.2	186.47	ANNU ANNU ANNU ANWA FULL FULL
9	A B C D E F	0.513 0.284 0.076 0.000 0.000 0.000	101.5	86.72	ANNU ANNU SLUG FULL FULL FULL
10	A B C D E F	$0.486 \\ 0.154 \\ 0.000 \\ 0.00$	100.1	50.41	ANNU SLUG STRA FULL FULL FULL
11	A B C D E F	$0.451 \\ 0.029 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.0	45.82	ANNU SLUG STRA FULL FULL FULL
12	A B C D E F	$0.479 \\ 0.021 \\ 0.000 \\ 0.00$	100.2	37.48	ANNU SLUG STRA FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
13	A B C D E F	$\begin{array}{c} 0.418 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.2	43.32	ANNU SLUG STRA FULL FULL FULL
14	A B C D E F	0.743 0.483 0.000 0.000 0.000 0.000	104.6	88.80	ANNU ANNU SLUG FULL FULL FULL
15	A B C D E F	$0.632 \\ 0.220 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.9	55.42	ANNU WAVY FULL FULL FULL FULL
16	A B C D E F	$0.368 \\ 0.001 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.9	<b>44.99</b>	ANWA SLUG STRA FULL FULL FULL
17	A B C D E F	0.290 0.026 0.000 0.000 0.000 0.000	101.8	65.44	ANNU SLUG FULL FULL FULL FULL
18	A B C D E F	0.011 0.000 0.000 0.000 0.000 0.000	100.2	32.89	SLUG FULL STRA FULL FULL FULL

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
19	A B C D E F	$\begin{array}{c} 0.421 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.2	34.97	ANWA FULL STRA FULL FULL FULL
20	A B C D E F	$0.182 \\ 0.000 \\ 0.00$	99.6	21.85	SLUG STRA STRA FULL FULL STRA
21	A B C D E F	0.530 0.170 0.000 0.000 0.000 0.000	100.6	40.40	ANNU SLUG STRA FULL FULL STRA
22	A B C D E F	$0.596 \\ 0.282 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.5	47.08	ANNU WAVY STRA FULL FULL STRA
23	A B C D E F	0.442 0.000 0.000 0.000 0.000 0.000	100.3	31.64	WAVY SLUG STRA FULL FULL STRA
24	А В С D Е F	$0.602 \\ 0.301 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.8	49.16	ANNU WAVY FULL FULL FULL STRA

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
25	A B C D E F	$\begin{array}{c} 0.575 \\ 0.251 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.3	44.99	ANNU WAVY STRA FULL FULL STRA
26	A B C D E F	$0.674 \\ 0.415 \\ 0.101 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.7	63.77	ANNU ANNU SLUG FULL FULL STRA
27	A B C D E F	0.667 0.387 0.072 0.000 0.000 0.000	101.7	59.59	ANNU ANNU SLUG FULL FULL STRA
28	A B C D E F	0.687 0.415 0.142 0.000 0.000 0.000	101.7	64.60	ANNU ANNU SLUG FULL FULL STRA
29	A B C D E F	0.658 0.376 0.090 0.000 0.000 0.000	101.9	59.59	ANNU ANNU SLUG FULL FULL STRA
30	A B C D E F	0.587 0.327 0.030 0.000 0.000 0.000	103.2	66.27	ANNU ANNU SLUG FULL FULL FULL

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.702 0.459 0.165 0.000 0.000 0.000	103.9	75.87	ANNU ANNU ANWA FULL FULL FULL
32	A B C D E F	0.629 0.370 0.103 0.000 0.000 0.000	103.1	65.02	ANNU ANNU SLUG FULL FULL FULL
33	A B C D E F	$0.646 \\ 0.407 \\ 0.144 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000$	103.9	72.53	ANNU ANNU ANWA FULL FULL FULL
34	A B C D E F	0.573 0.300 0.042 0.000 0.000 0.000	104.4	82.54	ANNU ANNU SLUG FULL FULL FULL
35	A B C D E F	$0.556 \\ 0.283 \\ 0.094 \\ 0.000 \\ 0.00$	104.2	82.96	ANNU ANNU SLUG FULL FULL FULL
36	A B C D E F	$0.672 \\ 0.450 \\ 0.240 \\ 0.00$	104.6	84.63	ANNU ANNU FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
37	A B C D E F	$\begin{array}{c} 0.640 \\ 0.428 \\ 0.176 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	104.2	89.22	ANNU ANNU ANNU FULL FULL FULL
38	A B C D E F	0.578 0.309 0.073 0.000 0.000 0.000	104.2	88.80	ANNU ANNU SLUG FULL FULL FULL
39	A B C D E F	$0.599 \\ 0.342 \\ 0.142 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.1	90.71	ANNU ANNU ANWA FULL FULL FULL
40	A B C D E F	0.553 0.280 0.000 0.000 0.000 0.000	102.6	81.50	ANNU ANNU SLUG FULL FULL FULL
41	A B C D E F	0.573 0.279 0.026 0.000 0.000 0.000	102.6	87.03	ANNU ANNU SLUG FULL FULL FULL
42	A B C D E F	0.691 0.495 0.306 0.000 0.000 0.000	104.3	105.44	ANNU ANNU FULL FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
43	A B C D E F	0.656 0.432 0.238 0.000 0.000 0.000	103.5	96.23	ANNU ANNU ANNU FULL FULL FULL
44	A B C D E F	0.537 0.307 0.107 0.000 0.000 0.000	102.6	88.87	ANNU ANNU ANWA FULL FULL FULL
45	A B C D E F	0.558 0.303 0.059 0.000 0.000 0.000	102.6	92.55	ANNU ANNU SLUG FULL FULL FULL
46	A B C D E F	0.750 0.566 0.395 0.171 0.000 0.000	117.2	273.02	ANNU ANNU ANNU ANNU ANWA FULL
47	A B C D E F	0.753 0.562 0.365 0.150 0.000 0.000	117.2	273.02	ANNU ANNU ANNU ANNU FULL FULL
48	A B C D E F	$0.692 \\ 0.439 \\ 0.219 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	114.8	236.19	ANNU ANNU FULL FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
49	A B C D E F	$\begin{array}{c} 0.684 \\ 0.427 \\ 0.273 \\ 0.026 \\ 0.000 \\ 0.000 \end{array}$	114.2	245.39	ANNU ANNU ANNU ANWA FULL FULL
50	A B C D E F	0.660 0.394 0.176 0.000 0.000 0.000	109.5	190.15	ANNU ANNU ANNU ANWA FULL FULL
51	A B C D E F	0.694 0.457 0.280 0.004 0.000 0.000	113.5	230.66	ANNU ANNU ANNU ANWA FULL FULL
52	A B C D E F	0.687 0.452 0.237 0.026 0.000 0.000	110.2	197.52	ANNU ANNU ANNU ANWA FULL FULL
53	A B C D E F	0.697 0.468 0.331 0.142 0.000 0.000	112.9	217.77	ANNU ANNU ANNU ANNU ANWA FULL
54	A B C D E F	0.661 0.400 0.181 0.000 0.000 0.000	110.8	215.93	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
55	A B C D E F	0.641 0.376 0.226 0.014 0.000 0.000	110.1	197.52	ANNU ANNU ANNU ANWA FULL FULL
56	A B C D E F	0.650 0.370 0.187 0.000 0.000 0.000	110.1	199.36	ANNU ANNU ANNU ANWA FULL FULL
57	A B C D E F	0.678 0.417 0.255 0.010 0.000 0.000	112.2	226.98	ANNU ANNU ANNU ANWA FULL FULL
58	A B C D E F	0.680 0.441 0.222 0.028 0.000 0.000	109.5	195.67	ANNU ANNU ANNU ANWA FULL FULL
59	A B C D E F	0.707 0.455 0.224 0.029 0.000 0.000	108.8	171.73	ANNU ANNU ANNU ANWA FULL FULL
60	A B C D E F	0.671 0.407 0.193 0.054 0.000 0.000	106.6	166.21	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
61	A B C D E F	$\begin{array}{c} 0.737 \\ 0.563 \\ 0.314 \\ 0.070 \\ 0.000 \\ 0.000 \end{array}$	105.0	116.49	ANNU ANNU ANNU ANWA FULL FULL
62	A B C D E F	0.727 0.520 0.257 0.043 0.000 0.000	105.0	120.17	ANNU ANNU ANNU SLUG FULL FULL
63	A B C D E F	0.669 0.406 0.209 0.017 0.000 0.000	109.0	191.99	ANNU ANNU ANNU ANWA FULL FULL
64	A B C D E F	0.704 0.461 0.272 0.049 0.000 0.000	106.0	134.91	ANNU ANNU ANNU ANWA FULL FULL
65	A B C D E F	0.678 0.420 0.201 0.013 0.000 0.000	106.0	142.27	ANNU ANNU ANNU ANWA FULL FULL
66	A B C D E F	0.630 0.408 0.199 0.010 0.000 0.000	104.4	109.13	ANNU ANNU ANNU SLUG FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	observed flow regime
67	A B C D E F	0.691 0.457 0.237 0.006 0.000 0.000	104.4	112.81	ANNU ANNU ANNU SLUG FULL FULL
68	A B C D E F	$0.717 \\ 0.458 \\ 0.250 \\ 0.030 \\ 0.00$	104.7	112.81	ANNU ANNU ANNU SLUG FULL FULL
69	A B C D E F	0.652 0.400 0.178 0.007 0.000 0.000	105.9	142.27	ANNU ANNU ANNU ANWA FULL FULL
70	A B C D E F	$0.258 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.4	27.16	WAVY FULL FULL FULL STRA
71	A B C D E F	$\begin{array}{c} 0.324 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.4	27.75	WAVY FULL FULL FULL STRA
72	A B C D E F	$0.257 \\ 0.000 \\ 0.00$	100.4	28.34	WAVY FULL FULL FULL FULL STRA

Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
А	0.285	100.4	35.81	WAVY
В	0.000			FULL
C	0.000			FULL
D	0.000			FULL
E	0.000			FULL
म	0.000			STRA
	Visual observation section A B C D E F	Visual         x           observation         section           A         0.285           B         0.000           C         0.000           D         0.000           E         0.000           F         0.000	Visual observation section         x         T <sub>s,av</sub> °C           A         0.285         100.4           B         0.000         0.000           C         0.000         0.000           D         0.000         E           F         0.000         F	Visual observation section       x       T <sub>s,av</sub> G °C kg/m².s         A       0.285 100.4       35.81         B       0.000       0.000         C       0.000       0.000         E       0.000       F

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
1	A B C D E F	$\begin{array}{c} 0.621 \\ 0.327 \\ 0.056 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.1	53.33	ANNU ANNU SLUG FULL FULL STRA
2	A B C D E F	0.619 0.333 0.017 0.000 0.000 0.000	101.1	53.33	ANNU ANNU WAVY STRA STRA STRA
3	A B C D E F	0.615 0.299 0.000 0.000 0.000 0.000	101.5	51.67	ANNU ANWA FULL STRA STRA STRA
4	A B C D E F	0.553 0.233 0.000 0.000 0.000 0.000	101.5	50.41	ANNU ANWA STRA STRA STRA STRA
5	A B C D E F	0.540 0.207 0.000 0.000 0.000 0.000	101.5	51.67	ANNU WAVY STRA STRA STRA STRA
6	A B C D E F	0.458 0.098 0.000 0.000 0.000 0.000 0.000	101.5	49.16	ANNU WAVY STRA STRA STRA STRA

# TABLE B.2 Flow-regime parameters for data set in $-1^{\circ}$ [ downward ] inclination

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
7	A B C D E F	$0.531 \\ 0.161 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.7	37.90	ANNU WAVY STRA STRA STRA STRA
8	A B C D E F	0.460 0.113 0.000 0.000 0.000 0.000	100.7	41.23	ANNU WAVY STRA STRA STRA STRA
9	A B C D E F	$0.449 \\ 0.019 \\ 0.000 \\ 0.00$	100.7	33.72	ANWA WAVY STRA STRA STRA STRA
10	A B C D E F	$0.481 \\ 0.046 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.2	32.89	ANWA WAVY STRA STRA STRA STRA
11	A B C D E F	0.365 0.000 0.000 0.000 0.000 0.000	100.2	34.14	WAVY STRA STRA STRA STRA STRA
12	A B C D E F	$0.201 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.2	34.14	WAVY STRA STRA STRA STRA STRA

# TABLE B.2 Flow-regime parameters for data set in $-1^{\circ}$ [ downward ] inclination (cont'd.)

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
13	A B C D E F	0.626 0.330 0.018 0.000 0.000 0.000	101.3	52.92	ANNU ANNU SLUG STRA FULL STRA
14	A B C D E F	0.655 0.364 0.065 0.000 0.000 0.000	101.3	53.33	ANNU ANNU WAVY STRA FULL STRA
15	A B C D E F	$0.496 \\ 0.209 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.4	57.51	ANNU ANWA WAVY STRA STRA STRA
16	A B C D E F	0.540 0.264 0.000 0.000 0.000 0.000	100.4	52.08	ANNU ANWA FULL STRA STRA STRA
17	A B C D E F	$0.712 \\ 0.463 \\ 0.204 \\ 0.000 \\ 0.00$	104.0	68.77	ANNU ANNU ANWA FULL FULL STRA
18	A B C D E F	0.642 0.383 0.112 0.000 0.000 0.000	102.7	66.69	ANNU ANNU ANWA FULL FULL STRA

# TABLE B.2 Flow-regime parameters for data set in $-1^{\circ}$ [ downward ] inclination (cont'd.)

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Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.597 0.312 0.075 0.000 0.000 0.000	103.1	70.03	ANNU ANNU SLUG FULL FULL STRA
20	A B C D E F	0.580 0.303 0.067 0.000 0.000 0.000	103.1	67.94	ANNU ANNU SLUG FULL FULL STRA
21	A B C D E F	$0.587 \\ 0.271 \\ 0.001 \\ 0.000 \\ 0.00$	104.1	81.29	ANNU ANNU SLUG FULL FULL FULL
22	A B C D E F	0.613 0.321 0.078 0.000 0.000 0.000	104.6	81.71	ANNU ANNU ANWA FULL FULL FULL
23	A B C D E F	0.617 0.317 0.060 0.000 0.000 0.000	103.7	85.47	ANNU ANNU SLUG FULL FULL FULL
24	A B C D E F	0.652 0.398 0.155 0.000 0.000 0.000	104.6	80.46	ANNU ANNU ANWA FULL FULL STRA

#### TABLE B.2 Flow-regime parameters for data set in -1° [ downward ] inclination (cont'd.)

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
25	A B C D E F	0.547 0.276 0.053 0.000 0.000 0.000	103.0	76.29	ANNU ANNU SLUG FULL FULL FULL
26	A B C D E F	0.605 0.316 0.082 0.000 0.000 0.000	103.9	78.37	ANNU ANNU SLUG FULL FULL FULL
27	A B C D E F	0.752 0.501 0.254 0.000 0.000 0.000	103.9	77.95	ANNU ANNU ANNU FULL FULL FULL
28	A B C D E F	0.581 0.369 0.166 0.000 0.000 0.000	102.1	80.46	ANNU ANNU ANWA FULL FULL STRA
29	A B C D E F	0.644 0.395 0.167 0.000 0.000 0.000	103.2	96.23	ANNU ANNU ANNU FULL FULL FULL
30	A B C D E F	0.573 0.285 0.006 0.000 0.000 0.000	102.4	88.87	ANNU ANNU SLUG FULL FULL FULL

## TABLE B.2 Flow-regime parameters for data set in -1° [ downward ] inclination (cont'd.)

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Run number	Visual observation section	x	T <sub>s, av</sub> °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.728 0.477 0.183 0.000 0.000 0.000	103.2	96.23	ANNU ANNU ANNU FULL FULL FULL
32	A B C D E F	0.546 0.264 0.044 0.000 0.000 0.000	102.4	99.92	ANNU ANNU SLUG FULL FULL FULL
33	A B C D E F	0.559 0.272 0.036 0.000 0.000 0.000	102.2	96.23	ANNU ANNU SLUG FULL FULL FULL
34	A B C D E F	0.549 0.267 0.018 0.000 0.000 0.000	102.2	94.39	ANNU ANNU SLUG FULL FULL FULL
35	A B C D E F	0.563 0.307 0.061 0.000 0.000 0.000	101.3	85.19	ANNU ANNU SLUG FULL FULL FULL
36	A B C D E F	0.574 0.237 0.000 0.000 0.000 0.000	103.1	123.86	ANNU ANNU ANWA FULL FULL FULL

# TABLE B.2 Flow-regime parameters for data set in -1° [ downward ] inclination (cont'd.)

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
37	A B C D E F	0.587 0.284 0.083 0.000 0.000 0.000	103.9	129.38	ANNU ANNU ANWA FULL FULL FULL
38	A B C D E F	0.585 0.280 0.067 0.000 0.000 0.000	103.9	136.75	ANNU ANNU ANWA FULL FULL FULL
39	A B C D E F	0.568 0.251 0.011 0.000 0.000 0.000	103.5	133.06	ANNU ANNU ANWA FULL FULL FULL
40	A B C D E F	0.570 0.269 0.024 0.000 0.000 0.000	102.1	103.60	ANNU ANNU SLUG FULL FULL FULL
41	A B C D E F	0.563 0.305 0.105 0.000 0.000 0.000	102.1	105.44	ANNU ANNU ANWA FULL FULL FULL
42	A B C D E F	0.651 0.394 0.168 0.000 0.000 0.000	103.0	105.44	ANNU ANNU ANNU FULL FULL FULL

## TABLE B.2 Flow-regime parameters for data set in -1° [ downward ] inclination (cont'd.)
Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
43	A B C D E F	$\begin{array}{c} 0.525 \\ 0.232 \\ 0.014 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	102.1	105.44	ANNU ANNU SLUG FULL FULL FULL
4 <u>4</u>	A B C D E F	0.600 0.317 0.087 0.000 0.000 0.000	103.0	122.02	ANNU ANNU ANWA FULL FULL FULL
45	A B C D E F	$0.659 \\ 0.398 \\ 0.220 \\ 0.046 \\ 0.000 \\ 0.000 \\ 0.000 $	105.8	142.27	ANNU ANNU ANNU ANWA FULL FULL
46	A B C D E F	0.678 0.419 0.183 0.004 0.000 0.000	105.8	134.91	ANNU ANNU ANNU ANWA FULL FULL
47	A B C D E F	0.639 0.329 0.086 0.000 0.000 0.000	105.0	138.59	ANNU ANNU ANWA FULL FULL FULL
48	A B C D E F	0.654 0.392 0.139 0.000 0.000 0.000	105.0	140.43	ANNU ANNU ANNU FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
49	A B C D E F	0.674 0.405 0.170 0.000 0.000 0.000	106.6	158.84	ANNU ANNU ANNU FULL FULL FULL
50	A B C D E F	0.627 0.331 0.077 0.000 0.000 0.000	106.2	158.84	ANNU ANNU ANWA FULL FULL FULL
51	A B C D E F	0.693 0.447 0.227 0.053 0.000 0.000	107.4	158.84	ANNU ANNU ANNU ANWA FULL FULL
52	A B C D E F	$0.695 \\ 0.439 \\ 0.210 \\ 0.013 \\ 0.000 \\ 0.000 \\ 0.000$	106.6	155.16	ANNU ANNU ANNU ANWA FULL FULL
53	A B C D E F	0.687 0.442 0.275 0.089 0.000 0.000	109.1	171.73	ANNU ANNU ANNU ANWA FULL FULL
54	A B C D E F	$0.701 \\ 0.449 \\ 0.237 \\ 0.043 \\ 0.000 \\ 0.000 \\ 0.000 $	108.9	168.05	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
55	A B C D E F	0.624 0.359 0.170 0.014 0.000 0.000	107.7	166.21	ANNU ANNU ANNU ANWA FULL FULL
56	A B C D E F	0.637 0.348 0.110 0.000 0.000 0.000	108.0	177.26	ANNU ANNU ANWA FULL FULL FULL
57	A B C D E F	0.711 0.474 0.275 0.061 0.000 0.000	111.2	223.30	ANNU ANNU ANNU ANWA FULL FULL
58	A B C D E F	0.674 0.413 0.195 0.016 0.000 0.000	110.9	223.30	ANNU ANNU ANNU ANWA FULL FULL
59	A B C D E F	0.717 0.486 0.315 0.118 0.000 0.000	112.2	217.77	ANNU ANNU ANNU ANNU FULL FULL
60	A B C D E F	$0.630 \\ 0.349 \\ 0.126 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.7	103.60	ANNU ANNU ANWA FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
61	Α	0.572	103.1	107.28	ANNU
	В	0.257			ANNU
	C	0.083			ANWA
	D	0.000			FULL
	E	0.000			FULL
	F	0.000			FULL
62	A	0.572	101.8	109.13	ANNU
	В	0.281			ANNU
	C	0.035			SLUG
	D	0.000			FULL
	E	0.000			FULL
	F	0.000			FULL
63	А	0.525	102.3	99.92	ANNU
	В	0.257			ANNU
	C	0.043			SLUG
	D	0.000			FULL
	E	0.000		·	FULL
	F	0.000			FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
1	A B C D E F	0.704 0.461 0.197 0.000 0.000 0.000	102.8	66.69	ANNU ANNU ANWA STRA STRA STRA
2	A B C D E F	0.707 0.472 0.222 0.000 0.000 0.000	104.1	76.70	ANNU ANNU ANWA STRA STRA STRA
3	A B C D E F	0.648 0.408 0.168 0.000 0.000 0.000	102.8	77.54	ANNU ANNU ANWA FULL STRA STRA
4	A B C D E F	0.559 0.300 0.076 0.000 0.000 0.000	104.1	85.47	ANNU ANNU WAVY STRA STRA STRA
5	A B C D E F	0.728 0.525 0.319 0.002 0.000 0.000	103.2	96.23	ANNU ANNU ANNU WAVY STRA STRA
6	A B C D E F	0.628 0.398 0.233 0.039 0.000 0.000	106.0	136.75	ANNU ANNU ANNU WAVY STRA STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
7	A B C D E F	0.629 0.365 0.168 0.000 0.000 0.000	106.0	136.75	ANNU ANNU ANNU WAVY FULL STRA
8	A B C D E F	0.586 0.292 0.084 0.000 0.000 0.000	104.4	112.81	ANNU ANNU ANWA STRA STRA STRA
9	A B C D E F	0.622 0.395 0.248 0.004 0.000 0.000	105.2	116.49	ANNU ANNU ANNU WAVY STRA STRA
10	A B C D E F	0.665 0.399 0.230 0.047 0.000 0.000	107.2	147.80	ANNU ANNU ANNU ANWA FULL STRA
11	A B C D E F	0.679 0.419 0.211 0.015 0.000 0.000	106.4	153.32	ANNU ANNU ANNU ANWA FULL STRA
12	A B C D E F	0.690 0.451 0.274 0.098 0.000 0.000	109.7	173.58	ANNU ANNU ANNU ANWA FULL STRA

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
13	A	0.662	107.9	173.58	ANNU
	В	0.394			ANNU
	C	0.185			ANNU
	D	0.000			ANWA
	E	0.000			FULL
	F	0.000			FULL
14	A	0.699	110.8	219.61	ANNU
	В	0.473			ANNU
	C	0.288			ANNU
	D	0.110			ANWA
	E	0.000			FULL
	푀	0.000			STRA
15	A	0.660	111.0	203.04	ANNU
	В	0.413			ANNU
	C	0.201			ANNU
	D	0.002			ANWA
	E	0.000			FULL
	भ	0.000			FULL
16	A	0.669	111.0	203.04	ANNU
70	B	0.410			ANNU
	Ē	0.191			ANNU
	D	0.000			ANWA
	E	0.000			FULL
	F	0.000			FULL
17	۵	0 677	112 1	241.71	ANNU
± /	B	0.428			ANNU
	Č	0.209			ANNU
	C D	0.010			ANWA
	<u>य</u>	0.000			FULL
	F	0.000			FULL
18	Δ	0.680	112.6	226.98	ANNU
TO	R	0 430	€ ەلىمىدىد	0	ANNU
	C C	0 233			ANNU
		0 021			ANWA
	<u>ज</u>	0.000			FULL
	F	0.000			STRA

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.683 0.432 0.207 0.000 0.000 0.000	104.6	122.02	ANNU ANNU ANNU WAVY STRA STRA
20	A B C D E F	0.673 0.458 0.261 0.018 0.000 0.000	104.2	116.49	ANNU ANNU ANNU WAVY STRA STRA
21	A B C D E F	0.680 0.493 0.279 0.033 0.000 0.000	101.4	99.92	ANNU ANNU ANNU WAVY STRA STRA
22	A B C D E F	0.626 0.387 0.154 0.000 0.000 0.000	102.6	72.11	ANNU ANNU ANWA STRA STRA STRA
23	A B C D E F	$0.642 \\ 0.408 \\ 0.020 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.6	73.36	ANNU ANNU WAVY STRA STRA STRA
24	A B C D E F	0.641 0.379 0.179 0.000 0.000 0.000	104.5	83.38	ANNU ANNU ANWA STRA STRA STRA

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
25	A B C D E F	0.696 0.433 0.226 0.000 0.000 0.000	105.3	82.54	ANNU ANNU ANNU STRA STRA STRA
26	A B C D E F	0.685 0.409 0.179 0.000 0.000 0.000	103.6	123.86	ANNU ANNU ANNU STRA STRA STRA
27	A B C D E F	0.637 0.347 0.140 0.000 0.000 0.000	103.6	127.54	ANNU ANNU ANNU STRA STRA STRA
28	A B C D E F	0.605 0.334 0.117 0.000 0.000 0.000	104.5	149.64	ANNU ANNU ANNU STRA STRA STRA
29	A B C D E F	0.742 0.527 0.319 0.086 0.000 0.000	107.5	147.80	ANNU ANNU ANNU ANWA FULL FULL
30	A B C D E F	0.697 0.450 0.227 0.005 0.000 0.000	105.8	157.00	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.712 0.481 0.279 0.067 0.000 0.000	107.5	149.64	ANNU ANNU ANNU ANWA FULL STRA
32	A B C D E F	0.652 0.368 0.133 0.000 0.000 0.000	102.7	105.44	ANNU ANNU STRA STRA STRA STRA
33	A B C D E F	0.625 0.333 0.086 0.000 0.000 0.000	103.2	105.44	ANNU ANNU ANWA STRA STRA STRA
34	A B C D E F	$0.609 \\ 0.299 \\ 0.031 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	103.2	107.28	ANNU ANNU WAVY STRA STRA STRA
35	А В С Д Е F	$0.481 \\ 0.209 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.6	49.16	ANNU WAVY STRA STRA STRA STRA
36	A B C D E F	0.307 0.085 0.000 0.000 0.000 0.000	102.0	60.01	ANNU WAVY STRA STRA STRA STRA

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
37	A B C D E F	$\begin{array}{c} 0.601 \\ 0.274 \\ 0.017 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.4	47.49	ANNU ANWA WAVY STRA STRA STRA
38	A B C D E F	$0.417 \\ 0.037 \\ 0.000 \\ 0.00$	100.4	39.15	ANWA WAVY STRA STRA STRA STRA
39	A B C D E F	0.463 0.204 0.000 0.000 0.000 0.000	100.4	53.33	ANNU ANWA STRA STRA STRA STRA
40	A B C D E F	0.480 0.223 0.000 0.000 0.000 0.000	100.4	55.42	ANNU ANWA STRA STRA STRA STRA
41	A B C D E F	$0.554 \\ 0.239 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.4	41.23	ANNU WAVY STRA STRA STRA STRA
42	A B C D E F	0.605 0.318 0.000 0.000 0.000 0.000 0.000	100.4	50.00	ANNU ANWA STRA STRA STRA STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
43	A	0.631	100.4	50.41	ANNU
	В	0.184			WAVY
	C	0.000			STRA
	D	0.000			STRA
	E	0.000			STRA
	F	0.000			STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
1	A B C D E F	0.651 0.219 0.000 0.000 0.000	105.1	98.08	ANNU ANNU ANNU STRA FULL STRA
2	A B C D E F	0.772 0.556 0.337 0.000 0.000 0.000	105.9	99.92	ANNU ANNU ANNU STRA FULL STRA
3	A B C D E F	0.581 0.219 0.000 0.000 0.000 0.000	104.3	99.92	ANNU ANNU STRA STRA STRA STRA
4	A B C D E F	0.578 0.258 0.033 0.000 0.000 0.000	104.3	99.92	ANNU ANNU WAVY STRA STRA STRA
5	A B C D E F	0.685 0.426 0.248 0.000 0.000 0.000	107.5	151.48	ANNU ANNU ANNU WAVY STRA STRA
6	A B C D E F	0.680 0.438 0.262 0.000 0.000 0.000	108.2	147.80	ANNU ANNU ANNU WAVY STRA STRA

Run number	Visual observation section	x	T <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
7	A B C D E F	0.673 0.441 0.252 0.013 0.000 0.000	112.1	197.52	ANNU ANNU ANNU ANWA FULL FULL
8	A B C D E F	0.673 0.416 0.252 0.074 0.000 0.000	111.4	206.72	ANNU ANNU ANNU ANWA FULL FULL
9	A B C D E F	0.613 0.381 0.180 0.000 0.000 0.000	107.9	151.48	ANNU ANNU ANNU ANWA STRA FULL
10	A B C D E F	0.728 0.525 0.345 0.138 0.000 0.000	109.4	166.21	ANNU ANNU ANNU ANNU FULL FULL
11	A B C D E F	$0.702 \\ 0.441 \\ 0.120 \\ 0.00$	102.8	68.77	ANNU ANNU WAVY STRA STRA STRA
12	А В С D Е F	0.635 0.339 0.000 0.000 0.000 0.000 0.000	102.8	57.09	ANNU ANNU WAVY STRA STRA STRA

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
13	A B C D E F	$\begin{array}{c} 0.517 \\ 0.229 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	103.2	63.77	ANNU ANWA STRA STRA STRA STRA
14	A B C D E F	0.617 0.381 0.117 0.000 0.000 0.000	105.3	81.71	ANNU ANNU ANWA STRA STRA STRA
15	A B C D E F	0.410 0.189 0.000 0.000 0.000 0.000	105.3	84.63	ANNU ANNU WAVY STRA STRA STRA
16	A B C D E F	0.545 0.224 0.000 0.000 0.000 0.000	101.8	81.50	ANNU ANNU WAVY STRA STRA STRA
17	A B C D E F	$\begin{array}{c} 0.619 \\ 0.334 \\ 0.082 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.8	85.19	ANNU ANNU WAVY STRA STRA STRA
18	A B C D E F	0.676 0.394 0.129 0.000 0.000 0.000	101.8	85.19	ANNU ANNU ANWA STRA STRA STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.622 0.372 0.143 0.000 0.000 0.000	101.8	85.19	ANNU ANNU ANWA STRA STRA STRA
20	A B C D E F	0.595 0.298 0.074 0.000 0.000 0.000	102.7	103.60	ANNU ANNU WAVY STRA STRA STRA
21	A B C D E F	0.583 0.282 0.047 0.000 0.000 0.000	101.8	99.92	ANNU ANNU WAVY STRA STRA STRA
22	A B C D E F	0.615 0.368 0.164 0.000 0.000 0.000	103.1	96.23	ANNU ANNU ANWA STRA STRA STRA
23	A B C D E F	$0.700 \\ 0.447 \\ 0.230 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	104.4	96.23	ANNU ANNU ANNU STRA STRA STRA
24	A B C D E F	$0.484 \\ 0.173 \\ 0.000 \\ 0.00$	103.2	63.77	ANNU ANWA STRA STRA STRA STRA

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Run number	Visual observation section	x	T <sub>s, av</sub> °C	G kg/m².s	Observed flow regime
25	A B C D E F	$\begin{array}{c} 0.419 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.9	32.47	WAVY STRA STRA STRA STRA STRA
26	A B C D E F	0.518 0.149 0.000 0.000 0.000 0.000	102.8	40.82	ANNU WAVY STRA STRA STRA STRA
27	A B C D E F	0.609 0.289 0.000 0.000 0.000 0.000	102.8	52.92	ANNU ANWA STRA STRA STRA STRA
28	A B C D E F	0.726 0.466 0.284 0.052 0.000 0.000	106.9	140.43	ANNU ANNU ANNU ANWA STRA FULL
29	А В С Д Е F	$0.676 \\ 0.405 \\ 0.188 \\ 0.000 \\ 0.00$	106.2	136.75	ANNU ANNU ANNU ANWA STRA FULL
30	A B C D E F	0.623 0.364 0.146 0.000 0.000 0.000	106.2	144.11	ANNU ANNU ANNU STRA STRA FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.642 0.370 0.175 0.001 0.000 0.000	106.9	153.32	ANNU ANNU ANNU WAVY STRA STRA
32	A B C D E F	0.653 0.390 0.227 0.055 0.000 0.000	107.7	166.21	ANNU ANNU ANNU ANWA STRA STRA
33	A B C D E F	0.607 0.323 0.135 0.000 0.000 0.000	108.1	166.21	ANNU ANNU ANNU WAVY FULL STRA
34	A B C D E F	0.746 0.533 0.334 0.108 0.000 0.000	109.6	177.26	ANNU ANNU ANNU ANWA FULL STRA
35	А В С Д Е F	0.675 0.416 0.193 0.025 0.000 0.000	108.1	162.53	ANNU ANNU ANNU ANWA FULL STRA
36	A B C D E F	$\begin{array}{c} 0.622 \\ 0.307 \\ 0.040 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	107.4	166.21	ANNU ANNU ANWA STRA STRA STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
37	A B C D E F	0.661 0.387 0.232 0.000 0.000 0.000	107.1	133.06	ANNU ANNU ANNU ANWA STRA STRA
38	A B C D E F	0.651 0.367 0.131 0.000 0.000 0.000	106.3	134.91	ANNU ANNU ANWA WAVY STRA STRA
39	A B C D E F	0.672 0.391 0.199 0.000 0.000 0.000	107.1	136.75	ANNU ANNU ANNU ANWA STRA STRA
<u>4</u> 0	A B C D E F	0.584 0.251 0.000 0.000 0.000 0.000	105.5	136.75	ANNU ANNU WAVY STRA STRA STRA
41	A B C D E F	0.667 0.410 0.205 0.006 0.000 0.000	106.7	144.11	ANNU ANNU ANNU ANWA FULL FULL
42	A B C D E F	0.683 0.237 0.026 0.000 0.000	107.5	151.48	ANNU ANNU ANNU ANWA STRA STRA

Run number	Visual observation section	x	Τ <sub>s,av</sub> °C	G kg/m².s	Observed flow regime
43	A B C D E F	0.680 0.438 0.225 0.007 0.000 0.000	108.2	166.21	ANNU ANNU ANNU ANWA STRA STRA
44	A B C D E F	0.694 0.431 0.196 0.000 0.000 0.000	108.2	169.89	ANNU ANNU ANNU ANWA STRA FULL
45	A B C D E F	0.506 0.203 0.005 0.000 0.000 0.000	104.1	105.44	ANNU ANNU WAVY STRA FULL STRA
46	A B C D E F	$0.544 \\ 0.251 \\ 0.030 \\ 0.00$	104.1	98.08	ANNU ANNU WAVY STRA FULL STRA
47	A B C D E F	0.360 0.071 0.000 0.000 0.000 0.000	102.8	70.45	ANNU WAVY STRA STRA STRA STRA
48	A B C D E F	$0.426 \\ 0.071 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	103.7	63.77	ANNU WAVY STRA STRA STRA STRA

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
49	A	0.098	103.2	47.08	WAVY
	В	0.000			STRA
	C	0.000			STRA
	D	0.000			STRA
	E	0.000			STRA
	F	0.000			STRA
50	А	0.107	103.7	51.25	WAVY
	В	0.000			STRA
	C	0.000			STRA
	D	0.000			STRA
	E	0.000			STRA
	F	0.000			STRA

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
1	A B C D E F	0.663 0.422 0.195 0.005 0.000 0.000	106.1	144.11	ANNU ANNU ANNU ANWA FULL FULL
2	A B C D E F	0.704 0.452 0.254 0.057 0.000 0.000	106.1	147.80	ANNU ANNU ANNU ANWA FULL FULL
3	A B C D E F	0.734 0.511 0.305 0.088 0.000 0.000	106.9	144.11	ANNU ANNU ANNU ANWA FULL FULL
4	A B C D E F	0.750 0.568 0.398 0.201 0.000 0.000	106.9	147.80	ANNU ANNU ANNU ANNU FULL FULL
5	A B C D E F	$0.691 \\ 0.440 \\ 0.262 \\ 0.049 \\ 0.000 \\ 0.000 \\ 0.000$	105.2	133.06	ANNU ANNU ANNU ANWA FULL FULL
6	A B C D E F	$0.569 \\ 0.258 \\ 0.014 \\ 0.000 \\ 0.00$	104.0	136.75	ANNU ANNU SLUG FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
7	A B C D E F	0.602 0.272 0.023 0.000 0.000 0.000	104.0	144.11	ANNU ANNU SLUG FULL FULL FULL
8	A B C D E F	0.610 0.329 0.121 0.000 0.000 0.000	104.8	147.80	ANNU ANNU ANNU FULL FULL FULL
9	A B C D E F	0.579 0.269 0.070 0.000 0.000 0.000	102.5	107.28	ANNU ANNU ANWA FULL FULL FULL
10	A B C D E F	$0.534 \\ 0.218 \\ 0.017 \\ 0.000 \\ 0.00$	102.5	99.92	ANNU ANNU SLUG FULL FULL FULL
11	A B C D E F	$0.536 \\ 0.217 \\ 0.034 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.5	99.92	ANNU ANNU SLUG FULL FULL FULL
12	A B C D E F	$0.606 \\ 0.339 \\ 0.123 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.5	99.92	ANNU ANNU FULL FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
13	A B C D E F	0.511 0.229 0.038 0.000 0.000 0.000	102.5	99.92	ANNU ANNU SLUG FULL FULL FULL
14	A B C D E F	0.545 0.242 0.047 0.000 0.000 0.000	101.4	85.19	ANNU ANNU SLUG FULL FULL FULL
15	A B C D E F	$0.564 \\ 0.274 \\ 0.049 \\ 0.000 \\ 0.00$	101.4	88.87	ANNU ANNU SLUG FULL FULL FULL
16	A B C D E F	0.580 0.297 0.040 0.000 0.000 0.000	101.4	92.55	ANNU ANNU SLUG FULL FULL FULL
17	A B C D E F	0.504 0.279 0.072 0.000 0.000 0.000	101.4	92.55	ANNU ANNU SLUG FULL FULL FULL
18	A B C D E F	$0.564 \\ 0.331 \\ 0.127 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.3	88.87	ANNU ANNU ANWA FULL FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.327 0.035 0.000 0.000 0.000 0.000	101.4	60.43	ANNU SLUG FULL FULL FULL FULL
20	A B C D E F	$\begin{array}{c} 0.353 \\ 0.053 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.4	57.51	ANNU SLUG FULL FULL FULL FULL
21	A B C D E F	$0.468 \\ 0.150 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	57.51	ANNU ANWA FULL FULL FULL FULL
22	A B C D E F	$0.652 \\ 0.310 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	57.51	ANNU ANNU FULL FULL FULL FULL
23	A B C D E F	$0.433 \\ 0.124 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	57.92	ANNU ANWA FULL FULL FULL FULL
24	A B C D E F	$\begin{array}{c} 0.334 \\ 0.045 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.4	58.76	ANNU SLUG FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
25	A B C D E F	$\begin{array}{c} 0.535 \\ 0.205 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.4	56.67	ANNU ANWA FULL FULL FULL FULL
26	A B C D E F	0.627 0.338 0.138 0.000 0.000 0.000	110.8	221.45	ANNU ANNU ANNU ANWA FULL FULL
27	A B C D E F	0.635 0.378 0.173 0.000 0.000 0.000	112.1	228.82	ANNU ANNU ANNU ANWA FULL FULL
28	A B C D E F	0.636 0.377 0.179 0.006 0.000 0.000	112.1	232.50	ANNU ANNU ANNU ANWA FULL FULL
29	A B C D E F	0.678 0.404 0.196 0.002 0.000 0.000	112.1	225.14	ANNU ANNU ANNU ANWA FULL FULL
30	A B C D E F	0.637 0.363 0.212 0.042 0.000 0.000	110.8	203.04	ANNU ANNU ANNU ANNU FULL FULL

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Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.645 0.333 0.168 0.015 0.000 0.000	110.1	199.36	ANNU ANNU ANNU ANWA FULL FULL
32	A B C D E F	0.660 0.359 0.138 0.000 0.000 0.000	110.1	206.72	ANNU ANNU ANNU ANWA FULL FULL
33	A B C D E F	0.651 0.345 0.160 0.026 0.000 0.000	110.1	203.04	ANNU ANNU ANNU ANWA FULL FULL
34	A B C D E F	0.655 0.349 0.140 0.008 0.000 0.000	110.1	203.04	ANNU ANNU ANNU ANWA FULL FULL
35	A B C D E F	$0.645 \\ 0.360 \\ 0.146 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000$	109.4	197.52	ANNU ANNU ANNU ANWA FULL FULL
36	A B C D E F	$\begin{array}{c} 0.658 \\ 0.396 \\ 0.243 \\ 0.044 \\ 0.000 \\ 0.000 \end{array}$	112.0	232.50	ANNU ANNU ANNU ANNU FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
37	A B C D E F	$\begin{array}{c} 0.666 \\ 0.412 \\ 0.245 \\ 0.048 \\ 0.000 \\ 0.000 \end{array}$	112.6	239.87	ANNU ANNU ANNU ANNU FULL FULL
38	A B C D E F	0.662 0.406 0.213 0.017 0.000 0.000	112.0	228.82	ANNU ANNU ANNU ANNU FULL FULL
39	A B C D E F	0.664 0.410 0.197 0.009 0.000 0.000	112.0	228.82	ANNU ANNU ANNU ANWA FULL FULL
40	A B C D E F	0.665 0.409 0.196 0.003 0.000 0.000	112.0	226.98	ANNU ANNU ANNU ANWA FULL FULL
41	A B C D E F	0.675 0.430 0.225 0.014 0.000 0.000	113.3	239.87	ANNU ANNU ANNU ANWA FULL FULL
42	A B C D E F	0.666 0.401 0.182 0.006 0.000 0.000	105.2	147.80	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	Т₅, av °С	G kg/m².s	Observed flow regime
43	A B C D E F	0.684 0.432 0.221 0.021 0.000 0.000	105.2	136.75	ANNU ANNU ANNU SLUG FULL FULL
44	A B C D E F	0.711 0.467 0.264 0.080 0.000 0.000	106.0	140.43	ANNU ANNU ANNU ANWA FULL FULL
45	A B C D E F	0.708 0.474 0.271 0.077 0.000 0.000	106.0	133.06	ANNU ANNU ANNU ANWA FULL FULL
46	A B C D E F	0.276 0.000 0.000 0.000 0.000 0.000	100.1	25.39	SLUG FULL FULL FULL FULL FULL
47	A B C D E F	$\begin{array}{c} 0.424 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.6	32.47	ANWA FULL FULL FULL FULL FULL
48	A B C D E F	0.282 0.000 0.000 0.000 0.000 0.000 0.000	100.6	33.31	ANWA FULL FULL FULL FULL FULL

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Run number	Visual observation section	x	T <sub>s, av</sub> °C	G kg/m².s	Observed flow regime
49	A B C D E F	$\begin{array}{c} 0.171 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.6	32.05	SLUG FULL FULL FULL FULL FULL
50	A B C D E F	$0.101 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.6	32.89	SLUG FULL FULL FULL FULL FULL
51	A B C D E F	$\begin{array}{c} 0.221 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.6	42.07	ANWA FULL FULL FULL FULL FULL
52	A B C D E F	$0.149 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.6	40.82	SLUG FULL FULL FULL FULL FULL
53	A B C D E F	$0.141 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.1	44.99	SLUG FULL FULL FULL FULL FULL
54	A B C D E F	0.438 0.067 0.000 0.000 0.000 0.000 0.000	100.6	45.82	ANNU SLUG FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
55	A B C D E F	$\begin{array}{c} 0.345 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.6	44.99	ANNU FULL FULL FULL FULL FULL
56	A B C D E F	$0.564 \\ 0.208 \\ 0.009 \\ 0.000 \\ 0.00$	101.7	114.65	ANNU ANNU SLUG FULL FULL FULL
57	A B C D E F	0.416 0.091 0.000 0.000 0.000 0.000	100.8	99.92	ANNU ANWA FULL FULL FULL FULL
58	A B C D E F	$\begin{array}{c} 0.424 \\ 0.143 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.8	103.60	ANNU ANNU FULL FULL FULL FULL
59	A B C D E F	0.423 0.121 0.000 0.000 0.000 0.000	100.8	99.92	ANNU ANNU FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
1	A B C D E F	$0.495 \\ 0.129 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.2	44.99	ANNU SLUG FULL FULL FULL FULL
2	A B C D E F	$0.442 \\ 0.059 \\ 0.000 \\ 0.00$	101.5	62.10	ANNU SLUG FULL FULL FULL FULL
3	A B C D E F	$\begin{array}{c} 0.344 \\ 0.103 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.5	65.02	ANNU SLUG FULL FULL FULL FULL
4	A B C D E F	$\begin{array}{c} 0.232 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.6	46.24	ANWA FULL FULL FULL FULL FULL
5	A B C D E F	0.232 0.000 0.000 0.000 0.000 0.000	100.6	63.77	ANNU FULL FULL FULL FULL FULL
6	A B C D E F	0.273 0.008 0.000 0.000 0.000 0.000	100.6	60.85	ANNU SLUG FULL FULL FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
7	A B C D E F	$0.477 \\ 0.226 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	96.23	ANNU ANNU SLUG FULL FULL FULL
8	A B C D E F	$0.501 \\ 0.247 \\ 0.064 \\ 0.000 \\ 0.00$	101.4	96.23	ANNU ANNU ANWA FULL FULL FULL
9	A B C D E F	$0.509 \\ 0.262 \\ 0.043 \\ 0.000 \\ 0.00$	101.4	98.08	ANNU ANNU ANWA FULL FULL FULL
10	A B C D E F	$0.509 \\ 0.219 \\ 0.024 \\ 0.000 \\ 0.00$	101.4	98.08	ANNU ANNU SLUG FULL FULL FULL
11	A B C D E F	0.551 0.197 0.028 0.000 0.000 0.000	101.4	92.55	ANNU ANNU SLUG FULL FULL FULL
12	A B C D E F	$0.411 \\ 0.149 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	96.23	ANNU ANNU FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
13	A B C D E F	$\begin{array}{c} 0.424 \\ 0.094 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.4	96.23	ANNU ANWA FULL FULL FULL FULL
14	A B C D E F	0.585 0.239 0.000 0.000 0.000 0.000	102.9	136.75	ANNU ANNU ANWA FULL FULL FULL
15	A B C D E F	0.555 0.209 0.003 0.000 0.000 0.000	101.8	140.43	ANNU ANNU SLUG FULL FULL FULL
16	A B C D E F	0.536 0.228 0.011 0.000 0.000 0.000	101.8	136.75	ANNU ANNU SLUG FULL FULL FULL
17	A B C D E F	0.533 0.225 0.004 0.000 0.000 0.000	100.9	122.02	ANNU ANNU SLUG FULL FULL FULL
18	A B C D E F	0.582 0.281 0.055 0.000 0.000 0.000	101.8	140.43	ANNU ANNU ANWA FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.652 0.366 0.172 0.000 0.000 0.000	108.9	184.63	ANNU ANNU ANNU ANWA FULL FULL
20	A B C D E F	0.637 0.375 0.177 0.000 0.000 0.000	108.2	177.26	ANNU ANNU ANNU ANWA FULL FULL
21	A B C D E F	0.692 0.449 0.247 0.063 0.000 0.000	109.6	191.99	ANNU ANNU ANNU FULL FULL
22	A B C D E F	$0.691 \\ 0.426 \\ 0.201 \\ 0.009 \\ 0.000 \\ 0.000 \\ 0.000$	108.9	184.63	ANNU ANNU ANNU ANWA FULL FULL
23	А В С Д Е F	0.595 0.275 0.025 0.000 0.000 0.000	107.4	188.31	ANNU ANNU ANWA FULL FULL FULL
24	A B C D E F	$0.592 \\ 0.270 \\ 0.043 \\ 0.000 \\ 0.00$	107.4	188.31	ANNU ANNU ANWA FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
25	A B C D E F	0.582 0.283 0.078 0.000 0.000 0.000	105.4	162.53	ANNU ANNU ANNU FULL FULL FULL
26	A B C D E F	0.565 0.253 0.046 0.000 0.000 0.000	104.6	151.48	ANNU ANNU ANWA FULL FULL FULL
27	A B C D E F	0.528 0.229 0.032 0.000 0.000 0.000	103.7	140.43	ANNU ANNU ANWA FULL FULL FULL
28	A B C D E F	0.553 0.232 0.001 0.000 0.000 0.000	103.7	144.11	ANNU ANNU SLUG FULL FULL FULL
29	A B C D E F	0.647 0.353 0.145 0.001 0.000 0.000	108.5	203.04	ANNU ANNU ANNU ANWA FULL FULL
30	A B C D E F	0.667 0.390 0.197 0.052 0.000 0.000	110.3	223.30	ANNU ANNU ANNU FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.676 0.403 0.189 0.000 0.000 0.000	111.3	223.30	ANNU ANNU ANNU ANWA FULL FULL
32	A B C D E F	0.666 0.390 0.191 0.026 0.000 0.000	110.7	221.45	ANNU ANNU ANNU ANWA FULL FULL
33	A B C D E F	$0.197 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.5	22.44	SLUG FULL FULL FULL FULL FULL
34	A B C D E F	$0.111 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.5	23.03	SLUG FULL FULL FULL FULL FULL
35	A B C D E F	0.069 0.000 0.000 0.000 0.000 0.000	100.5	23.91	SLUG FULL FULL FULL FULL FULL
36	A B C D E F	0.241 0.000 0.000 0.000 0.000 0.000	100.5	23.62	SLUG FULL FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
37	A B C D E F	$\begin{array}{c} 0.397 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.5	32.47	ANWA FULL FULL FULL FULL FULL
38	A B C D E F	$\begin{array}{c} 0.354 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.5	34.56	ANWA FULL FULL FULL FULL FULL
39	A B C D E F	$\begin{array}{c} 0.280 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.5	38.73	ANWA FULL FULL FULL FULL FULL
40	A B C D E F	0.436 0.000 0.000 0.000 0.000 0.000	100.4	36.64	ANNU FULL FULL FULL FULL FULL
41	A B C D E F	$\begin{array}{c} 0.340 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	100.4	38.73	ANWA FULL FULL FULL FULL FULL
42	A B C D E F	$0.286 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	100.4	42.90	ANWA FULL FULL FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
43	A B C D E F	0.197 0.000 0.000 0.000 0.000 0.000 0.000	100.4	43.74	SLUG FULL FULL FULL FULL FULL
44	A B C D E F	0.676 0.374 0.115 0.000 0.000 0.000	101.9	96.23	ANNU ANNU ANWA FULL FULL FULL
45	A B C D E F	0.612 0.350 0.125 0.000 0.000 0.000	101.0	81.50	ANNU ANNU ANWA FULL FULL FULL
46	A B C D E F	0.554 0.277 0.086 0.000 0.000 0.000	101.0	88.87	ANNU ANNU ANWA FULL FULL FULL
<u>4</u> 7	A B C D E F	0.561 0.285 0.051 0.000 0.000 0.000	101.0	88.87	ANNU ANNU SLUG FULL FULL FULL
48	A B C D E F	0.651 0.378 0.130 0.000 0.000 0.000	101.0	74.14	ANNU ANNU ANWA FULL FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
49	A B C D E F	$\begin{array}{c} 0.639 \\ 0.347 \\ 0.062 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	101.0	61.68	ANNU ANNU SLUG FULL FULL FULL
50	A B C D E F	0.493 0.157 0.000 0.000 0.000 0.000	101.0	53.33	ANNU ANWA FULL FULL FULL FULL
51	A B C D E F	0.557 0.226 0.000 0.000 0.000 0.000	101.0	53.33	ANNU ANWA FULL FULL FULL FULL
52	A B C D E F	0.673 0.405 0.200 0.038 0.000 0.000	113.0	269.33	ANNU ANNU ANNU ANWA FULL FULL
53	A B C D E F	0.672 0.410 0.207 0.044 0.000 0.000	113.7	276.70	ANNU ANNU ANNU ANWA FULL FULL
54	A B C D E F	0.670 0.404 0.223 0.058 0.000 0.000	114.3	276.70	ANNU ANNU ANNU ANNU FULL FULL

Run number	Visual observation section	x	Т₅, av °С	G kg/m².s	Observed flow regime
55	A	0.654	113.7	269.33	ANNU
	В	0.415			ANNU
	С	0.223			ANNU
	D	0.052			ANNU
	E	0.000			FULL
	F	0.000			FULL

TABLE B.	6	Flow-regime	parameters	for	data	set	in	+5°	Γ	upward	]
		i.	nclination	(con	t'd.)						

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
1	A B C D E F	0.540 0.189 0.000 0.000 0.000 0.000 0.000	101.4	47.08	ANNU ANWA FULL FULL FULL FULL
2	A B C D E F	$0.449 \\ 0.119 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	101.4	50.83	ANNU SLUG FULL FULL FULL FULL
3	A B C D E F	$0.449 \\ 0.177 \\ 0.000 \\ 0.00$	102.7	63.35	ANNU ANWA FULL FULL FULL FULL
4	A B C D E F	$0.401 \\ 0.145 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.7	69.19	ANNU ANWA FULL FULL FULL FULL
5	A B C D E F	$0.399 \\ 0.125 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	102.7	61.68	ANNU SLUG FULL FULL FULL FULL
6	A B C D E F	$0.277 \\ 0.013 \\ 0.000 \\ 0.00$	102.7	61.26	ANNU SLUG FULL FULL FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
7	A B C D E F	$\begin{array}{c} 0.261 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 \end{array}$	102.7	59.59	ANNU FULL FULL FULL FULL FULL
8	A B C D E F	0.537 0.209 0.000 0.000 0.000 0.000	102.7	65.44	ANNU ANNU FULL FULL FULL FULL
9	A B C D E F	$0.588 \\ 0.282 \\ 0.019 \\ 0.000 \\ 0.00$	103.4	74.20	ANNU ANNU SLUG FULL FULL FULL
10	A B C D E F	0.687 0.408 0.149 0.000 0.000 0.000	103.4	71.28	ANNU ANNU ANWA FULL FULL FULL
11	A B C D E F	0.561 0.311 0.083 0.000 0.000 0.000	103.4	75.45	ANNU ANNU ANWA FULL FULL FULL
12	A B C D E F	$0.518 \\ 0.275 \\ 0.041 \\ 0.000 \\ 0.00$	103.4	77.12	ANNU ANNU SLUG FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
13	A B C D E F	0.562 0.304 0.068 0.000 0.000 0.000	103.4	77.12	ANNU ANNU SLUG FULL FULL FULL
14	A B C D E F	0.560 0.224 0.000 0.000 0.000 0.000	103.9	129.38	ANNU ANNU SLUG FULL FULL FULL
15	A B C D E F	0.532 0.217 0.000 0.000 0.000 0.000	103.9	125.70	ANNU ANNU SLUG FULL FULL FULL
16	A B C D E F	0.590 0.289 0.049 0.000 0.000 0.000	103.9	125.70	ANNU ANNU ANWA FULL FULL FULL
17	A B C D E F	0.615 0.281 0.063 0.000 0.000 0.000	104.7	136.75	ANNU ANNU ANWA FULL FULL FULL
18	A B C D E F	$0.614 \\ 0.276 \\ 0.076 \\ 0.000 \\ 0.00$	104.7	136.75	ANNU ANNU FULL FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
19	A B C D E F	0.602 0.286 0.083 0.000 0.000 0.000	104.7	133.06	ANNU ANNU ANNU FULL FULL FULL
20	A B C D E F	0.596 0.297 0.116 0.000 0.000 0.000	104.7	133.06	ANNU ANNU ANNU FULL FULL FULL
21	A B C D E F	0.565 0.232 0.005 0.000 0.000 0.000	104.7	140.43	ANNU ANNU SLUG FULL FULL FULL
22	A B C D E F	0.562 0.230 0.015 0.000 0.000 0.000	103.9	136.75	ANNU ANNU SLUG FULL FULL FULL
23	A B C D E F	0.627 0.359 0.154 0.009 0.000 0.000	109.4	203.04	ANNU ANNU ANNU ANWA FULL FULL
24	A B C D E F	0.622 0.347 0.187 0.036 0.000 0.000	109.4	203.04	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T₅,av °C	G kg/m².s	Observed flow regime
25	A B C D E F	0.622 0.377 0.218 0.069 0.000 0.000	110.1	214.09	ANNU ANNU ANNU ANNU FULL FULL
26	A B C D E F	0.656 0.375 0.170 0.000 0.000 0.000	109.4	195.67	ANNU ANNU ANNU ANWA FULL FULL
27	A B C D E F	$0.646 \\ 0.388 \\ 0.178 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000$	109.4	195.67	ANNU ANNU ANNU ANWA FULL FULL
28	A B C D E F	$0.664 \\ 0.417 \\ 0.213 \\ 0.045 \\ 0.000 \\ 0.000$	110.8	214.09	ANNU ANNU ANNU ANNU FULL FULL
29	A B C D E F	0.641 0.391 0.201 0.050 0.000 0.000	110.1	199.36	ANNU ANNU ANNU ANNU FULL FULL
30	A B C D E F	0.669 0.427 0.235 0.077 0.000 0.000	110.1	203.04	ANNU ANNU ANNU ANNU FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
31	A B C D E F	0.663 0.403 0.205 0.006 0.000 0.000	112.6	228.82	ANNU ANNU ANNU ANWA FULL FULL
32	A B C D E F	$\begin{array}{c} 0.666 \\ 0.405 \\ 0.203 \\ 0.034 \\ 0.000 \\ 0.000 \end{array}$	112.0	228.82	ANNU ANNU ANNU ANWA FULL FULL
33	A B C D E F	0.660 0.399 0.199 0.053 0.000 0.000	112.0	232.50	ANNU ANNU ANNU ANNU FULL FULL
34	A B C D E F	0.663 0.397 0.215 0.067 0.000 0.000	112.6	232.50	ANNU ANNU ANNU FULL FULL
35	A B C D E F	0.672 0.418 0.211 0.015 0.000 0.000	114.9	254.60	ANNU ANNU ANNU ANWA FULL FULL
36	A B C D E F	0.668 0.402 0.178 0.001 0.000 0.000	114.2	258.28	ANNU ANNU ANNU ANWA FULL FULL

Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
37	A B C D E F	0.668 0.401 0.178 0.015 0.000 0.000	114.9	261.97	ANNU ANNU ANNU ANWA FULL FULL
38	A B C D E F	0.666 0.396 0.191 0.027 0.000 0.000	114.2	261.97	ANNU ANNU ANNU ANWA FULL FULL
39	A B C D E F	0.661 0.386 0.195 0.045 0.000 0.000	113.6	258.28	ANNU ANNU ANNU FULL FULL
40	A B C D E F	0.659 0.385 0.214 0.099 0.000 0.000	113.6	261.97	ANNU ANNU ANNU FULL FULL
41	A B C D E F	0.633 0.370 0.159 0.000 0.000 0.000	107.3	162.53	ANNU ANNU ANNU ANWA FULL FULL
42	A B C D E F	0.674 0.390 0.178 0.000 0.000 0.000	108.1	166.21	ANNU ANNU ANNU ANWA FULL FULL

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
43	A B C D E F	0.665 0.419 0.209 0.023 0.000 0.000	108.1	162.53	ANNU ANNU ANNU ANWA FULL FULL
44	A B C D E F	0.678 0.440 0.223 0.029 0.000 0.000	107.3	158.84	ANNU ANNU ANNU ANWA FULL FULL
45	A B C D E F	0.572 0.233 0.000 0.000 0.000 0.000	107.3	166.21	ANNU ANNU ANWA FULL FULL FULL
46	A B C D E F	0.546 0.258 0.039 0.000 0.000 0.000	106.6	166.21	ANNU ANNU ANWA FULL FULL FULL
47	A B C D E F	0.597 0.273 0.043 0.000 0.000 0.000	106.6	162.53	ANNU ANNU ANNU FULL FULL FULL
48	А В С D Е F	0.586 0.255 0.027 0.000 0.000 0.000	105.8	162.53	ANNU ANNU ANWA FULL FULL FULL

TABLE B.7	Flow-regime parameters	for data set	in	+10°	Ľ	upward	]
	inclination	(cont'd.)					

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Run number	Visual observation section	x	T₅, av °C	G kg/m².s	Observed flow regime
49	A B C	0.558 0.242 0.012	103.2	114.65	ANNU ANNU SLUG
	D E F	0.000 0.000 0.000			FULL FULL FULL
50	A B C D E F	0.522 0.209 0.007 0.000 0.000 0.000	103.2	114.65	ANNU ANNU SLUG FULL FULL FULL
51	A B C D E F	$0.559 \\ 0.242 \\ 0.028 \\ 0.000 \\ 0.000 \\ 0.000 \\ 0.000 $	103.2	114.65	ANNU ANNU SLUG FULL FULL FULL
52	A B C D E F	$0.556 \\ 0.234 \\ 0.022 \\ 0.000 \\ 0.00$	104.1	136.75	ANNU ANNU SLUG FULL FULL FULL

TABLE B.7	Flow-regime parameters	for data set	: in +10°	[ upward ]
	inclination	(cont'd.)		

#### Appendix C

### **ESTIMATION OF EXPERIMENTAL UNCERTAINTY**

This appendix describes the procedure followed in estimating the experimental uncertainty of measured and calculated variables described in the experimental study.

The uncertainty in measured variables such as temperatures, static pressures and volume flow rates were obtained from calibration curves. All pressure gauges, thermocouples and flow meters were calibrated prior to the experiment. From the calibration data of an instrument a least sum of square curve fit was obtained. This least sum of square fit to the calibration data [ of a given instrument ] provided an estimate of the uncertainty in the observed value [ using that instrument ]. From the curve fit the uncertainties were estimated at a confidence level of 20:1 odds or 95% probability. The confidence level indicates that the odds are 20 to 1 against the uncertainty for a measurement  $\chi_i$  being larger than  $\pm\delta\chi_i$ . In order to estimate the odds the standard deviation (S<sub>(N)</sub>) of the calibration curve was obtained. The uncertainty in the measurement is estimated by

$$\delta \chi_i = \frac{\overline{t} S_{(N)}}{\sqrt{N}} \tag{C.1}$$

where t is the Student's t values appropriate for the number of samples N and the confidence level desired.

The uncertainties in calculated variables [such as such as mass flux (G), quality

(x), superficial liquid velocity ( $V_{LS}$ ) and superficial vapor velocity ( $V_{VS}$ )] were estimated using the method suggested by Moffat(1988). If R is the calculated value from a set of measurements  $\chi_1$ ,  $\chi_2$ ,  $\chi_3$ , etc. using a data interpretation program then

$$R = R(\chi_1, \chi_2, \chi_3, \dots, \chi_n)$$
 (C.2)

The partial derivative of R with respect to  $\chi_n$  is defined as the sensitivity coefficient for the result R with respect to measurement  $\chi_n$ . When several independent measurements are used in the function R, the individual terms are combined by a rootsum-square method given below.

$$(\delta R)^2 = \sum_{i=1}^{N} \left( \frac{\partial R}{\partial \chi_i} \delta \chi_i \right)^2$$
(C.3)

The relative error is the fraction  $\delta R/R$ . The uncertainties reported in the following pages are the relative errors given as percentage.

A computer code was used to reduce the experimental data. The estimated uncertainties in the measured variables were supplied to this computer program that converted the measured data [ such as pressures, temperatures and flow rates ] to the final form of reduced data [ such as G, x and  $V_{vs}$ , and  $V_{Ls}$  ]. In order to calculate the superficial velocities the vapor quality and the mass flow rate are required. The vapor quality in each visual section was calculated by using the following relationship.

$$x_{i} = \frac{h_{in} - \frac{1}{\dot{m}_{s}} \sum_{j=1}^{6} [\dot{m}_{W,i} C_{PL} (T_{out,i} - T_{in,i})] - h_{f}}{h_{fg}}$$
(C.4)

where  $h_{in}$  is the enthalpy of steam at the inlet to the test section;  $\dot{m}_{w,i}$  is the mass flow rate of cooling water to i<sup>th</sup> heat exchanger; C<sub>PL</sub> is the average specific heat of liquid water;  $\mathring{m}_s$  is the steam mass flow rate;  $h_f$  and  $h_{fg}$  are the enthalpy of liquid water and the latent heat of vaporization respectively at the saturation temperature; and  $T_{OUT,i}$  and  $T_{IN,i}$  are the temperature of cooling water leaving and temperature of cooling water entering respectively in the i<sup>th</sup> heat exchanger. For any given test run the variables such as G, x,  $V_{\mbox{\tiny LS}}$  and  $V_{\mbox{\tiny VS}}$  were first calculated by the computer program using the observed values of the measured variables for that run. The resulting values of G, x,  $V_{LS}$  and  $V_{VS}$  were stored as base values for that run under consideration. Each of the measured variables used in the computer program [ such as pressures, temperatures and flow rates ] were perturbed sequentially by adding the uncertainty in the measurement [ estimated from the calibration curves ] to the respective observed value of the variable. The difference between the resulting value [after perturbation] and the base amount was then squared and summed as the measured variables were perturbed one by one. The root-sumsquare of all differences was recorded as the uncertainty in the calculated variable. The relative uncertainty was obtained by dividing the uncertainty by the base value. This relative uncertainty is reported as a percentage.

Run No.	Visual	G	I %	V <sub>oe</sub>	V	Run	Visual	G	Ĩ	Vas	V
			*		~	<u></u>	section		*	*	\$
1	A B C D E F	2.54	0.52 0.95 1.65 8.46 0.00 0.00	2.78 3.08 3.65 10.14 0.00 0.00	2.74 2.38 2.26 2.19 2.54 2.54	14	A B C D E	2.64	0.76 1.72 0.00 0.00 0.00	2.99 3.70 0.00 0.00 0.00	2.90 2.51 2.64 2.64 2.64
2	A B C D E F	2.54	0.52 0.96 1.78 8.92 0.00 0.00	2.77 3.08 3.76 10.59 0.00 0.00	2.75 2.38 2.25 2.19 2.54 2.54	15	A B C D E F	3.43	1.48 6.95 0.00 0.00 0.00 0.00	4.37 9.51 0.00 0.00 0.00 0.00	3.17 2.77 3.43 3.43 3.43 3.43
3	А В С С С С С Я Г	2.33	0.39 0.67 1.08 4.39 30.00 0.00	2.48 2.64 2.92 5.79 31.36 0.00	2.70 2.33 2.20 2.14 2.11 2.33	16	A B C D E F	3.98	4.83 1428.31 0.00 0.00 0.00 0.00	7.83 1468.01 0.00 0.00 0.00 0.00	3.41 2.79 3.98 3.98 3.98 3.98
٩	А В С D Е У	2.16	0.34 0.64 1.49 5.95 0.00 0.00	2.26 2.39 · 2.89 6.82 0.00 0.00	2.66 2.30 2.18 2.12 2.16 2.16	17	λ B C D Z F	3.09	5.75 67.71 0.00 0.00 0.00 0.00	7.58 70.03 0.00 0.00 0.00 0.00	3.06 2.67 3.09 3.09 3.09 3.09
5	A B C D E F	2.12	0.61 1.24 2.58 48.06 0.00 0.00	2.29 2.62 3.62 48.63 0.00 0.00	2.73 2.32 2.18 2.10 2.12 2.12	18	A B C D Z F	5.13	274.16 0.00 0.00 0.00 0.00 0.00	285.28 0.00 0.00 0.00 0.00 0.00	3.64 5.13 5.13 5.13 5.13 5.13 5.13
6	A B C D Z F	2.46	0.52 0.98 2.08 0.00 0.00 0.00	2.67 2.96 3.82 0.00 0.00 0.00	2.79 2.42 2.29 2.46 2.46 2.46	19	A B C D E F	4.87	4.24 0.00 0.00 0.00 0.00 0.00	8.40 0.00 0.00 0.00 0.00 0.00	3.67 4.87 4.87 4.87 4.87 4.87
7	A B C D E F	2.73	0.82 2.06 12.33 0.00 0.00 0.00	3.16 4.15 14.07 0.00 0.00 0.00	2.67 2.43 2.34 2.73 2.73 2.73 2.73	20	A B C D E F	7.40	18.94 0.00 0.00 0.00 0.00 0.00	25.95 0.00 0.00 0.00 0.00 0.00	4.87 7.40 7.40 7.40 7.40 7.40
8	A B C D B F	2.24	1.23 2.65 6.18 72.24 0.00 0.00	2.73 3.81 7.12 73.21 0.00 0.00	2.90 2.38 2.22 2.16 2.24 2.24	21	А В С D 2 F	4.33	2.54 11.46 0.00 0.00 0.00 0.00	6.25 15.14 0.00 0.00 0.00 0.00	3.49 3.12 4.33 4.33 4.33 4.33
9	A B C D Z F	2.67	2.09 4.05 16.02 0.00 0.00 0.00	3.88 5.70 17.59 0.00 0.00 0.00	2.93 2.52 2.35 2.67 2.67 2.67	22	A B C D Z F	3.85	1.79 5.40 0.00 0.00 0.00 0.00	5.09 8.57 0.00 0.00 0.00 0.00	3.29 2.92 3.85 3.85 3.85 3.85 3.85
10	A B C D E F	3.66	2.69 11.14 0.00 0.00 0.00 0.00	5.61 13.99 0.00 0.00 0.00 0.00	3.20 2.83 3.66 3.66 3.66 3.66 3.66	23	Х В С D E F	5.30	4.19 0.00 0.00 0.00 0.00 0.00	8.87 0.00 0.00 0.00 0.00 0.00	3.82 4.95 5.30 5.30 5.30 5.30
11	A B C D E F	3.93	3.38 72.96 0.00 0.00 0.00 0.00	6.46 77.06 0.00 0.00 0.00 0.00	3.40 2.96 3.93 3.93 3.93 3.93	24	<b>Х</b> A C D M F	3.73	1.73 4.94 0.00 0.00 0.00 0.00	4.89 7.91 0.00 0.00 0.00 0.00	3.30 2.94 2.75 3.73 3.73 3.73
12	A B C D E F	4.60	3.22 116.12 0.00 0.00 0.00 0.00	7.18 122.97 0.00 0.00 0.00 0.00	3.52 3.15 4.60 4.60 4.60 4.60	25	A B C D N F	3.98	2.02 6.63 0.00 0.00 0.00 0.00	5.41 9.88 0.00 0.00 0.00 0.00	3.38 3.01 3.98 3.98 3.98 3.98 3.98
13	A B C D E F	4.10	4.07 0.00 0.00 0.00 0.00 0.00	7.26 0.00 0.00 0.00 0.00 0.00	3.49 4.10 4.10 4.10 4.10 4.10	26	A B C D Z F	3.14	1.14 2.52 13.53 0.00 0.00 0.00	3.80 5.02 15.90 0.00 0.00 0.00	3.05 2.65 2.49 3.14 3.14 3.14

TABLE C.1 Experimental uncertainty estimates in the horizontal data set

Pre -- 6--

Run No.	Visual	G	ĭ	V <sub>79</sub>	VL2	Run	Visual	G	x	Vaa	V
<u> </u>				3	*	- <u>No.</u>	section	%	\$	*	Š.
27	A B C D E F	3.27	1.20 2.92 20.74 0.00 0.00 0.00	4.01 5.58 23.44 0.00 0.00 0.00	3.04 2.65 2.50 3.27 3.27 3.27	40	A B C D Z F	3.14	2.02 4.73 0.00 0.00 0.00 0.00	4.40 7.00 0.00 0.00 0.00 0.00	3.14 2.66 2.39 3.14 3.14 3.14
28	A B C D E F	3.11	1.06 2.45 8.99 0.00 0.00 0.00	3.72 4.94 11.35 0.00 0.00 0.00	3.02 2.62 2.48 3.11 3.11 3.11	41	A B C D E F	3.02	1.82 4.50 55.17 0.00 0.00 0.00	4.09 6.60 57.74 0.00 0.00 0.00	3.12 2.63 2.46 3.02 3.02 3.02
29	A B C D E F	3.27	1.26 3.05 16.20 0.00 0.00 0.00	4.03 5.65 18.74 0.00 0.00 0.00	3.10 2.71 2.56 3.27 3.27 3.27	42	Х В С D E F	2.73	0.99 1.63 3.01 0.00 0.00 0.00	3.21 3.74 5.00 0.00 0.00 0.00	2.95 2.54 2.38 2.69 2.73 2.73
30	A B C D E F	3.07	1.65 3.62 48.33 0.00 0.00 0.00	4.05 5.88 50.94 0.00 0.00 0.00	3.04 2.64 2.47 3.07 3.07 3.07	43	λ B C D E F	2.85	1.19 2.16 4.44 0.00 0.00 0.00	3.48 4.33 6.49 0.00 0.00 0.00	2.99 2.57 2.42 2.85 2.85 2.85
31	A B C D E F	2.85	0.96 1.99 7.18 0.00 0.00 0.00	3.34 4.19 9.11 0.00 0.00 0.00	2.96 2.57 2.42 2.85 2.85 2.85 2.85	44	λ B C D Z F	2.98	2.11 4.04 12.50 0.00 0.00 0.00	4.25 6.10 14.53 0.00 0.00 0.00	3.14 2.66 2.49 2.98 2.98 2.98
32	A B C D E F	3.10	1.41 3.12 13.87 0.00 0.00 0.00	3.93 5.48 16.10 0.00 0.00 0.00	3.04 2.66 2.51 3.10 3.10 3.10	45	a B C D E F	2.91	1.92 3.94 22.37 0.00 0.00 0.00	4.02 5.93 24.38 0.00 0.00 0.00	3.12 2.62 2.43 2.91 2.91 2.91
33	λ B C D E F	2.91	1.27 2.59 9.05 0.00 0.00 0.00	3.62 4.76 11.00 0.00 0.00 0.00	3.00 2.62 2.47 2.91 2.91 2.91	46	<b>)</b> В С D Е F	2.10	0.60 0.90 1.37 3.46 0.00 0.00	2.27 2.42 2.71 4.39 0.00 0.00	2.66 2.29 2.16 2.09 2.10 2.10
34	A B C D E F	2.73	1.72 3.87 31.38 0.00 0.00 0.00	3.67 5.61 33.07 0.00 0.00 0.00	3.01 2.56 2.39 2.73 2.73 2.73 2.73	47	A в с р F	2.10	0.59 0.91 1.53 4.00 0.00 0.00	2.27 2.42 2.81 4.87 0.00 0.00	2.66 2.28 2.16 2.09 2.10 2.10
35	A B C D Z F	2.72	1.82 4.08 13.24 0.00 0.00 0.00	3.73 5.79 14.85 0.00 0.00 0.00	3.01 2.54 2.40 2.72 2.72 2.72 2.72	48	Х H C D N F	2.14	0.94 1.73 3.61 0.00 0.00 0.00	2.45 2.96 4.53 0.00 0.00 0.00	2.38 2.38 2.21 2.14 2.14 2.14
36	λ B C D E F	2.70	1.06 1.92 4.18 0.00 0.00 0.00	3.21 3.92 6.00 0.00 0.00 0.00	2.91 2.52 2.38 2.70 2.70 2.70	49	A B C D E F	2.13	0.96 1.78 2.78 29.79 0.00 0.00	2.45 2.97 3.78 30.35 0.00 0.00	2.86 2.37 2.22 2.12 2.13 2.13
37	A B C D N F	2.63	1.23 2.10 5.89 0.00 0.00 0.00	3.23 3.97 7.52 0.00 0.00 0.00	2.94 2.53 2.35 2.63 2.63 2.63	50	<b>λ</b> В С Э Е	2.23	1.13 2.16 4.96 0.00 0.00 0.00	2.66 3.41 5.94 0.00 0.00 0.00	2.94 2.41 2.23 2.14 2.23 2.23 2.23
38	A B C D Z F	2.64	1.64 3.51 16.36 0.00 0.00 0.00	3.49 5.16 17.84 0.00 0.00 0.00	2.97 2.52 2.36 2.64 2.64 2.64	51	א פ ס פ ז	2.15	0.88 1.53 2.60 202.10 0.00 0.00	2.44 2.85 3.69 203.15 0.00 0.00	2.79 2.35 2.21 2.12 2.15 2.15
39	A B C D E F	2.95	1.61 3.33 8.89 0.00 0.00 0.00	3.86 5.44 10.91 0.00 0.00 0.00	3.09 2.62 2.47 2.95 2.95 2.95	52	<b>х</b> вс вс в г	2.21	0.96 1.65 3.28 30.65 0.00 0.00	2.55 3.02 4.39 31.48 0.00 0.00	2.88 2.38 2.21 2.13 2.21 2.21

TABLE C.1 Experimental uncertainty estimates in the horizontal data set (cont'd.)

Run No.	Visual section	G 3	I %	V.76 %	V <sub>15</sub> %	Run No.	Visual section	G %	X S	V.; ; 3	V.2 \$	
53	Х В С D	2.17	0.86 1.44 2.05 4.95	2.46 2.82 3.30 5.89	2.78 2.34 2.21 2.13	66	<b>λ</b> В С D	2.68	1.40 2.47 5.61 121.35	3.38 4.31 7.28 123.89	3.08 2.59 2.41 2.33	
54	E F A B C	2.17	0.00 0.00 1.14 2.11 4.72	0.00 0.00 2.58 3.27 5.59	2.17 2.17 2.96 2.42 2.22	67	e F A B	2.54	0.00 0.00 1.01 1.88	0.00 0.00 3.12 3.82	2.68 2.68 2.97 2.51	
55	D E F	2.21	0.00 0.00 0.00	0.00 0.00 0.00 2.71	2.17 2.17 2.17 3.01		C D E F		4.12 194.32 0.00 0.00	5.89 197.86 0.00 0.00	2.34 2.26 2.64 2.64	
20	BCD NF		2.40 3.97 64.19 0.00 0.00	3.56 4.96 65.00 0.00 0.00	2.44 2.28 2.17 2.21 2.21	68	A B C D E F	2.64	0.90 1.87 3.89 36.72 0.00 0.00	3.06 3.82 5.69 38.59 0.00 0.00	2.97 2.50 2.34 2.26 2.64 2.64	
56	A B C D E F	2.21	1.23 2.46 4.86 0.00 0.00 0.00	2.68 3.60 5.77 0.00 0.00 0.00	3.01 2.44 2.26 2.21 2.21 2.21	69	А В С Д Е	2.42	1.23 2.26 5.37 140.12 0.00 0.00	2.95 3.78 6.68 142.15 0.00 0.00	3.00 2.46 2.27 2.20 2.42 2.42	
57	A B C D E F	2.16	1.04 1.95 3.23 90.43 0.00 0.00	2.51 3.13 4.21 91.13 0.00 0.00	2.93 2.41 2.25 2.15 2.16 2.16	70	A B C D E F	6.06	12.55 0.00 0.00 0.00 0.00 0.00	17.27 0.00 0.00 0.00 0.00 0.00 0.00	4.83 6.06 6.06 6.06 6.06 6.06	
58	λ B C D E F	2.22	1.05 1.82 3.75 31.00 0.00 0.00	2.59 3.13 4.79 31.78 0.00 0.00	2.97 2.43 2.24 2.16 2.22 2.22	71	A B C D E F	5.95	8.93 0.00 0.00 0.00 0.00 0.00	13.66 0.00 0.00 0.00 0.00 0.00	4.72 5.95 5.95 5.95 5.95 5.95 5.95	
59	A B C D E F	2.28	0.90 1.69 3.73 30.74 0.00 0.00	2.62 3.16 4.93 31.74 0.00 0.00	2.91 2.41 2.23 2.16 2.28 2.28	72	Х В С D E F	5.84	12.21 0.00 0.00 0.00 0.00 0.00	16.69 0.00 0.00 0.00 0.00 0.00	4.70 5.84 5.84 5.84 5.84 5.84	
60	A ВСD E F	2.30	1.14 2.16 4.66 17.07 0.00 0.00	2.75 3.51 5.78 18.02 0.00 0.00	3.05 2.47 2.27 2.20 2.30 2.30	73	A B C D E F	4.78	8.98 0.00 0.00 0.00 0.00 0.00	12.41 0.00 0.00 0.00 0.00 0.00	4.12 4.78 4.78 4.78 4.78 4.78 4.78	
61	A B C D E F	2.61	0.81 1.28 2.89 15.58 0.00 0.00	2.96 3.32 4.68 17.12 0.00 0.00	2.98 2.56 2.38 2.30 2.61 2.61							
62	A B C D E F	2.57	0.85 1.47 3.66 25.00 0.00 0.00	2.94 3.41 5.34 26.55 0.00 0.00	2.98 2.52 2.34 2.27 2.57 2.57							
63	Х В С D 2 F	2.23	1.11 2.07 4.03 48.19 0.00 0.00	2.64 3.33 5.06 49.04 0.00 0.00	2.98 2.43 2.24 2.15 2.23 2.23							
64	A B C D E F	2.46	0.95 1.77 3.27 20.34 0.00 0.00	2.86 3.48 4.81 21.66 0.00 0.00	2.96 2.47 2.31 2.23 2.46 2.46							
65	<b>λ</b> в с р г	2.42	1.09 2.09 6.65 76.13 0.00 0.00	2.87 3.64 5.99 77.67 0.00 0.00	3.00 2.47 2.29 2.21 2.42 2.42							

						( ام الم م م )
TABLE C.1	Experimental uncertaint	y estimates II	n the	horizontal	data set	(conta.)

Run No.	Visual section	G %	x %	V <sub>32</sub> %	V.,	Run No.	Visual section	G N	x ħ	V.,,	V <sub>12</sub> %	
1	А В С Д 2 7	3.52	1.61 4.42 33.16 0.00 0.00 0.00	4.56 7.15 36.05 0.00 0.00 0.00	3.23 2.88 2.74 3.52 3.52 3.52	14	<b>Х</b> вс D M F	3.52	1.45 3.89 28.94 0.00 0.00 0.00	4.43 6.62 31.68 0.00 0.00 0.00	3.31 2.93 2.78 3.52 3.52 3.52 3.52	
2	a B C D E F	3.52	1.63 6.32 113.55 0.00 0.00 0.00	4.54 6.99 117.46 0.00 0.00 0.00	3.31 2.96 2.81 3.52 3.52 3.52	15	A B C D N F	3.35	2.79 8.07 0.00 0.00 0.00 0.00	5.20 10.30 0.00 0.00 0.00 0.00	3.36 2.91 3.35 3.35 3.35 3.35 3.35	
з	a C D F	3.60	1.64 5.00 0.00 0.00 0.00 0.00	4.66 7.77 0.00 0.00 0.00 0.00	3.29 2.93 2.60 3.60 3.60 3.60	16	A B C D Z F	3.58	2.39 6.30 0.00 0.00 0.00 0.00	5.20 8.94 0.00 0.00 0.00 0.00	3.37 2.95 3.58 3.58 3.58 3.58 3.58	
4	Х В С Д Д Г	3.66	2.19 7.34 0.00 0.00 0.00 0.00	5.14 10.03 0.00 0.00 0.00 0.00	3.37 2.99 3.66 3.66 3.66 3.66	17	A B C D E F	3.00	1.09 2.50 7.61 0.00 0.00 0.00	3.56 4.68 9.43 0.00 0.00 0.00	3.27 2.89 2.74 3.00 3.00 3.00	
5	A B C D E F	3.60	2.29 8.37 0.00 0.00 0.00 0.00	5.12 10.94 0.00 0.00 0.00 0.00	3.36 2.98 3.60 3.60 3.60 3.60	18	A B C D E F	3.06	1.48 3.42 15.09 0.00 0.00 0.00	3.89 5.56 16.95 0.00 0.00 0.00	3.25 2.85 2.70 3.06 3.06 3.06	
6	A B C D E F	3.73	3.28 20.36 0.00 0.00 0.00 0.00	6.10 23.13 0.00 0.00 0.00 0.00	3.40 2.98 3.73 3.73 3.73 3.73 3.73	19	A B C D E F	2.97	1.78 4.54 22.78 0.00 0.00 0.00	3.97 6.42 24.48 0.00 0.00 0.00	3.26 2.84 2.69 2.97 2.97 2.97	
7	А В С D 2 2 8	4.56	2.80 14.35 0.00 0.00 0.00 0.00	6,69 18.09 0.00 0.00 0.00 0.00	3.69 3.36 4.56 4.56 4.56 4.56	20	A B C D E F	3.02	1.93 4.80 25.91 0.00 0.00 0.00	4.14 6.74 27.72 0.00 0.00 0.00	3.27 2.84 2.69 3.02 3.02 3.02	
8	A B C D E F	4.26	3.72 20.73 0.00 0.00 0.00 0.00	7.08 24.08 0.00 0.00 0.00 0.00	3.69 3.27 4.26 4.26 4.26 4.26 4.26	21	Х В С D Z Z Z	2.75	1.70 4.72 1459.11 0.00 0.00 0.00	3.67 6.39 1478.43 0.00 0.00 0.00	3.07 2.61 2.30 2.75 2.75 2.75	
9	A B C D E F	5.02	4.30 155.50 0.00 0.00 0.00 0.00	8.49 163.15 0.00 0.00 0.00 0.00	3.96 3.60 5.02 5.02 5.02 5.02	22	A B C D E F	2.74	1.50 3.71 17.82 0.00 0.00 0.00	3.53 5.46 19.39 0.00 0.00 0.00	3.04 2.60 2.45 2.74 2.74 2.74	
10	A B C D E F	5.13	3.82 64.51 0.00 0.00 0.00 0.00	8.19 69.96 0.00 0.00 0.00 0.00	3.99 3.66 5.13 5.13 5.13 5.13	23	Х В С D E F	2.68	1.49 3.70 22.59 0.00 0.00 0.00	3.44 5.36 24.07 0.00 0.00 0.00	3.08 2.60 2.43 2.68 2.68 2.68	
11	A B C D E F	4.97	6.10 0.00 0.00 0.00 0.00 0.00	10.07 0.00 0.00 0.00 0.00 0.00	3.98 4.73 4.97 4.97 4.97 4.97	24	A B C D E F	2.76	1.27 2.67 8.19 0.00 0.00 0.00	3.41 4.59 9.87 0.00 0.00 0.00	3.04 2.61 2.45 2.76 2.76 2.76	
12	A B C D E F	4.97	14.54 0.00 0.00 0.00 0.00 0.00	18.12 0.00 0.00 0.00 0.00 0.00	4.16 4.97 4.97 4.97 4.97 4.97	25	Х В С D 2 7	2.84	2.09 4.98 29.25 0.00 0.00 0.00	4.05 6.70 30.91 0.00 0.00 0.00	3.17 2.71 2.54 2.84 2.84 2.84	
13	А В С D 2 7	3.54	1.64 4.49 106.49 0.00 0.00 0.00 0.00	4.60 7.22 110.56 0.00 0.00 0.00	3.30 2.90 2.75 3.54 3.54 3.54	26	х В С D 2 Г	2.80	1.60 3.93 17.73 0.00 0.00 0.00	3.65 5.70 19.30 0.00 0.00 0.00	3.13 2.67 2.52 2.80 2.80 2.80 2.80	

TABLE C.2 Experimental uncertainty estimates in the -1° [ downward ] data set

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Run No.	Visual section	G %	I X	V <sub>79</sub> %	V <sub>1.2</sub> 35	Run No.	Visual section	G %	I S	V <sub>38</sub> %	V.,2
27	A B C D E F	2.81	0.85 2.02 5.26 0.00 0.00 0.00	3.20 4.05 6.94 0.00 0.00 0.00	3.20 2.81 2.66 2.81 2.81 2.81	40	A B C D E F	2.75	1.93 4.84 60.26 0.00 0.00	3.81 6.48 62.09 0.00 0.00	3.19 2.64 2.45 2.75 2.75 2.75
28	A B C D E F	2.76	1.88 3.46 8.86 0.00 0.00 0.00	3.78 5.15 10.33 0.00 0.00 0.00	3.24 2.81 2.64 2.76 2.76 2.76	41	A B C D E F	2.73	2.00 4.14 13.07 0.00 0.00 0.00	3.82 5.78 14.56 0.00 0.00 0.00	3.22 2.67 2.49 2.73 2.73 2.73
29	Х В С D Z F	2.85	1.39 2.90 8.14 0.00 0.00 0.00	3.58 4.86 9.86 0.00 0.00 0.00	3.17 2.72 2.56 2.85 2.85 2.85	42	<b>Х</b> В С D 2 7	2.73	1.27 2.62 7.06 0.00 0.00 0.00	3.37 4.51 8.75 0.00 0.00 0.00	3.05 2.58 2.42 2.73 2.73 2.73
30	<b>Х</b> В С D 2 2 2	2.98	1.97 4.92 271.54 0.00 0.00 0.00	4.11 6.82 275.71 0.00 0.00. 0.00	3.27 2.77 2.59 2.98 2.98 2.98	43	λ С D 22 7	2.73	2.23 5.70 104.45 0.00 0.00 0.00	4.02 7.27 106.63 0.00 0.00 0.00	3.13 2.59 2.42 2.73 2.73 2.73
31	Х В С D E F	2.85	0.93 2.03 7.03 0.00 0.00 0.00	3.31 4.18 8.84 0.00 0.00 0.00	3.11 2.68 2.51 2.85 2.85 2.85	44	A B C D E F	2.56	1.61 3.47 13.63 0.00 0.00 0.00	3.35 4.98 14.94 0.00 0.00 0.00	3.10 2.54 2.36 2.56 2.56 2.56
32	λ B C D E F	2.80	2.14 5.08 33.55 0.00 0.00 0.00	4.02 6.75 35.24 0.00 0.00 0.00	3.22 2.67 2.49 2.80 2.80 2.80	45	A B C D Z F	2.42	1.17 2.26 4.33 22.01 0.00 0.00	2.91 3.77 5.66 23.18 0.00 0.00	2.98 2.46 2.31 2.24 2.42 2.42
33	λ B C D E F	2.85	2.10 5.18 44.54 0.00 0.00 0.00	4.04 6.87 46.26 0.00 0.00 0.00	3.30 2.75 2.58 2.85 2.85 2.85	46	A B C D S F	2.46	1.06 2.11 5.45 248.29 0.00 0.00	2.92 3.73 6.82 251.09 0.00 0.00	2.96 2.47 2.30 2.24 2.46 2.46 2.46
34	A B C D Z F	2.88	2.23 5.42 89.21 0.00 0.00 0.00	4.17 7.12 91.31 0.00 0.00 0.00	3.34 2.78 2.59 2.88 2.88 2.88	47	A B C D E F	2.44	1.31 3.11 12.77 0.00 0.00 0.00	3.02 4.51 13.91 0.00 0.00 0.00	3.03 2.48 2.30 2.44 2.44 2.44
35	A B C D E F	3.05	2.07 4.50 26.50 0.00 0.00	4.28 6.54 28.51 0.00 0.00 0.00	3.28 2.79 2.61 3.05 3.05 3.05	48	入 B C D E F	2.43	1.21 2.37 7.40 0.00 0.00 0.00	2.95 3.87 8.61 0.00 0.00 0.00	3.00 2.48 2.30 2.43 2.43 2.43
36	A B C D E F	2.54	1.88 5.50 0.00 0.00 0.00 0.00	3.51 5.78 0.00 0.00 0.00 0.00	3.19 2.59 2.54 2.54 2.54 2.54 2.54	49	A B C D स F	2.33	1.09 2.14 5.47 0.00 0.00 0.00	2.77 3.56 6.61 0.00 0.00 0.00	2.97 2.44 2.26 2.33 2.33 2.33
37	A B C D E F	2.50	1.71 3.99 14.23 0.00 0.00 0.00	3.34 5.36 15.45 0.00 0.00 0.00	3.10 2.51 2.34 2.50 2.50 2.50	50	A B C D R P	2.33	1.39 3.00 13.49 0.00 0.00 0.00	2.93 4.25 14.45 0.00 0.00 0.00	3.03 2.45 2.26 2.33 2.33 2.33
38	A B C D E F	2.45	1.76 4.15 18.11 0.00 0.00 0.00	3.30 5.40 19.17 0.00 0.00 0.00	3.15 2.54 2.35 2.45 2.45 2.45 2.45	51	A B C D Z F	2.33	0.95 1.74 3.71 16.95 0.00 0.00	2.70 3.27 5.01 18.03 0.00 0.00	2.89 2.41 2.25 2.18 2.33 2.33
39	λ B C D Z F	2.47	1.96 4.95 117.71 0.00 0.00 0.00	3.46 6.16 119.20 0.00 0.00 0.00	3.23 2.57 2.36 2.47 2.47 2.47	52	A ас рив	2.35	0.95 1.81 4.16 72.39 0.00 0.00	2.72 3.35 5.45 73.75 0.00 0.00	2.90 2.41 2.25 2.18 2.35 2.35

# TABLE C.2 Experimental uncertainty estimates in the -1° [ downward ] data set (cont'd.)

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Run No.	Visual section	G %	x %	V.72 %	V.,
53	λ	2.28	0.94	2.64	2.83
	в		1.69	3.17	2.37
	n n		2.83	4.14	2.24
	2		9.34	10.38	2.16
	Ŧ		0.00	0.00	2.28
54	λ	2.30	0.88	2.63	2.83
	8		1.67	3.18	2.38
	n n		3.44	6./1	2.23
	2		20.40	21.49	2.10
	F		0.00	0.00	2.30
55	λ	2.30	1.32	2.86	2.93
	8		2.52	3.82	2.41
	C D		5.42	6.51	2.25
	2		00.77	09.91	2.18
	F		0.00	0.00	2.30
56	λ	2.27	1.28	2.78	2.97
	в		2.64	3.85	2.42
	C D		8.58	9.48	2.23
	2		0.00	0.00	2.27
	F		0.00	0.00	2.27
57	λ	2.16	0.80	2.42	2.79
	8		1.41	2.79	2.34
	2		2.54	3.67	2.19
	2		0.00	14.04	2.12
	F		0.00	0.00	2.16
58	λ	2.16	1.02	2.51	2.89
	8		1.88	3.09	2.37
	n		50.26	4.9/	2.20
	2		0.00	0 00	2.15
	F		0.00	0.00	2.16
59	λ	2.17	0.77	2.42	2.77
	B C		1.34	2.76	2.34
	5		2.10	3.39	2.20
	E		0.00	0.00	2.17
	F		0.00	0.00	2.17
60	λ	2.75	1.42	3.49	3.09
	ĉ		10 09	5.04	2.60
	Ď		0.00	0.00	2 75
	E		0.00	0.00	2.75
	F		0.00	0.00	2.75
61	λ	2.70	1.84	3.70	3.12
	ĉ		4.88	6.48	2.57
	D D		13.37	17.49	2.43
	E		0.00	0.00	2.70
	F		0.00	0.00	2.70
62	λ	2.68	1.87	3.68	3.15
	B C		4.29	5.90	2.58
	D D		30.39	38.62	2.38
	E		0.00	0.00	2.00
	F		0.00	0.00	2.68
63	λ	2.80	2.24	4.11	3.15
	å C		5.16	6.83	2.65
	Ď		0.00	0.00	2.40
	E		0.00	0.00	2.80
	F		0.00	0.00	2.80

TABLE C.2 Experimental uncertainty estimates in the -1° [ downward ] data set (cont'd.)

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Run No.	Visual section	G %	х %	V <sub>39</sub>	V <sub>L9</sub> %	Run No.	Visual section	G %, •	x ¥	V <sub>28</sub> %	V.,,
1	λ	3.06	1.07	3.62	3.20	14	λ	2.17	0.96	2.49	2.96
	в		2.34	4.65	2.81		в		1.56	2.87	2.41
	с		7.23	9.23	2.66		c		2.56	3.67	2.23
	D		0.00	0.00	3.06		D		6.68	7.51	2.14
	E		0.00	0.00	3.06		E		0.00	0.00	2.17
	F		0.00	0.00	3.06		P		0.00	0.00	2.17
2	λ	2.83	0.99	3.32	3.06	15	A	2.20	1.19	2.65	3.02
	5		4.04	6.16	4.00		8		2.12	3.34	2.40
	ç		5.45	7.29	2.51		C .		4.47	5.40	2.20
	5		0.00	0.00	2.83		D		432.36	434.50	2.13
	e F		0.00	0.00	2.83		e F		0.00	0.00	2.20
3	λ	2.81	1.30	3.49	3.07	16	λ	2.20	1.16	2.63	3.04
	в		2.58	4.57	2.64		в		2.15	3.34	2.46
	c		7.49	9.25	2.48		c		4.73	5.64	2.26
	Ď		0.00	0.00	2.81		n		0.00	0.00	2.20
	R		0.00	0.00	2.81		R		0.00	0.00	2.20
	F		0.00	0.00	2.81		P		0.00	0.00	2.20
4	λ	2.68	1.86	3.69	3.06	17	λ	2.13	1.06	2.50	2.97
	в		3.90	5.54	2.59		в		1.94	3.08	2.44
	с		16.73	18.22	2.41		C		4.03	4.87	2.23
	D		0.00	0.00	2.68		D		83.48	84.10	2.14
	E		0.00	0.00	2.68		E		0.00	0.00	2.13
	F		0.00	0.00	2.68		7		0.00	0.00	2.13
5	λ	2.85	0.89	3.30	3.05	18	λ	2.16	1.03	2.51	2.93
	в		1.57	3.86	2.61		в		1.87	3.07	2.42
	C		3.10	5.24	2.44		C		3.51	4.46	2.23
	D		592.98	603.47	2.31		D		39.85	40.48	2.14
	E		0.00	0.00	2.85		E		0.00	0.00	2.16
	F		0.00	0.00	2.85		<b>P</b>		0.00	0.00	2.16
5	λ	2.45	1.37	3.08	3.02	19	λ	2.56	1.11	3.06	3.06
•	8		2.32	3.88	2.48		n 1		2.16	3.90	2.54
	ā		4.07	5.50	2.31		č		5.10	6.62	2.35
	n		25.59	26.92	2.22		ñ		0.00	0.00	2 56
	7		0.00	0.00	2 45		7		0 00	0.00	2 56
	F		0.00	0.00	2.45		2		0.00	0.00	2.56
-		a (5		2 40			-	• •			
/	A	2.45	1.38	3.08	3.03	20	A 7	2.61	1.13	3.14	3.01
	5		2.10	3.47	2.00		5		1.35	3.01	2.34
	C P		0.11	1.41	2.30		ç		3.8/	5.55	2.3/
	D		0.00	0.00	4.45		D		64.96	66.87	2.28
	F		0.00	0.00	2.45		E F		0.00	0.00	2.61
		2 64	1 77	3 57	3 15			2 80			3 00
	- A-		1 00	5.57	2.45		<u>^</u>	4.00	1.15	3.30	2.63
	-		4.03	5.01	2.30		5		1.05	3.35	2.03
	2		14.94	10.41	2.3/		2		3.84	5.81	2.44
	D		0.00	0.00	2.04		D		38.74	40.81	2.35
	E		0.00	0.00	2.64		E		0.00	0.00	2.80
	5.		0.00	0.00	2.64		F		0.00	0.00	2.80
9	λ	2.61	1.44	3.32	3.04	22	λ	2.92	1.51	3.76	3.15
	8		4.51	6.20	2.34		в		3.09	5.14	2.72
	ç		4.20	5.85	2.39		с		9.37	11.20	2.56
	D		262.62	266.42	2.27		ם		0.00	0.00	2.92
	2		0.00	0.00	2.61		E		0.00	0.00	2.92
	5.		0.00	0.00	2.01		r		0.00	0.00	2.92
10	λ	2.39	1.15	2.87	2.98	23	λ	2.90	1.42	3.65	3.18
	в		2.25	3.74	2.45		в		2.86	4.87	2.76
	c		4.08	5.41	2.29		c		82.16	84.29	2.57
	D		21.38	22.54	2.21		D		0.00	0.00	2.90
	E		0.00	0.00	2.39		E		0.00	0.00	2.90
	F		0.00	0.00	2.39		P		0.00	0.00	2.90
11	λ	2.36	1.08	2.79	3.00	24	λ	2.72	1.37	3.41	3.10
	в		2.06	3.54	2.45		в		2.99	4.76	2.66
	C		4.32	5.58	2.27		C		7.34	8.88	2.52
	p		63.74	65.04	2.19		D		0.00	0.00	2.72
	E		0.00	0.00	2.36		z		0.00	0.00	2.72
	2		0.00	0.00	2.36		P		0.00	0.00	2.72
12	λ	2.28	0.96	2,64	2.88	25	λ	2.73	1.06	3.24	3.07
	 В	2.20	1 69	3,16	2.39				2.40	4.29	2.66
	č		2.05	1 1 9	2 24		č		5 4 9	7 14	2.51
	n		4.JU 8 54	9 57	2 17		5		0 00	0 00	2.73
	5		0.34	0.00			5		0.00	0.00	2 73
	F		0.00	0.00	2.28		F		0.00	0.00	2.73
1 2	3	2 20	1 17	2 74	3.00	24	3	7 54	1 15	3 05	3.16
<b>1</b> - 1	a	4.40	2.24	4./4	2.44	40	3	A • 29	2.46	4,08	2.59
	č		4.90	5,97	2.25		č		6.30	7.68	2.40
	n		0 00	0.00	2.28		ñ		0 00	0.00	2.54
	5		0.00	0.00	2 28		2		0.00	0.00	2.54
	2 7		0.00	0.00	2 78		3		0.00	0.00	2.54
	5		0.00	0.00	4 • 4 0		2		0.00	0.00	* •

# TABLE C.3 Experimental uncertainty estimates in the -5° [ downward ] data set

					(-		, 				
Run No.	Visual section	G %	x %	V <sub>58</sub> %	V <sub>C2</sub>	Rur No.	visual section	G %	I %	V <sub>59</sub> %	V.2
27	λ B C D E F	2.51	1.44 3.17 8.41 0.00 0.00 0.00	3.18 4.63 9.67 0.00 0.00 0.00	3.18 2.58 2.39 2.51 2.51 2.51	40	A B C D E F	3.43	3.17 8.42 0.00 0.00 0.00 0.00	5.60 10.64 0.00 0.00 0.00 0.00	3.47 3.08 3.43 3.43 3.43 3.43
28	A B C D E F	2.38	1.57 3.20 9.50 0.00 0.00 0.00	3.09 4.46 10.52 0.00 0.00 0.00	3.09 2.53 2.33 2.38 2.38 2.38 2.38	41	A B C D E F	4.26	2.66 9.25 0.00 0.00 0.00 0.00	6.13 12.38 0.00 0.00 0.00 0.00	3.82 3.50 4.26 4.26 4.26 4.26 4.26
29	A B C D E F	2.39	0.72 1.28 2.46 10.63 0.00 0.00	2.67 3.05 4.03 11.88 0.00 0.00	2.81 2.40 2.25 2.18 2.39 2.39	42	A B C D E F	3.69	1.89 5.26 0.00 0.00 0.00 0.00	4.91 7.99 0.00 0.00 0.00 0.00	3.46 3.12 2.81 3.69 3.69 3.69
30	A B C D E F	2.34	0.95 1.78 3.88 187.61 0.00 0.00	2.72 3.31 5.16 189.58 0.00 0.00	2.92 2.43 2.26 2.18 2.34 2.34	43	A B C D Z F	3.66	1.69 10.77 0.00 0.00 0.00 0.00	4.74 13.29 0.00 0.00 0.00 0.00	3.44 3.10 3.66 3.66 3.66 3.66 3.66
31	A B C D E F	2.38	0.85 1.55 2.98 13.80 0.00 0.00	2.72 3.22 4.44 15.00 0.00 0.00	2.86 2.41 2.26 2.19 2.38 2.38						
32	A B C D Z F	2.73	1.27 2.94 9.41 0.00 0.00 0.00	3.38 4.80 11.07 0.00 0.00 0.00	3.03 2.56 2.40 2.73 2.73 2.73 2.73						
33	A B C D E F	2.73	1.44 3.43 15.24 0.00 0.00 0.00	3.48 5.22 16.85 0.00 0.00 0.00	3.05 2.57 2.40 2.73 2.73 2.73 2.73						
34	A B C D Z F	2.70	1.54 3.98 43.17 0.00 0.00 0.00	3.51 5.67 44.87 0.00 0.00 0.00	3.06 2.57 2.39 2.70 2.70 2.70						
35	λ B C D E F	3.73	3.11 9.00 0.00 0.00 0.00 0.00	5.94 11.68 0.00 0.00 0.00 0.00	3.46 3.07 3.73 3.73 3.73 3.73 3.73						
36	Х В С D E F	3.26	6.47 24.21 0.00 0.00 0.00 0.00	8.32 26.13 0.00 0.00 0.00 0.00	3.45 2.97 3.26 3.26 3.26 3.26 3.26						
37	Х В С D E F	3.83	2.15 7.30 152.45 0.00 0.00 0.00	5.19 9.92 156.49 0.00 0.00 0.00	3.77 3.39 3.27 3.83 3.83 3.83						
38	A B C D Z F	4.44	5.20 82.47 0.00 0.00 0.00 0.00	8.37 86.24 0.00 0.00 0.00 0.00	4.21 3.77 4.44 4.64 4.64 4.64						
39	х вс р г	3.52	3.43 9.65 0.00 0.00 0.00 0.00	5.93 11.95 0.00 0.00 0.00 0.00	3.50 3.12 3.52 3.52 3.52 3.52 3.52						

TABLE C.3 Experimental uncertainty estimates in the -5°[ downward ] data set (cont'd.)

Run No.	Visual section	G S	X N	V %	V <u></u> %	Run No.	Visual section	G %	x %	V.12 %	V
1	A B C D E F	2.83	1.26 2.63 5.67 0.00 0.00 0.00	3.49 4.65 7.51 0.00 0.00 0.00	3.02 2.62 2.50 2.83 2.83 2.83	14	A B C D E F	2.74	1.36 2.69 10.61 0.00 0.00 0.00	3.47 4.61 12.30 0.00 0.00 0.00	2.91 2.54 2.40 2.74 2.74 2.74
2	A B C D E F	2.80	0.69 1.43 3.10 0.00 0.00 0.00	3.13 3.67 5.09 0.00 0.00 0.00	3.01 2.64 2.51 2.80 2.80 2.80	15	<b>Х</b> В С Д Е Г	2.70	3.39 7.56 0.00 0.00 0.00 0.00	4.91 8.95 0.00 0.00 0.00 0.00	3.06 2.64 2.70 2.70 2.70 2.70
3	A B C D E F	2.80	1.74 6.17 0.00 0.00 0.00 0.00	3.76 7.83 0.00 0.00 0.00 0.00	3.08 2.60 2.60 2.80 2.80 2.80	16	a B D Z F	3.14	2.17 6.78 0.00 0.00 0.00 0.00	4.49 8.87 0.00 0.00 0.00 0.00	3.20 2.74 3.14 3.16 3.14 3.14
4	A B C D Z F	2.80	1.74 4.99 44.32 0.00 0.00	3.77 6.72 46.14 0.00 0.00 0.00	3.06 2.60 2.46 2.80 2.80 2.80 2.80	17	<b>λ</b> В С Д 2 Г	3.05	1.54 3.81 18.89 0.00 0.00 0.00	3.94 5.98 20.93 0.00 0.00 0.00	3.14 2.72 2.57 3.05 3.05 3.05
5	A B C D E F	2.37	0.97 1.92 3.58 0.00 0.00 0.00	2.75 3.45 4.90 0.00 0.00 0.00	2.87 2.42 2.29 2.37 2.37 2.37	18	A B C D E F	3.05	1.20 2.94 11.45 0.00 0.00 0.00	3.71 5.19 13.45 0.00 0.00 0.00	3.14 2.74 2.60 3.05 3.05 3.05
6	A B C D V F	2.39	0.99 1.85 3.39 0.00 0.00 0.00	2.79 3.43 4.77 0.00 0.00 0.00	2.86 2.43 2.30 2.39 2.39 2.39	19	A B C D Z F	3.05	1.53 3.27 10.25 0.00 0.00 0.00	3.93 5.46 12.25 0.00 0.00 0.00	3.16 2.75 2.61 3.05 3.05 3.05
7	A B C D E F	2.21	0.97 1.67 3.07 65.06 0.00 0.00	2.56 3.04 4.21 65.96 0.00 0.00	2.79 2.36 2.22 2.14 2.21 2.21	20	A B C D R F	2.75	1.62 4.00 18.07 0.00 0.00 0.00	3.62 5.74 19.67 0.00 0.00 0.00	3.06 2.59 2.44 2.75 2.75 2.75
8	А В С Д Е F	2.19	1.00 1.83 3.08 10.86 0.00 0.00	2.55 3.12 4.18 11.66 0.00 0.00	2.83 2.35 2.22 2.14 2.19 2.19	21	λ B C D E F	2.80	1.73 4.43 29.69 0.00 0.00 0.00	3.75 6.18 31.38 0.00 0.00 0.00	3.10 2.62 2.47 2.30 2.80 2.80
9	A B C D E F	2.37	1.42 2.47 5.51 0.00 0.00 0.00	3.00 3.87 6.69 0.00 0.00 0.00	2.96 2.47 2.29 2.37 2.37 2.37	22	A B C D E F	2.85	1.53 3.16 8.21 0.00 0.00 0.00	3.69 5.11 9.97 0.00 0.00 0.00	3.11 2.68 2.53 2.85 2.85 2.85 2.85
10	A B C D Z F	2.30	0.74 1.21 2.05 5.79 0.00 0.00	2.58 2.89 3.55 6.99 0.00 0.00	2.76 2.37 2.23 2.17 2.30 2.30	23	A B C D R F	2.85	1.00 2.19 5.20 0.00 0.00 0.00	3.37 4.32 7.11 0.00 0.00 0.00	3.02 2.63 2.50 2.85 2.85 2.85 2.85
11	A B C D E F	3.00	1.01 2.34 11.83 0.00 0.00 0.00	3.56 4.66 13.84 0.00 0.00 0.00	3.02 2.66 2.52 3.00 3.00 3.00	24	A B C D E F	3.14	2.81 10.25 0.00 0.00 0.00 0.00	4.98 12.11 0.00 0.00 0.00 0.00	3.26 2.39 3.14 3.14 3.14 3.14
12	A B C D E F	3.37	1.46 4.03 0.00 0.00 0.00 0.00	4.28 6.59 0.00 0.00 0.00 0.00	3.16 2.82 2.70 3.37 3.37 3.37	25	A B C D Z F	5.19	5.69 0.00 0.00 0.00 0.00 0.00	9.65 0.00 0.00 0.00 0.00 0.00	4.55 5.19 5.19 5.19 5.19 5.19 5.19
13	A B C D Z F	3.14	2.28 6.42 0.00 0.00 0.00 0.00	4.60 8.53 0.00 0.00 0.00 0.00	3.11 2.73 3.14 3.16 3.16 3.14	26	А В С Д 2 7	4.30	3.24 17.85 0.00 0.00 0.00 0.00	6.60 20.79 0.00 0.00 0.00 0.00	3.96 3.67 4.30 4.30 4.30

TABLE C.4 Experimental uncertainty estimates in the -10° [ downward ] data set

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						<u></u>						
Run No.	Visual section	G %	X X	V <sub>as</sub> \$	V. <u>.</u> %		Run No.	Visual section	G %	x z	V <sub>ca</sub> %	V_10 %
27	A B C	3.54	1.88 6.19 0.00	4.72 8.60 0.00	3.48 3.16 3.54		40	х В С	2.45	1.64 4.48 0.00	3.24 5.74 0.00	3.01 2.47 2.45
	E P		0.00 0.00 0.00	0.00	3.54 3.54 3.54			D E F		0.00 0.00 0.00	0.00 0.00 0.00	2.45 2.45 2.45
28	A B C D E	2.43	0.80 1.63 2.95 18.58 0.00	2.75 3.33 4.47 19.82 0.00	2.87 2.42 2.29 2.22 2.43		41	A B C D E	2.40	1.08 2.10 4.60 162.21	2.86 3.65 5.93 164.23	2.89 2.43 2.28 2.21 2.40
29	P A B C	2.45	0.00 1.04 2.14 5.05	0.00 2.90 3.75 6.44	2.43 2.90 2.43 2.28		42	F A B	2.37	0.00	0.00 2.76 3.31	2.86 2.40
30	D E F	2 (0	0.00	0.00 0.00 0.00	2.45 2.45 2.65			C D F		3.53 34.91 0.00 0.00	4.91 36.13 0.00 0.00	2.25 2.18 2.37 2.37
30	В С D E F	<b>2.4</b> U	2.54 6.67 0.00 0.00 0.00	2.99 3.98 7.88 0.00 0.00 0.00	2.93 2.45 2.28 2.40 2.40 2.40		43	λ Β Ο Ξ	2.30	0.98 1.73 3.62 121.10 0.00	2.68 3.23 4.88 122.63 0.00	2.84 2.38 2.23 2.15 2.30
31	λ В С D 2 2 2 2 2 2 2	2.36	1.21 2.38 5.25 703.12 0.00 0.00	2.87 3.79 6.44 709.40 0.00 0.00	2.92 2.42 2.26 2.15 2.36 2.36		44	A B C D E F	2.29	0.91 1.76 4.18 0.00 0.00	2.63 3.23 5.37 0.00 0.00	2.30 2.84 2.37 2.21 2.15 2.29
32	A B C D E F	2.30	1.11 2.10 3.71 15.94 0.00 0.00	2.75 3.50 4.94 16.94 0.00 0.00	2.87 2.38 2.25 2.18 2.30 2.30		45	A B C D E	2.73	2.38 6.91 330.76 0.00 0.00	4.13 8.40 334.50 0.00 0.00	3.11 2.62 2.46 2.73 2.73
33	A B C D E F	2.30	1.40 2.90 7.05 0.00 0.00 0.00	2.90 4.13 8.06 0.00 0.00 0.00	2.92 2.40 2.25 2.30 2.30 2.30		46	A B C D B F	2.83	2.03 5.44 51.60 0.00	4.00 7.13 53.40 0.00 0.00	3.09 2.67 2.53 2.83 2.83
34	A B C D Z F	2.27	0.67 1.14 2.04 7.13 0.00 0.00	2.50 2.79 3.48 8.20 0.00 0.00	2.76 2.35 2.22 2.15 2.27 2.27		47	A B C D E F	3.44	5.06 30.21 0.00 0.00 0.00	7.25 32.38 0.00 0.00 0.00	3.45 3.05 3.44 3.44 3.44
35	A B C D E F	2.32	0.99 1.90 4.39 36.06 0.00 0.00	2.71 3.37 5.60 37.15 0.00 0.00	2.84 2.38 2.23 2.17 2.32 2.32	4	48	A B C D E F	3.14	3.65 28.86 0.00 0.00 0.00	5.66 30.63 0.00 0.00 0.00	3.30 2.92 3.14 3.14 3.14
36	A B C D M F	2.30	1.37 3.19 25.16 0.00 0.00 0.00	2.88 4.36 26.05 0.00 0.00 0.00	2.98 2.42 2.23 2.30 2.30 2.30	a	69	A B C D E F	3.85	33.43 0.00 0.00 0.00 0.00 0.00	35.38 0.00 0.00 0.00 0.00 0.00	4.11 3.85 3.85 3.85 3.85 3.85
37	A B C D E F	2.47	1.09 2.31 4.15 0.00 0.00 0.00	2.96 3.94 5.62 0.00 0.00 0.00	2.86 2.43 2.31 2.47 2.47 2.47	5	50	A B C D E	3.62	28.66 0.00 0.00 0.00 0.00	30.38 0.00 0.00 0.00 0.00	3.96 3.62 3.62 3.62 3.62
38	A B C D Z F	2.46	1.16 2.53 7.90 0.00 0.00 0.00	2.98 4.09 9.20 0.00 0.00 0.00	2.90 2.43 2.28 2.46 2.46 2.46			£		U.00	0.00	3.62
39	A B C D Z F	2.45	1.03 2.24 4.81 0.00 0.00 0.00	2.90 3.84 6.21 0.00 0.00 0.00	2.86 2.42 2.29 2.45 2.45 2.45 2.45							

TABLE C.4 Experimental uncertainty estimates in the -10°[ downward ] data set (cont'd.)

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Run No.	Visual section	G %	x %	V <sub>22</sub> %	V %	Run No.	Visual section	G %	I %	V <sub>59</sub> %	Va %
1	A B C D E F	2.40	1.08 2.00 4.81 186.40 0.00 0.00	2.87 3.57 6.13 188.57 0.00 0.00	2.86 2.43 2.28 2.21 2.40 2.40	14	A B C D E F	3.05	2.07 5.87 33.98 0.00 0.00 0.00	4.32 7.88 36.08 0.00 0.00 0.00	3-14 2-71 2-59 3-05 3-05 3-05
2	<b>Х</b> В С D 2 5	2.39	0.88 1.72 3.40 16.95 0.00 0.00	2.74 3.34 4.81 18.11 0.00 0.00	2.85 2.41 2.27 2.21 2.39 2.39	15	A B C D E F	2.98	1.91 4.88 31.45 0.00 0.00 0.00	4.11 6.85 33.44 0.00 0.00 0.00	3.13 2.69 2.55 2.98 2.98 2.98
3	A B C D E F	2.40	0.75 1.37 2.66 10.63 0.00 0.00	2.70 3.13 4.20 11.86 0.00 0.00	2.82 2.41 2.27 2.21 2.40 2.40	16	A B C D Z F	2.91	1.78 4.29 37.61 0.00 0.00 0.00	3.93 6.21 39.54 0.00 0.00 0.00	3.13 2.67 2.52 2.91 2.91 2.91
4	Х В С D E F	2.39	0.67 1.06 . 1.72 3.94 0.00 0.00	2.65 2.91 3,42 5.38 0.00 0.00	2.79 2.40 2.27 2.20 2.39 2.39	17	A B C D E F	2.91	2.40 4.85 20.92 0.00 0.00 0.00	4.39 6.69 22.68 0.00 0.00 0.00	3.12 2.72 2.56 2.91 2.91 2.91
5	<b>)</b> В С С Е Г	2.47	0.96 1.88 3.50 21.56 0.00 0.00	2.89 3.58 5.02 22.86 0.00 0.00	2.88 2.45 2.32 2.25 2.47 2.47	18	A B C D E F	2.98	1.88 3.81 11.38 0.00 0.00 0.00	4.10 5.86 13.28 0.00 0.00 0.00	3.10 2.71 2.57 2.98 2.98 2.98
6	A B C D E F	2.45	1.85 4.57 87.00 0.00 0.00 0.00	3.37 5.79 88.31 0.00 0.00 0.00	3.12 2.52 2.34 2.45 2.45 2.45	19	Х В С Р 2	3.24	5.78 51.92 0.00 0.00 0.00 0.00	7.66 63.99 0.00 0.00 0.00 0.00	3.42 3.00 3.24 3.24 3.24 3.24 3.24
7	λ B C D E F	2.40	1.54 4.00 48.82 0.00 0.00 0.00	3.12 5.23 49.94 0.00 0.00 0.00	3.03 2.47 2.29 2.40 2.40 2.40	20	A B C D E F	3.35	5.20 41.46 0.00 0.00 0.00 0.00	7.25 43.52 0.00 0.00 0.00 0.00	3.45 3.05 3.35 3.35 3.35 3.35 3.35
8	A B C D E F	2.39	1.45 3.01 8.58 0.00 0.00 0.00	3.04 4.33 9.67 0.00 0.00 0.00	3.00 2.46 2.30 2.39 2.39 2.39	21	A B C D E F	3.35	3.16 13.03 0.00 0.00 0.00 0.00	5.50 15.07 0.00 0.00 0.00 0.00	3.39 3.02 3.35 3.35 3.35 3.35
9	A B C D E F	2.70	1.74 4.64 19.70 0.00 0.00 0.00	3.64 6.24 21.16 0.00 0.00 0.00	3.07 2.59 2.46 2.70 2.70 2.70	22	A B C D E F	3.35	1.47 5.08 0.00 0.00 0.00 0.00	4.23 7.40 0.00 0.00 0.00 0.00	3.33 2.98 3.35 3.35 3.35 3.35 3.35
10	Х В С D E F	2.80	2.15 6.37 91.20 0.00 0.00 0.00	4.04 7.98 93.25 0.00 0.00 0.00	3.13 2.65 2.51 2.80 2.80 2.80	23	A B C D E F	3.33	3.62 16.01 0.00 0.00 0.00 0.00	5.88 18.03 0.00 0.00 0.00 0.00	3.37 2.98 3.33 3.33 3.33 3.33 3.33
11	A B C D Z F	2.80	2.12 6.36 44.58 0.00 0.00 0.00	4.03 8.00 46.32 0.00 0.00 0.00	3.11 2.62 2.50 2.80 2.80 2.80	24	A B C D E F	3.30	5.52 47.99 0.00 0.00 0.00 0.00	7.51 50.09 0.00 0.00 0.00 0.00	3.39 2.99 3.30 3.30 3.30 3.30 3.30
12	Х В С D E F	2.80	1.58 3.53 11.29 0.00 0.00 0.00	3.65 5.35 12.90 0.00 0.00 0.00	3.09 2.66 2.52 2.80 2.80 2.80	25	λ B C D E F	3.38	2.56 9.64 0.00 0.00 0.00 0.00	5.01 11.66 0.00 0.00 0.00 0.00	3.53 3.17 3.38 3.38 3.38 3.38
13	A B C D Z F	2.80	2.36 6.08 40.10 0.00 0.00 0.00	4.21 7.71 41.78 0.00 0.00 0.00	3.13 2.65 2.51 2.80 2.80 2.80	26	A ВС D R F	2.16	1.26 2.60 6.36 0.00 0.00 0.00	2.65 3.65 7.13 0.00 0.00 0.00	2.88 2.37 2.21 2.16 2.16 2.16

TABLE C.5 Experimental uncertainty estimates in the  $+1^{\circ}$  [ upward ] data set

Run No.	Visual section	G %	r z	V.79 %	V_19 %	Run No.	Visual section	G %	x %	V <sub>72</sub>	V.,p %
27	A B C D E F	2.15	1.20 2.19 4.84 0.00 0.00 0.00	2.60 3.31 5.68 0.00 0.00 0.00	2.86 2.37 2.21 2.15 2.15 2.15 2.15	40	A B C D E F	2.16	1.01 1.82 3.90 263.86 0.00 0.00	2.50 3.06 4.84 265.15 0.00 0.00	2.80 2.33 2.18 2.11 2.16 2.16
28	A B C D Z F	2.15	1.19 2.17 4.58 137.99 0.00 0.00	2.59 3.29 5.42 138.80 0.00 0.00	2.86 2.36 2.20 2.13 2.15 2.15	41	A B C D E F	2.14	0.95 1.65 3.24 54.83 0.00 0.00	2.45 2.90 4.21 55.48 0.00 0.00	2.77 2.32 2.18 2.11 2.14 2.14
29	A B C D E F	2.16	0.96 1.89 4.04 335.21 0.00 0.00	2.49 3.11 4.96 336.70 0.00 0.00	2.80 2.34 2.20 2.12 2.16 2.16	42	a B C D E F	2.39	1.06 2.07 4.91 147.78 0.00 0.00	2.83 3.61 6.22 149.73 0.00 0.00	2.87 2.40 2.25 2.19 2.39 2.39
30	<b>λ</b> В С Д Е Г	2.20	1.19 2.31 3.97 20.40 0.00 0.00	2.66 3.49 4.96 21.16 0.00	2.86 2.36 2.23 2.15 2.20 * 2.20	43	<b>Х</b> ВС D 2 7	2.45	0.98 1.88 4.08 47.54 0.00 0.00	2.87 3.57 5.56 49.04 0.00 0.00	2.86 2.41 2.27 2.20 2.45 2.45
31	X B C D E F	2.21	1.15 2.65 5.24 58.86 0.00 0.00	2.65 3.77 6.15 59.67 0.00 0.00	2.86 2.36 2.23 2.16 2.21 2.21	44	A B C D R F	2.43	0.84 1.59 3.15 11.49 0.00 0.00	2.78 3.32 4.69 12.81 0.00 0.00	2.83 2.40 2.26 2.20 2.43 2.43
32	A B C D E F	2.19	1.07 2.35 6.23 0.00 0.00 0.00	2.58 3.51 7.09 0.00 0.00 0.00	2.85 2.36 2.20 2.09 2.19 2.19	45	A B C D E F	2.47	0.85 1.58 3.16 12.54 0.00 0.00	2.84 3.40 4.78 13.95 0.00 0.00	2.81 2.40 2.27 2.21 2.47 2.47
33	A B C D Z F	2.20	1.13 2.50 5.40 33.78 0.00 0.00	2.62 3.63 6.29 34.52 0.00 0.00	2.87 2.36 2.21 2.15 2.20 2.20	46	A B C D E F	6.44	12.80 0.00 0.00 0.00 0.00 0.00	17.72 0.00 0.00 0.00 0.00 0.00	5.30 6.44 6.44 6.44 6.44 6.44
34	A B C D E F	2.20	1.10 2.44 5.17 108.14 0.00 0.00	2.61 3.59 7.03 109.09 0.00 0.00	2.86 2.36 2.20 2.15 2.20 2.20	47	A B C D Z F	5.19	5.59 0.00 0.00 0.00 0.00 0.00	9.55 0.00 0.00 0.00 0.00 0.00	4.58 5.19 5.19 5.19 5.19 5.19 5.19
35	A B C D E F	2.21	1.16 2.37 5.97 0.00 0.00 0.00	2.66 3.56 6.87 0.00 0.00 0.00	2.88 2.37 2.21 2.19 2.21 2.21	48	A B C D E F	5.08	10.47 0.00 0.00 0.00 0.00 0.00	13.93 0.00 0.00 0.00 0.00 0.00	4.63 5.08 5.08 5.08 5.08 5.08
36	A B C D Z F	2.15	1.03 1.89 3.07 17.06 0.00 0.00	2.51 3.09 4.09 17.71 0.00 0.00	2.78 2.32 2.20 2.12 2.15 2.15	49	A B C D E F	5.24	19.66 0.00 0.00 0.00 0.00 0.00	23.36 0.00 0.00 0.00 0.00 0.00	4.50 5.24 5.24 5.24 5.24 5.24
37	A B C D E F	2.14	0.99 1.76 2.96 15.23 0.00 0.00	2.47 2.98 3.97 15.87 0.00 0.00	2.78 2.32 2.19 2.11 2.14 2.14	50	A ЭС D E F	5.13	36.43 0.00 0.00 0.00 0.00 0.00	39.95 0.00 0.00 0.00 0.00 0.00	4.58 5.13 5.13 5.13 5.13 5.13 5.13
38	A B C D E F	2.15	1.02 1.84 3.56 44.70 0.00 0.00	2.51 3.07 4.53 45.38 0.00 0.00	2.79 2.33 2.19 2.12 2.15 2.15	51	A B C D P F	4.19	12.07 0.00 0.00 0.00 0.00 0.00	14.73 0.00 0.00 0.00 0.00 0.00	3.91 4.19 4.19 4.19 4.19 4.19 4.19
39	A B C D E F	2.15	1.01 1.81 3.87 83.88 0.00 0.00	2.50 3.04 4.81 84.65 0.00 0.00	2.79 2.33 2.18 2.11 2.15 2.15	52	λ B C D E F	4.30	20.62 0.00 0.00 0.00 0.00 0.00	23.16 0.00 0.00 0.00 0.00 0.00	4.14 4.30 4.30 4.30 4.30 4.30

TABLE C.5 Experimental uncertainty estimates in the +1° [ upward ] data set (cont'd.)

Run No.	Visual section	G %	X %	V.18 %	V.2 %	
53	λ	3.98	20.86	23.08	3.96	
	в		0.00	0.00	3.98	
	2		0.00	0.00	3.38	
	2		0.00	0.00	3.90	
	F		0.00	0.00	3.98	
54	λ	3.93	4.21	6.99	3.83	
	в		39.88	42.49	3.49	
	c		0.00	0.00	3.93	
	5		0.00	0.00	3.93	
	2		0.00	0.00	3.73	
	2		0.00	0.00	5.55	
55	λ	3.98	6.33	8.94	3.89	
	в		0.00	0.00	3.01	
	c		0.00	0.00	3.98	
	a		0.00	0.00	3.98	
	z		0.00	0.00	3.98	
	F		0.00	0.00	3.98	
56	λ	2.62	1.85	3.61	3.09	
	в		6.20	7.59	2.55	
	c		149.15	151.23	2.42	
	D		0.00	0.00	2.62	
	E		0.00	0.00	2.62	
	£.		0.00	0.00	4.04	
57	λ	2.80	3.56	5.17	3.20	
	в		17.37	18.82	2.62	
	c		0.00	0.00	2.80	
	D		0.00	0.00	2.80	
	E .		0.00	0.00	2.80	
	F		0.00	0.00	2.80	
58	А	2.75	3.39	4.96	3.16	
	Э		10.50	11.92	2.62	
	C		0.00	0.00	2.75	
	D		0.00	0.00	2.75	
	Z		0.00	0.00	2.75	
	у.		0.00	0.00	2.75	
59	λ	2.80	3.47	5.09	3.19	
	в		12.83	14.31	2.63	
	C		0.00	0.00	2.80	
	D		0.00	0.00	2.80	
	E		0.00	0.00	2.80	
	F		0.00	0.00	2.80	

TABLE C.5 Experimental uncertainty estimates in the +1° [ upward ] data set (cont'd.)

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Run No.	Visual section	G %	I %	¥ گ <sup>18</sup>	V <sub>L2</sub> 3	Run No.	Visual section	G %	r S	V.20 \$	V.2 %
1	A B C D E F	3.98	3.19 18.51 0.00 0.00 0.00 0.00	6.24 21.21 0.00 0.00 0.00 0.00	3.69 3.39 3.98 3.98 3.98 3.98	14	ג ד ד ד	2.45	1.61 4.61 0.00 0.00 0.00 0.00	3.24 5.90 0.00 0.00 0.00 0.00	2.98 2.42 2.45 2.45 2.45 2.45 2.45
2	A В С D L F	3.19	3.30 32.85 0.00 0.00 0.00 0.00	5.45 34.83 0.00 0.00 0.00 0.00	3.25 2.84 3.19 3.19 3.19 3.19 3.19	15	Х В С D L F	2.43	1.87 5.57 372.25 0.00 0.00 0.00	3.38 6.74 375.52 0.00 0.00 0.00	3.03 2.44 2.24 2.43 2.43 2.43
3	A B C D Z F	3.10	4.88 18.30 0.00 0.00 0.00 0.00	6.72 20.00 0.00 0.00 0.00 0.00	3.23 2.89 3.10 3.10 3.10 3.10 3.10	16	λ B C D E F	2.45	2.03 5.15 110.27 0.00 0.00 0.00	3.52 6.37 111.81 0.00 0.00 0.00	3.04 2.47 2.30 2.45 2.45 2.45
4	A B C D Z F	3.90	10.450.000.000.000.000.00	12.85 0.00 0.00 0.00 0.00 0.00	3.72 3.90 3.90 3.90 3.90 3.90 3.90	17	A B C D E F	2.56	2.09 5.44 279.12 0.00 0.00 0.00	3.70 6.81 282.23 0.00 0.00 0.00	3.06 2.50 2.32 2.56 2.56 2.56 2.56
5	A B C D E F	3.14	8.99 0.00 0.00 0.00 0.00 0.00	10.59 0.00 0.00 0.00 0.00 0.00	3.34 2.57 3.14 3.14 3.14 3.14	18	A B C D E F	2.43	1.64 3.80 20.25 0.00 0.00 0.00	3.22 5.10 21.37 0.00 0.00 0.00	3.00 2.45 2.28 2.43 2.43 2.43 2.43
6	A B C D R F	3.23	7.28 260.57 0.00 0.00 0.00 0.00	9.05 264.33 0.00 0.00 0.00 0.00	3.37 2.94 3.23 3.23 3.23 3.23 3.23	19	入 B C D た デ	2.25	1.08 2.24 4.92 0.00 0.00 0.00	2.66 3.52 5.95 0.00 0.00 0.00	2.81 2.35 2.21 2.08 2.25 2.25
7	A B C D E F	2.85	$\begin{array}{r} 2.71 \\ 6.57 \\ 4653.74 \\ 0.00 \\ 0.00 \\ 0.00 \\ 0.00 \end{array}$	4.56 8.21 4712.95 0.00 0.00 0.00	3.13 2.72 2.37 2.85 2.85 2.85	20	A B C D R F	2.27	1.16 2.21 6.91 0.00 0.00 0.00	2.74 3.53 5.98 0.00 0.00 0.00	2.82 2.36 2.22 2.19 2.27 2.27
8	A B C D R F	2.85	2.45 5.73 24.55 0.00 0.00 0.00	4.36 7.43 26.19 0.00 0.00 0.00	3.12 2.70 2.56 2.85 2.85 2.85 2.85	21	Х В С С 2 2 2 7	2.23	0.87 1.55 3.02 12.61 0.00 0.00	2.53 2.99 4.21 13.49 0.00 0.00	2.75 2.33 2.20 2.14 2.23 2.23
9	Х В С D N F	2.83	2.35 5.23 35.88 0.00 0.00 0.00	4.25 5.94 37.57 0.00 0.00 0.00	3.10 2.68 2.53 2.83 2.83 2.83 2.83	22	A B C D E F	2.25	0.89 1.73 3.99 100.63 0.00 0.00	2.57 3.15 5.11 101.79 0.00 0.00	2.78 2.34 2.20 2.14 2.25 2.25
10	A B C D E F	2.83	2.34 6.46 64.68 0.00 0.00 0.00	4.24 8.12 66.60 0.00 0.00 0.00	3.09 2.65 2.52 2.83 2.83 2.83 2.83	23	A B C D Z F	2.24	1.53 3.68 40.38 0.00 0.00 0.00	2.89 4.68 41.10 0.00 0.00 0.00	2.98 2.41 2.23 2.24 2.24 2.24
11	A B C D E F	2.91	2.05 7.54 57.37 0.00 0.00 0.00	4.11 9.25 59.32 0.00 0.00 0.00	3.17 2.69 2.58 2.91 2.91 2.91 2.91	24	A B C D E F	2.26	1.56 3.79 23.87 0.00 0.00 0.00	2.91 4.78 24.58 0.00 0.00 0.00	2.99 2.41 2.23 2.24 2.24 2.24
12	A B C D Z F	2.85	3.59 10.78 0.00 0.00 0.00 0.00	5.28 12.31 0.00 0.00 0.00 0.00	3.16 2.71 2.85 2.85 2.85 2.85 2.85	25	A B C D E F	2.32	1.63 3.67 13.66 0.00 0.00 0.00	3.07 4.80 14.56 0.00 0.00 0.00	2.99 2.43 2.27 2.32 2.32 2.32
13	<b>入</b> ち ひ ヹ デ	2.85	3.38 17.45 0.00 0.00 0.00 0.00	5.11 18.98 0.00 0.00 0.00 0.00	3.15 2.65 2.85 2.85 2.85 2.85 2.85	26	A B C D E F	2.37	1.79 4.42 24.94 0.00 0.00 0.00	3.24 5.57 25.90 0.00 0.00 0.00	3.03 2.45 2.29 2.37 2.37 2.37

TABLE C.6 Experimental uncertainty estimates in the +5° [ upward ] data set

Run No.	Visual section	G %	r %	V <sub>32</sub> %	V.:: %	Run No.	Visual section	G %	X %	V.20 %	V.,2 %
27	λ B C	2.43	2.14 5.26 39.03	3.55 6.40 40.09	3.08 2.50 2.34	40	λ B	4.69	4.54	8.18	4.05 4.03 4.59
	D		0.00	0.00	2.63		D		0.00	0.00	4.69
	E		0.00	0.00	2.43		Z		0.00	0.00	4.69
	2		0.00	0.00	2.43		F		0.00	0.00	4.69
28	λ.	2.40	1,90	3.36	3.04	41	λ	4.48	6.52	9.80	3.90
	c		1095.31	1104.26	2.19		B C		0.00	0.00	4.48
	D		0.00	0.00	2.40		D		0.00	0.00	4.48
	E		0.00	0.00	2.40		2		0.00	0.00	4.48
29	r 3	2 20	0.00	0.00	2.40		2ª		0.00	0.00	6.60
.,	B	2.20	2.33	3.51	2.34	42	x	4.13	7.89	10.69	3.74
	с		5.78	6.67	2.20		в		0.00	0.00	4.13
	ם		1002.46	1008.16	2.09		c		0.00	0.00	4.13
	2		0.00	0.00	2.20		E		0.00	0.00	4.13
30	,	2 16	0 97	2 50	2 76		F		0.00	0.00	4.13
50	3	2.10	1.92	3.14	2.32	43	λ	4.07	12.69	15.31	3.68
	c		3.89	4.84	2.18		в		0.00	0.00	4.07
	D		15.09	15.78	2.13		C		0.00	0.00	4.07
	F		0.00	0.00	2.16		E		0.00	0.00	4.07
	-						F		0.00	0.00	4.07
31	λ	2.16	0.93	2.48	2.76			2.95	1 00	2.44	2 95
	c C		4.08	5.01	2.18	64	8	2.05	2.86	4.92	2.58
	D		0.00	0.00	2.05		ĉ		11.49	13.30	2.46
	E		0.00	0.00	2.16		a		0.00	0.00	2.85
	F		0.00	0.00	2.10		F		0.00	0.00	2.85
32	X	2.16	0.97	2.50	2.75						
	c		4.04	4.99	2.18	45	B	3.14	3.60	5.88	2.76
	D		30.92	31.60	2.13		č		12.31	14.40	2.64
	e F		0.00	0.00	2.16 2.16		D E		0.00	0.00	3.14 3.14
33	2	7 22	19 34	25 52	5 23		F		0.00	0.00	3.14
55	в		0.00	0.00	7.22	46	λ	2.98	1.89	4.12	3.04
	C		0.00	0.00	7.22		в		4.73	6.73	2.67
	D P		0.00	0.00	7.22		c		17.50	19.39	2.56
	7		0.00	0.00	7.22		E		0.00	0.00	2.98
34	2	7.05	36.68	43 15	5.05		P		0.00	0.00	2.98
	в		0.00	0.00	7.05	47	λ	2.98	1.84	4.08	3.05
	c		0.00	0.00	7.05		в		4.56	6.56	2.68
	D		0.00	0.00	7.05		C		30.22	32.19	2.98
	F		0.00	0.00	7.05		ž		0.00	0.00	2.98
35	λ	6.81	60.01	66.66	5.02		r.		0.00	0.00	2.30
	в		0.00	0.00	6.81	48	λ	3.33	1.37	4.16	3.19
	C D		0.00	0.00	6.81		3		3.41	5.94	2.86
	z		0.00	0.00	6.81		D		0.00	0.00	3.33
	F		0.00	0.00	6.81		E		0.00	0.00	3.33
36	3	5.88	14.08	19.95	4.96		P		0.00	0.00	3.33
20	в	0.00	0.00	0.00	6.88	49	λ	3.20	1.44	4.06	3.17
	c		0.00	0.00	6.88		в	· .	3.99	6.27	2.86
	2		. 0.00	0.00	6.88		ç		29.55	31.65	2.76
	F		0.00	0.00	6.88		E		0.00	0.00	3.20
37	λ	5.19	5.41	9.61	4.15		F		0.00	0.00	3.20
	в		0.00	0.00	5.19	50	λ	3.52	2.87	5.49	3.40
	c		0.00	0.00	5.19		в		12.67	14.94	3.08
	2		0.00	0.00	5.19		D D		0.00	0.00	3.52
	2		0.00	0.00	5.19		Z		0.00	0.00	3.52
38	λ	4.92	6.16	10.07	3.92		r		0.00	0.00	J.J.
	з		0.00	0.00	4.92	51	λ	3.52	2.23	4.96	3.42
	C		0.00	0.00	4.92		3		8.24	10.55	3.13
	E		0.00	0.00	4.92		G		0.00	0.00	3.52
	F		0.00	0.00	4.92		2		0.00	0.00	3.52
39	λ	4.48	8.21	11.47	3.79		F		0.00	v.vv	
	в		0.00	0.00	6.68	52	λ	2.10	0.93	2.40	2.75
	C D		0.00	0.00	4.48		č		3.60	4.45	2.17
	Z		0.00	0.00	4.48		ס		19.04	19.56	2.11
	F		0.00	0.00	4.48		E		0.00	0.00	2.10
							*				

TABLE C.6 Experimental uncertainty estimates in the +5° [ upward ] data set (cont'd.)

Run No.	Visual section	G %	r %	V.22 %	V_12 %	
53	λ	2.10	0.92	2.39	2.72	
	в		1.70	2.87	2.29	
	с		3.41	4.27	2.16	
	D		15.85	16.37	2.10	
	3		0.00	0.00	2.10	
	F		0.00	0.00	2.10	
54	λ	2.10	0.93	2.39	2.73	
	в		1.74	2.90	2.29	
	c		3.16	4.05	2.17	
	D		12.11	12.65	2.11	
	2		0.00	0.00	2.10	
	F		0.00	0.00	2.10	
55	,	2 10	1 01	2 44	2 74	
22	2	****	1 70	2 99	2 31	
	5		2.10	4.00	2.31	
	5		3.19	4.10	2.11	
	5		13.08	19.43	4.11	
	<u>ب</u>		0.00	0.00	2.10	
			0.00	0.00	2.10	

TABLE C.6 Experimental uncertainty estimates in the +5° [ upward ] data set (cont'd.)

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Run	Visual	G	x	V.72	VLa	Run	Visual	G	I	V.28	V.,
No.	section	*	%	*	*	No.	section	*	3	*	
1	λ	3.85	2.74	5.67	3.77	14	λ	2.50	1.76	3.41	2.95
	в		12.26	14.68	3.50		в		5.21	6.52	2-40
	c		0.00	0.00	3.85		c		0.00	0.00	2.50
	D		0.00	0.00	3.85		D		0.00	0.00	2.50
	E		0.00	0.00	3.85		E		0.00	0.00	2.50
	P		0.00	0.00	3.05		F		0.00	••••	
2	λ	3.64	3.71	6.27	3.61	15	λ	2.53	1.97	3.59	2.96
	в		19.62	21.82	3.32		в		5.53	6.85	2.48
	c		0.00	0.00	3.64		c		0.00	0.00	2 53
	D		0.00	0.00	3.04		D		0.00	0.00	2.53
	2		0.00	0.00	3.64		2		0.00	0.00	2.53
	÷		0.00								
3	λ	3.15	3.19	5.32	3.23	16	λ	2.53	1.55	3.31	2.94
	в		10.13	11.98	2.92		в		3.77	2.42	3.97
	c		0.00	0.00	3.15		c		28.70	10.00	2.53
	0		0.00	0.00	3 15		5		0.00	0.00	2.53
	2		0.00	0.00	3.15		P		0.00	0.00	2.53
	-						-				
4	Å	2.99	3.75	5.59	3.18	17	λ	2.45	1.36	3.08 5.10	2.43
	B		14.41	13.04	2.99		н		18 01	19.17	2.29
	5		0.00	0.00	2.99		2		0.00	0.00	2.45
	7		0.00	0.00	2.99		2		0.00	0.00	2.45
	P		0.00	0.00	2.99		F		0.00	0.00	2.45
								<b>•</b> / <b>-</b>		3 60	2 91
5	λ	3.20	4.01	6.06	3.30	18	Å	2.45	1.37	5.09	2.43
	в		15.72	17.52	2.33		3		14 77	15,92	2.30
	C		0.00	0.00	3.20		C n		0.00	0.00	2.45
	2		0.00	0.00	3.20		2		0.00	0.00	2.45
	P		0.00	0.00	3.20		F		0.00	0.00	2.45
											<b>2 1 1</b>
6	λ	3.22	7.01	8.82	3.32	19	λ	2.47	1.44	3.17	2.14
	в		167.27	170.10	2.99		3		13 79	14.99	2.31
	C		0.00	0.00	3.22		C D		0.00	0.00	2.47
	2		0.00	0.00	3.22		2		0.00	0.00	2.47
	F		0.00	0.00	3.22		P		0.00	0.00	2.47
_										2 1 9	2 91
7	λ	3.27	7.71	9.56	3.33	20	y	2.47	1.60	4 94	2.45
	8		0.00	0.00	3 27		8		9 65	10.88	2.32
			0.00	0.00	3.27		5		0.00	0.00	2.47
	2		0.00	0.00	3.27		R		0.00	0.00	2.47
	P		0.00	0.00	3.27		7		0.00	0.00	2.47
_	_						_		1 60	3 25	2.93
8	Å.	3.09	4.41	4.4/	2.40	21	A.	4.43	4.74	5.97	2.43
	ĉ		0.00	0.00	3.09		ĉ		214.15	216.15	2.29
	n		0.00	0.00	3.09		D D		0.00	0.00	2.43
	z		0.00	0.00	3.09		E		0.00	0.00	2.43
	P		0.00	0.00	3.09		F		0.00	0.00	2.43
	•			2 80	3 46			2.45	1 74	3 32	2.95
9	A	2.00	4.74	6.54	2.71	44	A a	2.43	4.91	6.16	2.44
	č		89.26	91.32	2.50		č		79.16	80.53	2.30
	â		0.00	0.00	2.88		ā		0.00	0.00	2.45
	Z		0.00	0.00	2.88		E		0.00	0.00	2.45
	F		0.00	0.00	2.88		F		0.00	0.00	4.43
10	λ	2.94	1.09	3.52	3.06	23	λ	2.20	1.20	2.66	2.81
	в		2.80	4.90	2.74		в		2.30	3.49	2.35
	c		10.05	11.81	2.64		с		5.48	6.38	2.20
	D		0.00	0.00	2.94		D		96.95	97.85	2.15
	2		0.00	0.00	2.94		Z		0.00	0.00	2.20
	e		0.00	0.00	4.33		r		0.00		
11	λ	2.85	1.79	3.89	3.00	24	λ	2.20	1.23	2.68	2.81
	з		4.04	5.88	2.67		в		2.42	3.58	2.34
	ç		18.02	19.66	2.55		ç		4.54	24 55	2.16
	D		0.00	0.00	2.03		D		0 00	0.00	2.20
	5 P		0.00	0.00	2.85		5		0.00	0.00	2.20
	•						•			<b>.</b>	
12	λ	2.82	2.13	4.10	2.99	25	λ	2.18	1.20	2.63	2.77
	в		4.82	6.55	2.67		в		2.09	3.29	2.34
	с		38.61	40.29	2.54		c		3.64	4.03	2.15
	5		0.00	0.00	4.04		D		71.13	0_00	2.18
	5 7		0.00	0,00	2.82		<u>ت</u>		0.00	0.00	2.18
	•						•			<u> </u>	
13	λ	2.82	1.80	3.85	3.01	26	λ	2.22	1.04	2.61	2.79
	в		4.18	5.96	2.67		в		2.13	5.91	2.21
	c		22.45	24.03	2.33		c		0.00	0.00	2.22
	ע ק		0.00	0.00	2.82		2		0.00	0.00	2.22
	5		0.00	0,00	2.82		÷ F		0.00	0.00	2.22
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TABLE C.7 Experimental uncertainty estimates in the +10° [ upward ] data set

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Run No.	Visual section	G %	X %	V	V.2 %	Run No.	Visual section	G %	X L	V <sub>22</sub> %	V.,,
27	A B C D E F	2.22	1.08 2.03 4.66 0.00 0.00 0.00	2.63 3.31 5.66 0.00 0.00 0.00	2.77 2.34 2.21 2.09 2.22 2.22	40	A B C D E F	2.11	0.98 1.89 3.34 7.17 0.00 0.00	2.44 3.03 4.24 7.85 0.00 0.00	2.73 2.30 2.17 2.12 2.11 2.11
28	A B C D Z F	2.18	0.98 1.74 3.55 17.43 0.00 0.00	2.52 3.04 4.57 18.15 0.00 0.00	2.75 2.33 2.19 2.13 2.18 2.18 2.18	41	Х В С D Z F	2.32	1.18 2.26 5.55 0.00 0.00 0.00	2.81 3.66 6.71 0.00 0.00 0.00	2.80 2.36 2.22 2.32 2.32 2.32 2.32
29	A B C D E F	2.21	1.11 1.99 4.00 16.70 0.00 0.00	2.63 3.27 5.03 17.48 0.00 0.00	2.78 2.34 2.21 2.15 2.21 2.21	42	A B C D E F	2.30	0.96 2.01 4.71 0.00 0.00 0.00	2.68 3.46 5.91 0.00 0.00 0.00	2.77 2.33 2.20 2.09 2.30 2.30
30	λ Β Ο Σ F	2.20	0.93 1.65 3.18 10.18 0.00 0.00	2.53 3.02 4.29 11.02 0.00 0.00	2.71 2.32 2.19 2.14 2.20 2.20	43	A B C D E F	2.32	1.00 1.82 3.92 38.32 0.00 0.00	2.72 3.33 5.20 39.48 0.00 0.00	2.77 2.35 2.22 2.16 2.32 2.32
31	A B C D E F	2.15	0.97 1.82 3.73 140.26 0.00 0.00	2.49 3.06 4.68 141.15 0.00 0.00	2.73 2.32 2.18 2.12 2.15 2.15	44	a B C D E F	2.33	0.94 1.69 3.65 30.68 0.00 0.00	2.71 3.26 4.98 31.84 0.00 0.00	2.77 2.36 2.22 2.16 2.33 2.33
32	A B C D E F	2.15	0.96 1.81 3.73 22.94 0.00 0.00	2.48 3.05 4.68 23.59 0.00 0.00	2.74 2.32 2.18 2.12 2.15 2.15	45	х в с <b>р</b> в г	2.30	1.67 4.70 0.00 0.00 0.00 0.00	3.08 5.72 0.00 0.00 0.00 0.00	2.96 2.42 2.30 2.30 2.30 2.30 2.30
33	A B C D E F	2.15	0.98 1.83 3.78 14.41 0.00 0.00	2.49 3.06 4.71 15.07 0.00 0.00	2.72 2.31 2.18 2.12 2.15 2.15	46	A B C D E F	2.30	1.89 4.23 28.71 0.00 0.00 0.00	3.23 5.28 29.54 0.00 0.00 0.00	2.99 2.44 2.27 2.30 2.30 2.30
34	A B C D E F	2.15	0.98 1.85 3.49 11.35 0.00 0.00	2.48 3.07 4.45 12.04 0.00 0.00	2.74 2.31 2.18 2.13 2.15 2.15	47	λ B C D Z F	2.32	1.50 3.77 24.82 0.00 0.00 0.00	2.99 4.90 25.71 0.00 0.00 0.00	2.95 2.42 2.26 2.32 2.32 2.32
35	A B C D E F	2.12	0.90 1.65 3.39 49.95 0.00 0.00	2.41 2.88 4.32 50.54 0.00 0.00	2.69 2.29 2.16 2.10 2.12 2.12	48	λ B C D E F	2.32	1.54 4.05 39.70 0.00 0.00 0.00	3.02 5.16 40.64 0.00 0.00 0.00	2.92 2.40 2.24 2.32 2.32 2.32
36	A B C D E F	2.12	0.94 1.79 4.17 485.77 0.00 0.00	2.42 2.97 5.00 487.56 0.00 0.00	2.72 2.30 2.16 2.08 2.12 2.12	49	እ ይ ር ይ ያ	2.62	1.79 4.96 110.01 0.00 0.00 0.00	3.59 6.48 112.03 0.00 0.00 0.00	2.96 2.50 2.36 2.62 2.62 2.62
37	A B C D Z F	2.11	0.94 1.79 4.14 47.56 0.00 0.00	2.42 2.96 4.96 48.10 0.00 0.00	2.72 2.30 2.16 2.10 2.11 2.11	50	Х ВС D E F	2.62	2.09 5.99 180.40 0.00 0.00 0.00	3.80 7.43 182.85 0.00 0.00 0.00	2.99 2.52 2.38 2.62 2.62 2.62 2.62
38	A B C D E F	2.11	0.95 1.82 3.82 26.66 0.00	2.42 2.98 4.67 27.19 0.00 0.00	2.72 2.30 2.16 2.11 2.11	51	<b>入</b> 日 で ロ ジ ア	2.62	1.78 4.94 45.28 0.00 0.00 0.00	3.59 6.46 47.85 0.00 0.00 0.00	2.96 2.50 2.37 2.62 2.62 2.62
39	A B C D Z F	2.12	0.99 1.92 3.80 16.28 0.00 0.00	2.44 3.06 4.66 15.84 0.00 0.00	2.75 2.31 2.17 2.11 2.12 2.12	52	א פ פ פ פ	2.45	1.77 4.76 52.77 0.00 0.00 0.00	3.34 6.02 54.02 0.00 0.00 0.00	2.95 2.44 2.30 2.45 2.45 2.45

# TABLE C.7 Experimental uncertainty estimates in the +10° [ upward ] data set (cont'd.)

4.

### Appendix D

### THE ANALYSIS OF STRATIFIED-NONSTRATIFIED TRANSITION DURING CONDENSATION BY WAVE THEORY

The one dimensional, co-current stratified flow configuration in an inclined condenser tube is shown in Figure 5.1. Considering this flow configuration and applying the one dimensional two-fluid transient conservation laws, the resulting continuity and momentum equations are,

$$\rho_L \frac{\partial}{\partial t} < 1 - \alpha > + \rho_L \frac{\partial}{\partial Z} (< 1 - \alpha > < u_L > L) = \dot{W}_i, \qquad (D.1)$$

$$\rho_{G} \frac{\partial}{\partial t} <\alpha > + \rho_{G} \frac{\partial}{\partial Z} (<\alpha > < u_{G} >_{G}) = -\dot{W}_{i} , \qquad (D.2)$$

$$\rho_{L}\frac{\partial}{\partial t} \langle u_{L} \rangle_{L} + \frac{\rho_{L} \langle u_{L} \rangle_{L}}{\langle 1 - \alpha \rangle} \frac{\partial}{\partial t} \langle 1 - \alpha \rangle + \frac{C_{3L} \langle u_{L} \rangle_{L}}{\langle 1 - \alpha \rangle} \dot{W}_{i}$$

$$- \frac{C_{3L}\rho_{L} \langle u_{L} \rangle_{L}}{\langle 1 - \alpha \rangle} \frac{\partial}{\partial t} \langle 1 - \alpha \rangle + C_{3L}\rho_{L} \langle u_{L} \rangle_{L} \frac{\partial}{\partial Z} \langle u_{L} \rangle_{L}$$

$$+ \frac{\tau_{L}S_{L}}{A \langle 1 - \alpha \rangle} - \frac{\tau_{i}S_{i}}{A \langle 1 - \alpha \rangle} + \rho_{L}g \sin\theta + \frac{\partial P_{iL}}{\partial Z} + \rho_{L}g \cos\theta \frac{\partial h_{L}}{\partial Z}$$

$$- \frac{\dot{W}_{i}}{\langle 1 - \alpha \rangle} [\eta \langle u_{L} \rangle_{L} + (1 - \eta) \langle u_{G} \rangle_{G}] = 0 , \qquad (D.3)$$

and
$$\rho_{G} \frac{\partial}{\partial t} \langle u_{G} \rangle + \frac{\rho_{G} \langle u_{G} \rangle_{G}}{\langle \alpha \rangle} \frac{\partial}{\partial t} \langle 1 - \alpha \rangle - \frac{C_{3G} \langle u_{G} \rangle_{G}}{\alpha} \dot{W}_{i}$$

$$- \frac{C_{3G} \rho_{G} \langle u_{G} \rangle_{G}}{\alpha} \frac{\partial}{\partial t} \langle \alpha \rangle + C_{3G} \rho_{G} \langle u_{G} \rangle_{G} \frac{\partial}{\partial Z} \langle u_{G} \rangle_{G}$$

$$+ \frac{\tau_{G} S_{G}}{A \langle \alpha \rangle} + \frac{\tau_{i} S_{i}}{A \langle \alpha \rangle} + \rho_{G} g \sin \theta + \frac{\partial P_{iG}}{\partial Z} + \rho_{G} g \cos \theta \frac{\partial h_{L}}{\partial Z}$$

$$+ \frac{\dot{W}_{i}}{\langle \alpha \rangle} [\eta \langle u_{L} \rangle_{L} + (1 - \eta) \langle u_{G} \rangle_{G}] = 0 , \qquad (D.4)$$

where  $P_{iL}$  is the interfacial pressure experienced by the liquid,  $P_{iG}$  is the interfacial pressure on the vapor and t is time. All the other variables were defined in Chapter 6.

Substituting Equations (D.1) and (D.2) into Equations (D.3) and (D.4) respectively to eliminate  $\partial/\partial t(\langle \rho_{\rm G} \langle \alpha \rangle)$  and  $\partial/\partial t(\langle \rho_{\rm L} \langle 1 - \alpha \rangle)$  and subtracting Equation (D.3) from (D.4),

$$\begin{bmatrix} \rho_{L}(1 - C_{3L}) \frac{\langle u_{L} \rangle_{L}}{A_{L}} + \rho_{G}(1 - C_{3G}) \frac{\langle u_{G} \rangle_{G}}{A_{G}} \end{bmatrix} \frac{dA_{L}}{dh_{L}} \frac{\partial h_{L}}{\partial t} \\ + (\rho_{L} - \rho_{G})g\cos\theta \frac{\partial h_{L}}{\partial Z} + \frac{(\partial P_{iL} - \partial P_{iG})}{\partial Z} + \rho_{L} \frac{\partial \langle u_{L} \rangle_{L}}{\partial t} \\ \rho_{L} \langle u_{L} \rangle_{L} C_{3L} \frac{\partial \langle u_{L} \rangle_{L}}{\partial Z} - \rho_{G} \frac{\partial \langle u_{G} \rangle_{G}}{\partial t} - \rho_{G} \langle u_{G} \rangle_{G} C_{3G} \frac{\partial \langle u_{G} \rangle_{G}}{\partial Z} = \Delta f_{ab} , \quad (D.5) \end{bmatrix}$$

where

$$\Delta f_{ab} = -\frac{\tau_L S_L}{A_L} + \tau_I S \left[ \frac{1}{A_L} + \frac{1}{A_G} \right] + \frac{\tau_G S_G}{A_G} - (\rho_L - \rho_G) g \sin\theta$$

$$\left\{ \left( \eta \left[ \frac{1}{A_G} + \frac{1}{A_L} \right] - \frac{C_{3G}}{A_L} \right] u_L + \left( (1 - \eta) \left[ \frac{1}{A_G} + \frac{1}{A_L} \right] - \frac{C_{3G}}{A_G} \right] u_G \right\} \frac{\dot{W}_I}{A} . \quad (D.5a)$$

The effect of surface tension,  $\sigma$  is assumed to cause a difference in the interfacial pressures ( $P_{iL} \neq P_{iG}$ ) experienced by the two phases where

$$\frac{(\partial P_{iL} - \partial P_{iG})}{\partial Z} = -\frac{\partial}{\partial Z} \left[ \sigma \frac{\frac{\partial^2 h_L}{\partial Z^2}}{\left[1 + \left(\frac{\partial h_L}{\partial Z}\right)^2\right]^{3/2}} \right].$$
 (D.5b)

The analysis of instability and the transitional criteria are obtained by linearizing Equations (D.1), (D.2) and (D.5) around a smooth fully-developed stratified flow pattern ( $H_L$ ,  $U_L$ ,  $U_G$ ) where the instantaneous phase averaged velocities are perturbed using the following:

The parameters  $H_L$ ,  $U_L$ ,  $U_G$ , and  $\Delta F_{ab}$  are obtained by solving the steady stratified flow equation for a given flow rate. The steady flow equations obtained from the present analysis are exactly the same equations as in Chapter 5. Substituting the terms given in Equation (D.6) into Equations (D.1), (D.2) and (D.5) and performing the required differentiations two set of equations are obtained. One set describes the equilibrium steady stratified flow and the other set describing the perturbed unsteady flow. The perturbed set of equations are linearized by neglecting terms such as

$$h_L^* | H_L \ll 1$$
,  
 $u_L^* | U_L \ll 1$ , (D.7)  
 $u_G^* | U_G \ll 1$ ,

and the time variation of the steady state parameters for small perturbations. These parameters are small and do not provide any significant contributions to the resulting equations. Hence they are neglected.

The equilibrium condition in the flow field is described by,

$$\left(K\frac{\partial}{\partial Z}\right)\phi = I \tag{D.8}$$

where

$$K = \begin{bmatrix} \frac{dA_L}{dh_L}U_L & A_L & 0\\ A_LU_G & 0 & -A_G\\ (\rho_L - \rho_G)g\cos\theta - \sigma \frac{\partial^2}{\partial Z^2} & \rho_LU_LC_{3L} & -\rho_GU_GC_{3G} \end{bmatrix}, (D.8a)$$

$$I = \begin{bmatrix} \frac{\dot{W}_{i}}{A\rho_{L}} \\ \frac{\dot{W}_{i}}{A\rho_{G}} \\ \Delta F_{ab} \end{bmatrix}, \qquad (D.8b)$$

$$\phi = \begin{bmatrix} H \\ U_{L} \\ U_{G} \end{bmatrix}. \qquad (D.8c)$$

and

The linerized forms of the perturbed equations are given by

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$$\left(T\frac{\partial}{\partial t} + \bar{R}\frac{\partial}{\partial Z}\right)B = \hat{F}B \tag{D.9}$$

where

$$T = \begin{vmatrix} \frac{dA_L}{dh_L} & 0 & 0 \\ \frac{dA_L}{dh_L} & 0 & 0 \\ N & \rho_L & -\rho_G \end{vmatrix}, \qquad (D.9a)$$

$$\vec{R} = \begin{bmatrix} \frac{dA_L}{dh_L}U_L & A_L & 0\\ \frac{dA_L}{dh_L}U_G & 0 & -A_G\\ \vec{G} & \rho_L C_{3L}U_L & -\rho_G C_{3G}U_G \end{bmatrix}, \qquad (D.9b)$$

$$\begin{bmatrix} \left(\frac{\partial \dot{W}_I}{\partial H_L}\right) \frac{1}{A\rho_L} & 0 & 0 \end{bmatrix}$$

-

$$\hat{F} = \begin{pmatrix} \frac{\partial \dot{W}_i}{\partial H_L} \frac{1}{A\rho_G} & 0 & 0 \\ \frac{\partial \Delta F_{ab}}{\partial H_L} & \frac{\partial \Delta F_{ab}}{\partial U_L} & \frac{\partial \Delta F_{ab}}{\partial U_G} \end{pmatrix}, \quad (D.9c)$$

$$B = \begin{bmatrix} h_L^{\star} \\ u_L^{\star} \\ u_G^{\star} \end{bmatrix}, \qquad (D.9d)$$

$$\overline{G} = (\rho_L - \rho_G)g\cos\theta - \sigma \frac{\partial^2}{\partial Z^2}, \qquad (D.10a)$$

$$N = \left[\rho_L (1 - C_{3L}) \frac{U_L}{A_L} + \rho_G (1 - C_{3G}) \frac{U_G}{A_G} \right] \frac{dA_L}{dh_L} , \qquad (D.10b)$$

$$\frac{\partial \Delta F_{ab}}{\partial H_L} = \frac{\partial \Delta f_{ab}}{\partial h_L} \bigg|_{h_L} = H_L, \qquad (D.10c)$$

and

$$\frac{\partial \Delta F_{ab}}{\partial U_j} = \frac{\partial \Delta f_{ab}}{\partial u_j} \bigg|_{u_j} = U_j , \quad j = L, G.$$
 (D.10d)

The stability analysis is performed by substituting a standard form of perturbation into the linearized perturbed equation, i.e Equation(D.9)

$$h_{L}^{\star} = \hat{h}_{L} \Theta^{i} (kZ - \omega t) ,$$

$$u_{L}^{\star} = \hat{u}_{L} \Theta^{i} (kZ - \omega t) , \text{ and}$$

$$u_{G}^{\star} = \hat{u}_{G} \Theta^{i} (kZ - \omega t)$$
(D.11)

where k is the real wave number,  $\omega$  is the complex angular velocity, i is  $\sqrt{-1}$ , and  $\hat{h}$ ,  $\hat{u}_L$ , and  $\hat{u}_G$  are complex amplitudes of the perturbation. When these terms are substituted Equation (D.9) becomes,

$$M\hat{B} = 0 \tag{D.12}$$

where

$$\hat{\boldsymbol{B}} = \begin{bmatrix} \hat{\boldsymbol{h}}_L \\ \hat{\boldsymbol{u}}_L \\ \hat{\boldsymbol{u}}_G \end{bmatrix}, \quad (D.12a)$$

$$M = \begin{bmatrix} \frac{dA_L}{dh_L} \frac{1}{A_L} \left[ -\frac{\omega}{k} + U_L + \left( \frac{\partial \dot{W}_i}{\partial H_L} \right) \left( \frac{dh_L}{dA_L} \right) \frac{i}{k\rho_L A} \right] & 1 & 0 \\ \frac{dA_L}{dh_L} \frac{1}{A_G} \left[ \frac{\omega}{k} - U_G - \left( \frac{\partial \dot{W}_i}{\partial H_L} \right) \left( \frac{dh_L}{dA_L} \right) \frac{i}{k\rho_G A} \right] & 0 & 1 \\ M_1 & M_2 & M_3 \end{bmatrix},$$
 (D.12b)

for comes

$$M_1 = -\frac{N\omega}{k} + (\rho_L - \rho_G)g\cos\theta + \sigma k^2 + \frac{i}{k}\frac{\partial\Delta F_{ab}}{\partial H_L}, \qquad (D.13a)$$

$$M_2 = -\frac{\rho_L \omega}{k} + \rho_L U_L C_{3L} + \frac{i}{k} \frac{\partial \Delta F_{ab}}{\partial U_L} , \qquad (D.13b)$$

$$M_3 = \frac{\rho_G \omega}{k} - \rho_G U_G C_{3G} + \frac{i}{k} \frac{\partial \Delta F_{ab}}{\partial U_G} . \qquad (D.13c)$$

For non-trivial solutions det M = 0 from where the dispersion equation is obtained. The dispersion equation is given by,

$$aC^2 - 2(b_1 + ib_2)C + d_1 + id_2 = 0$$
 (D.14)

where

$$C = \frac{\omega}{k} , \qquad (D.14a)$$

$$a = \frac{dA_L}{dh_L}\frac{\rho_L}{A_L} + \frac{dA_L}{dh_L}\frac{\rho_G}{A_G}, \qquad (D.14b)$$

$$b_1 = \rho_L \frac{dA_L}{dh_L} \left(1 + \frac{(C_{3L} - 1)}{2}\right) \frac{U_L}{A_L} + \rho_G \frac{dA_L}{dh_L} \left(1 + \frac{(C_{3G} - 1)}{2}\right) \frac{U_G}{A_G} - \frac{1}{2}N, \quad (D.14c)$$

and

$$b_{2} = \frac{1}{2k} \left( \frac{dA_{L}}{dh_{L}} \frac{1}{A_{L}} \frac{\partial \Delta F_{ab}}{\partial U_{L}} - \frac{dA_{L}}{dh_{L}} \frac{1}{A_{G}} \frac{\partial \Delta F_{ab}}{\partial U_{G}} + \left[ \frac{1}{A_{G}} + \frac{1}{A_{L}} \right] \frac{\partial \dot{W}_{i}}{\partial H_{L}} \frac{1}{A} \right), \quad (D.14d)$$

$$d_{1} = \frac{\rho_{L}C_{3L}U_{L}^{2}}{A_{L}} \frac{dA_{L}}{dh_{L}} + \frac{\rho_{G}C_{3G}U_{G}^{2}}{A_{G}} \frac{dA_{L}}{dh_{L}}$$

$$- \left\{ (\rho_{L} - \rho_{G})g\cos\theta + \sigma k^{2} \right\}$$

$$+ \left( \frac{\partial \dot{W}_{i}}{\partial H_{L}} \right) \frac{1}{Ak^{2}} \left\{ \frac{1}{\rho_{G}A_{G}} \frac{\partial \Delta F_{ab}}{\partial U_{G}} - \frac{1}{\rho_{L}A_{L}} \frac{\partial \Delta F_{ab}}{\partial U_{L}} \right\}, \quad (D.14e)$$

and

$$d_{2} = \frac{1}{k} \left( \frac{dA_{L}}{dh_{L}} \frac{U_{L}}{A_{L}} \frac{\partial \Delta F_{ab}}{\partial U_{L}} - \frac{dA_{L}}{dh_{L}} \frac{U_{G}}{A_{G}} \frac{\partial \Delta F_{ab}}{\partial U_{G}} - \frac{\partial \Delta F_{ab}}{\partial H_{L}} + \frac{1}{A} \left( \frac{\partial \dot{W}_{i}}{\partial H_{L}} \right) \left( \frac{U_{G}C_{3G}}{A_{G}} + \frac{U_{L}C_{3L}}{A_{L}} \right) \right) . (D.14\hbar)$$

The neutral stability condition is obtained when the imaginary quantities in Equation (D.14) become equal to zero. Then

$$C_m = \frac{d_2}{2b_2}$$
 (D.15)

Substituting the values of  ${\rm d_2}$  and  ${\rm b_2},$ 

$$C_{m} = \frac{\frac{dA_{L}}{dh_{L}}\frac{U_{L}}{A_{L}}\frac{\partial\Delta F_{ab}}{\partial U_{L}} - \frac{dA_{L}}{dh_{L}}\frac{U_{G}}{A_{G}}\frac{\partial\Delta F_{ab}}{\partial U_{G}} - \frac{\partial F_{ab}}{\partial H_{L}} + \frac{1}{A} \left(\frac{\partial\dot{W}_{i}}{\partial H_{L}}\right) \left(\frac{U_{G}C_{3G}}{A_{G}} + \frac{U_{L}C_{3L}}{A_{L}}\right)}{\frac{1}{A_{L}}\frac{dA_{L}}{dh_{L}}\frac{\partial\Delta F_{ab}}{\partial U_{L}} - \frac{1}{A_{G}}\frac{dA_{L}}{dh_{L}}\frac{\partial\Delta F_{ab}}{\partial U_{G}} + \frac{1}{A} \left[\frac{1}{A_{G}} + \frac{1}{A_{L}}\right] \left(\frac{\partial\dot{W}_{i}}{\partial H}\right)}{\frac{1}{A_{L}}\frac{\partial\dot{W}_{i}}{\partial H_{L}}\frac{\partial\Delta F_{ab}}{\partial U_{L}} - \frac{1}{A_{G}}\frac{dA_{L}}{dh_{L}}\frac{\partial\Delta F_{ab}}{\partial U_{G}} + \frac{1}{A} \left[\frac{1}{A_{G}} + \frac{1}{A_{L}}\right] \left(\frac{\partial\dot{W}_{i}}{\partial H}\right)}$$
(D.15a)

Substituting the value of  $C_{rn}$  in Equation (D.14) the equation of stable equilibrium is obtained.

$$\left(\frac{\rho_L}{A_L}\frac{dA_L}{dh_L} + \frac{\rho_G}{A_G}\frac{dA_L}{dh_L}\right)C_m^2 - 2\left(\frac{\rho_L C_{3L}U_L}{A_L}\frac{dA_L}{dh_L} + \frac{\rho_G C_{3G}U_G}{A_G}\frac{dA_L}{dh_L}\right)C_m + \frac{\rho_L C_{3L}U_L^2}{A_L}\frac{dA_L}{dh_L} + \frac{\rho_G C_{3G}U_G^2}{A_G}\frac{dA_L}{dh_L} - \left\{(\rho_L - \rho_G)g\cos\theta + \sigma k_n^2\right\} + \frac{1}{A_K_n^2}\left(\frac{\partial \dot{W}_I}{\partial H_L}\right)\left\{\frac{1}{\rho_G A_G}\frac{\partial \Delta F_{ab}}{\partial U_G} - \frac{1}{\rho_L A_L}\frac{\partial \Delta F_{ab}}{\partial U_L}\right\} = 0.$$
(D.16)

This dimensionless form of this equation is,

$$\frac{\pi^{2}}{16gD\cos\theta} \left\{ \frac{\rho_{G}U_{GS}^{2}}{\rho_{L}\overline{A}_{G}^{3}} \left( \frac{d\overline{A}_{L}}{d\overline{h}_{L}} \right) \left[ \left( \frac{C_{m}}{U_{G}} - 1 \right)^{2} + (C_{3G} - 1) \left( 1 - 2\frac{C_{m}}{U_{G}} \right) \right] \right\}$$

$$\left\{ + \frac{U_{LS}^{2}}{\overline{A}_{L}^{3}} \left( \frac{d\overline{A}_{L}}{d\overline{h}_{L}} \right) \left[ \left( \frac{C_{m}}{U_{L}} - 1 \right)^{2} + (C_{3L} - 1) \left( 1 - \frac{2C_{m}}{U_{L}} \right) \right] \right\}$$

$$- \left[ \frac{(\rho_{L} - \rho_{G})}{\rho_{L}} + \frac{\sigma k_{n}^{2}}{\rho_{L}g\cos\theta} - \frac{\partial \dot{W}/\partial H_{L}}{D^{2}k_{n}^{2}A\rho_{L}g\cos\theta} \left\{ \frac{1}{\rho_{G}\overline{A}_{G}} \frac{\partial \Delta F_{ab}}{\partial U_{G}} - \frac{1}{\rho_{L}\overline{A}_{L}} \frac{\partial \Delta F_{ab}}{\partial U_{L}} \right\} \right] = 0.(D.17)$$

The last term in Equation (D.17) is the contribution due to condensation during the flow. If the last term in Equation (D.17) becomes zero (adiabatic) then the analysis must yield the gas-liquid transition boundary given by Brauner and Maron(1991). The results obtained with the properties of air and water under adiabatic conditions are given in Figure D.1. These are exactly the same as reported by Brauner and Maron(1991). In Figure D.2 the predictions of Equation (D.17) are compared (diabatic flow) with horizontal







steam-water data of 0.0134m I. D. tube. The predictions show similar trends as the mechanistic model described in Chapter 5.